

TRISEP 2024 - The Standard Model

Class Worksheet

Stephen Sekula

1 Day 1

If you need to look up numbers (e.g., masses, fundamental constants) please use the Particle Data Group website (pdg.lbl.gov). Their interactive tables are an excellent source of data (pdglive.lbl.gov).

1.1 Estimating Nuclear Energy Scales

Nuclear processes often emit photons, which we would associate with the movement of electric charge within the nucleus. We wish to estimate the energy scale of nuclear interactions using a purely classical calculation. Imagine a tritium nucleus (one proton and two neutrons) into which you then bring a proton to form a helium nucleus. Assume you are bringing the proton from an infinite distance away and placing it so that the centres of the two protons are 1 fm apart.

- Estimate the work required to assemble these charges in this way. *This provides a very rough classical estimate of the energy scale associated with the nucleus (e.g., the potential energy stored in the electromagnetic field, which could be converted into other forms of energy).*
- **BONUS:** estimate the wavelength of a photon that could be released from a nuclear process after calculating the above work (here, you are free to use modern physics). What class of photon is this? (*radio, infrared, visible, uv, x-ray, gamma ray*)

1.2 Converting mass units

Using Einstein's relation between mass, energy, and momentum, compute the rest mass of the electron in units of MeV/c^2 starting from the MKS value, $m_e = 9.109 \times 10^{-31}$ kg.

1.3 Beta Decay of Free Neutron

Consider a free neutron at rest. Beta decay is the emission of a fast-moving electron from a nuclear process. Let us hypothesize that the neutron decays as $n^0 \rightarrow p^+e^-$ (this conserves electric charge and was a reasonable first guess for this process in the early 1900s). What will be the kinetic energy of the electron? You should use relativistic mechanics to do this calculation.

1.4 Muon Lifetime and Survival

The famous "Mount Washington" or "Frisch-Smith" experiment used an apparatus to observe cosmic ray muons at high altitude (atop Mt. Washington). The experiment observed 563 muons per hour at an altitude of 1917 m above sea level. The same experiment measured 412 muons per hour at sea level. The experiment was designed to sample muons with velocities between $0.9950c$ and $0.9954c$. The mean lifetime of the muon measured at rest with respect to the muon is $2.1969811 \mu\text{s}$.

- Using a perfectly classical calculation (ignore special relativity), how many muons SHOULD the experiment have measured at sea level?

- Now using special relativity, estimate the number of muons the experiment was expected to measure at sea level.
- Compare the latter calculation to the observed numbers. Comment on any uncertainties based on information given in the problem.

1.5 Fitting the Muon Lifetime

A data set from a muon decay experiment is available online. This is real data from the instrument depicted in the slides and operated for many years at Southern Methodist University in Dallas, TX. The data represents continuous data-taking from about 4 months in 2020.

Download this data and, using your favourite software framework (Excel, Python, C++, etc.) determine the observed lifetime of the muon assuming that the data can be described by a simple model involving both real muon decay coincidences (a stopping muon energy pulse followed by the muon decay energy pulse) and random noise coincidences in the instrument (which should be uniformly distributed in time),

$$P(t) = Ae^{-t/\tau} + B.$$

- Determine the three parameters - A, B, and τ - by fitting the model to the data (using a least-squares, maximum likelihood, etc. approach).
- Compare your result for τ to the accepted value, 2.1969811 μ s. Comment on your observation(s).

Format of the Data and Important Comments The data is formatted into a file with two columns. The first column is the time between the two pulses in nanoseconds. The second column is the timestamp of the event in UNIX time. You should not need the second column.

The maximum time between pulses in this instrument is 20000 ns. If the experiment counts to 20000 ns after the initial (trigger) pulse, it times out and stores that timeout as a muon decay candidate with exactly 20000 ns of lifetime. This is unphysical. *However, timeout events have already been eliminated from the dataset. You should use data from 1000-20000 in your fit.*