

Neutrinoless Double Beta Decay

$0\nu\beta\beta$ – part 2

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TRISEP 2024, Sudbury



Outline

Lecture 1

- What is double beta decay?
 - SEMF splitting
 - Known isotopes
- 2 neutrino double beta decay
- Neutrinoless double beta decay
 - Theory
 - Dirac and Majorana neutrinos
 - See-saw mechanism

Lecture 2

- Half-life / rate
 - Phase space
 - Matrix elements
- Experimental considerations
 - Challenges
 - Backgrounds
- Experiment examples

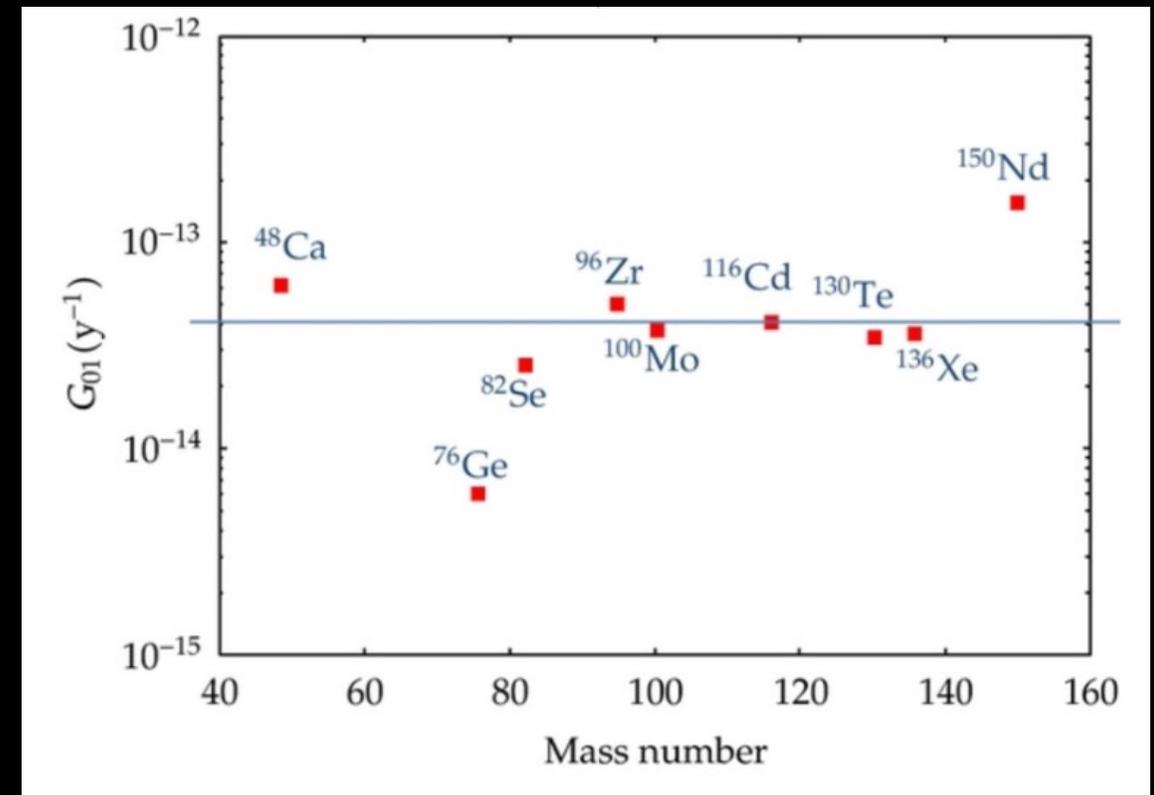
Lecture 3

- Neutrino mass
- Lobster plots
- Limits vs Discovery
- Alternative mechanisms and probing new physics
- $\beta^+ \beta^+$ decays
- Future prospects

$0\nu\beta\beta$ Rate

$$\left(t_{0\nu}^{1/2}\right)^{-1} = G^{0\nu} g_A^4 |M^{0\nu}|^2 \langle m_{\beta\beta} \rangle^2$$

- $G^{0\nu}$ phase space factor
 - Dependent on nucleus (Z and Q-value)
 - Directly calculable
- $g_A^4 =$ axial coupling constant
 - Free nucleon value $g_A = 1.27$
 - Quenching due to multinucleon effects

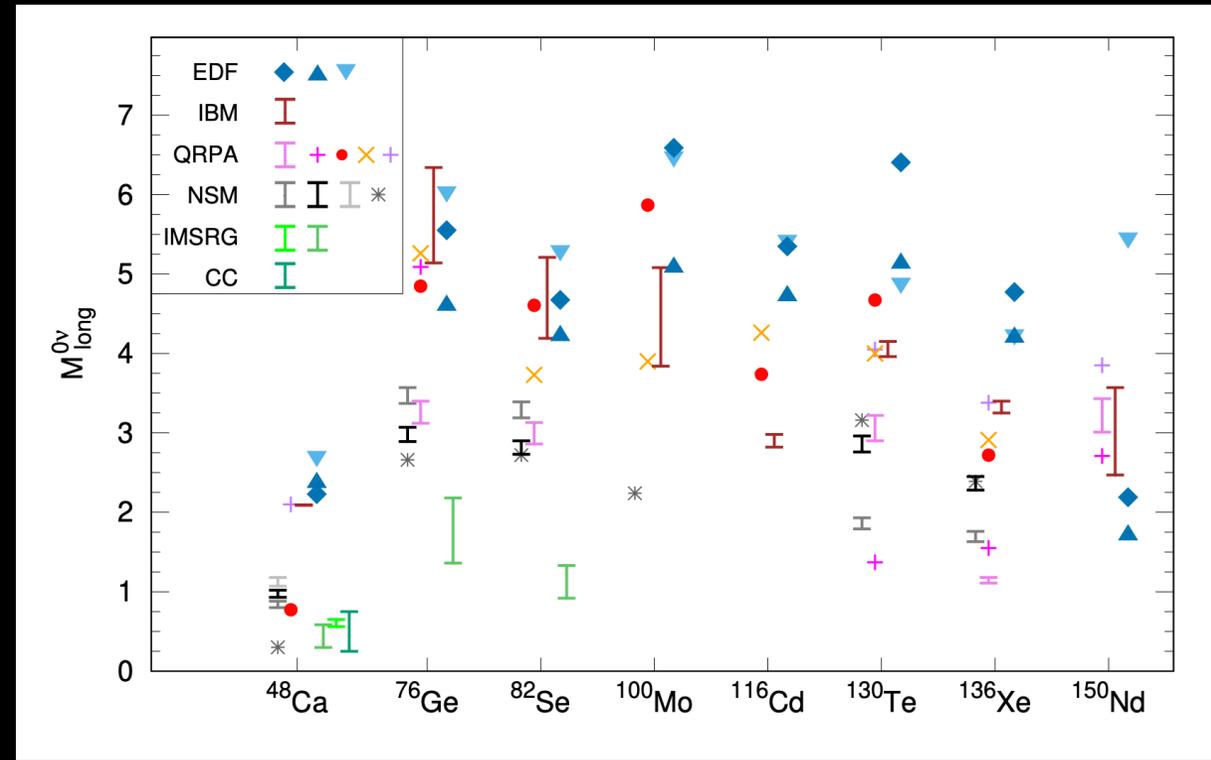


typical values $G^{0\nu} \sim 10^{-14} y^{-1}$

$0\nu\beta\beta$ Rate

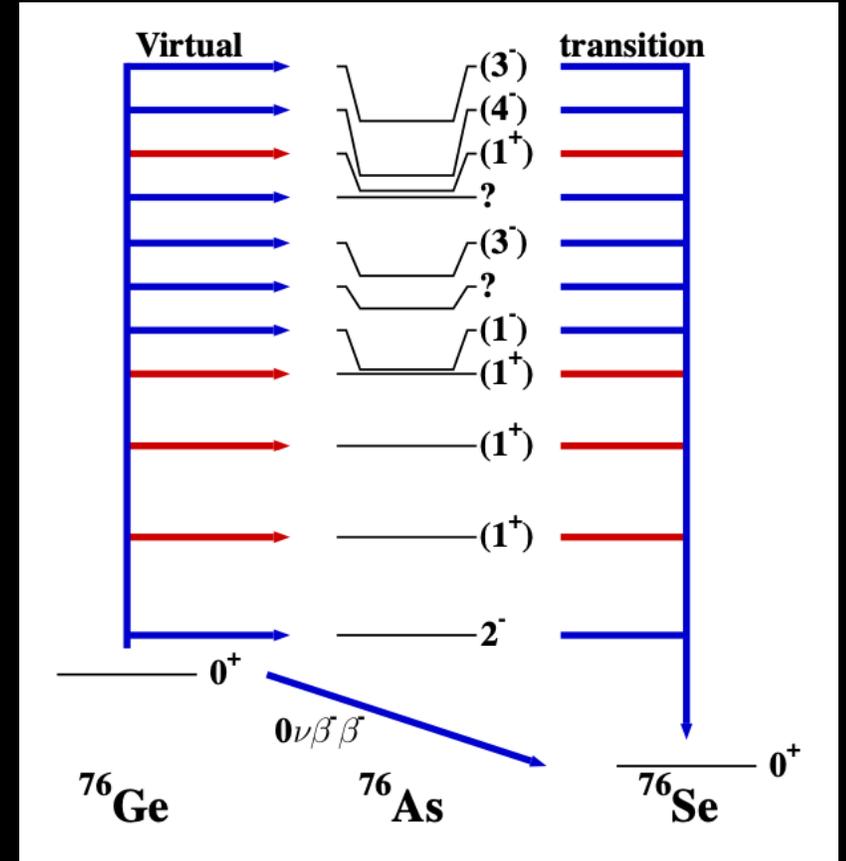
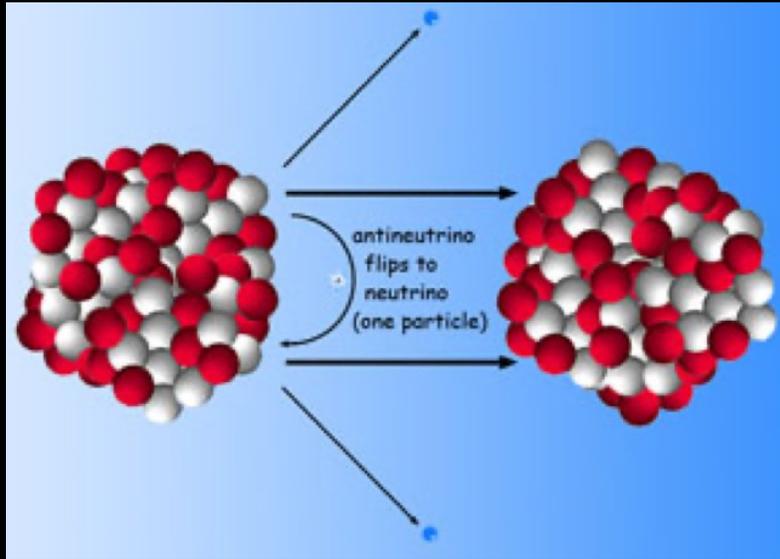
$$\left(t_{0\nu}^{1/2}\right)^{-1} = G^{0\nu} g_A^4 \left|M^{0\nu}\right|^2 \langle m_{\beta\beta}\rangle^2$$

- $|M^{0\nu}|^2 =$ nuclear matrix element
 - Depends on nuclear structure of parent, daughter and intermediate nuclei
 - Very computationally intensive to calculate – requires model approximations
 - Factor 4 variation between models \rightarrow 2 order mag variation in predicted half-life for given $\langle m_{\beta\beta}\rangle^2$



Agostini et al, Rev Mod Phys 95 025002 (2023)
<https://arxiv.org/abs/2202.01787>

Nuclear Matrix Element Calculations



- Initial state consists of $\mathcal{O}(100)$ nuclei
- Final state consists of $\mathcal{O}(100)$ nuclei + electrons
- Via large number of potential intermediate states
- Short range correlations? Quenching?
- Computationally infeasible without model assumptions
- Some aspects of models can be tested with $2\nu\beta\beta$ measurements (but not all)

$0\nu\beta\beta$ Rate

$$\left(t_{0\nu}^{1/2}\right)^{-1} = G^{0\nu} g_A^4 |M^{0\nu}|^2 \langle m_{\beta\beta} \rangle^2$$

$$\langle m_{\beta\beta} \rangle = \left| \sum_i U_{ei}^2 m_i \right|$$

Square of the effective Majorana mass
See lecture 3

$0\nu\beta\beta$ Rate

- Looking at half-lives $T_{1/2} > 10^{25}$ years and longer
- Very rare decays:
 - Need a lot of candidate isotopes
 - Need to measure for a long time

$$N_{iso} = m \times a \times N_A$$

Mass of element (points to m)
Isotopic abundance (points to a)
Avogadro's Number $\sim 6 \times 10^{23}$ (points to N_A)

- Measure number of ' $0\nu\beta\beta$ ' decays, $N_{\beta\beta}$ in a given time t

$$N_t = N_{iso} - N_{\beta\beta} = N_0 e^{-(t/\tau)}$$

$$\rightarrow T_{1/2}^{\beta\beta}$$

N_t = number of isotopes after time t

N_0 = initial number of isotopes

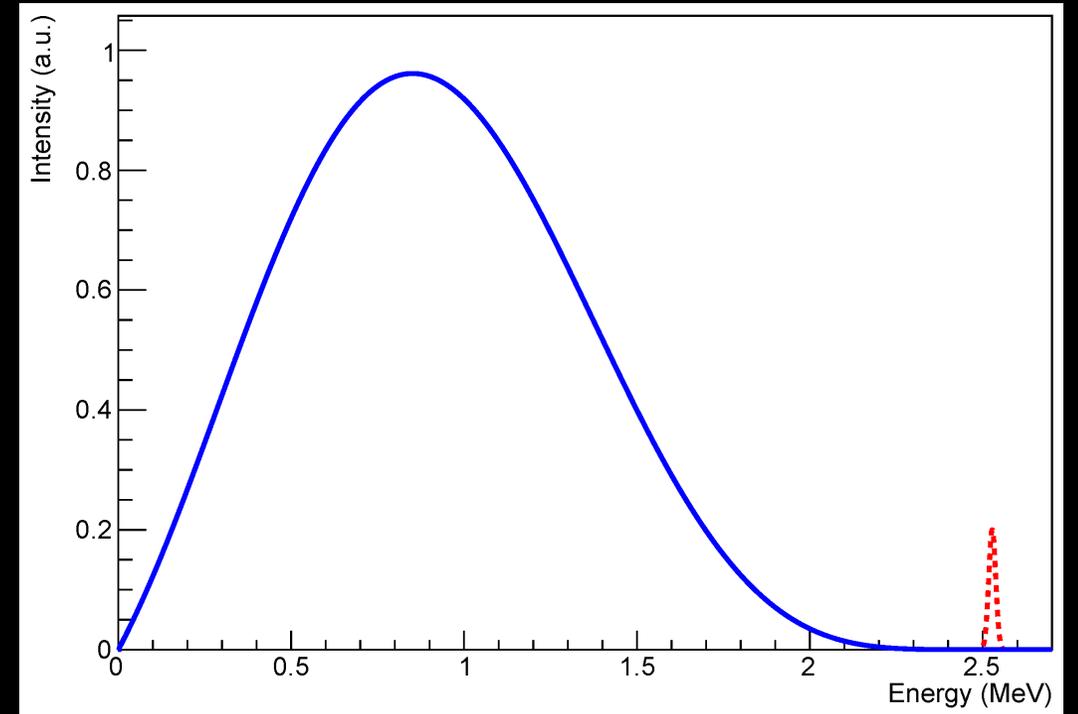
N_d = number of decays

t = measuring time

τ = time it takes to reduce to $1/e$

Experimental Considerations

- Signature of $0\nu\beta\beta$ is a peak at the endpoint of the $2e^-$ spectrum
 - Need to detect the electrons efficiently and measure their energy very accurately
 - Need to minimize the chance of any other events mimicking your signal



Sum energy of 2 betas

Background Free



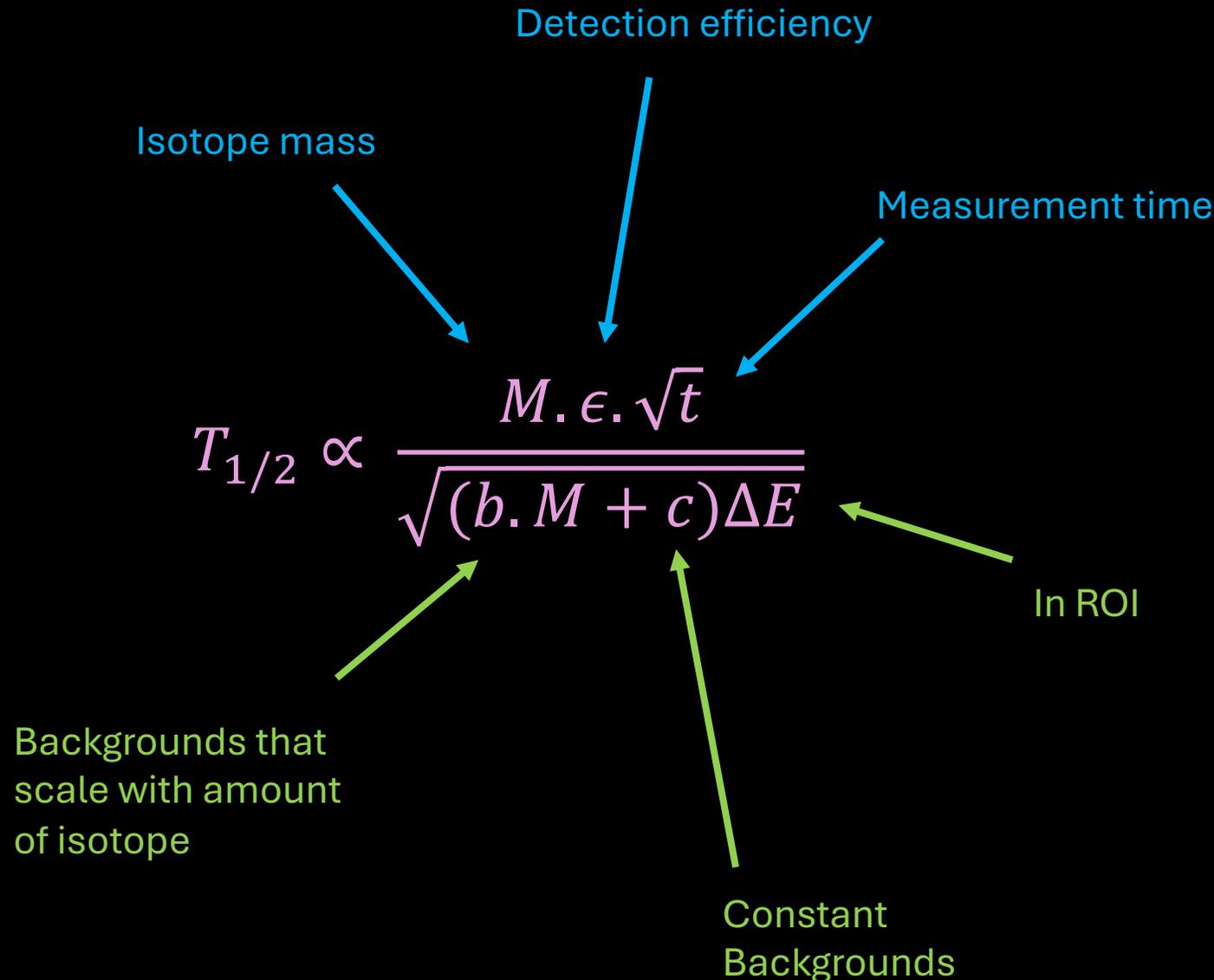
Isotope mass

Detection efficiency

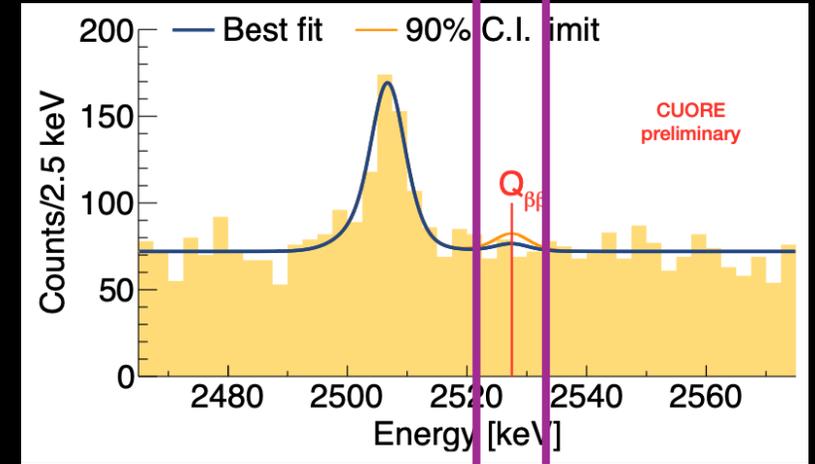
Measurement time

$$T_{1/2}^{0\nu} \propto M\epsilon t$$

Experimental Considerations



ROI =
Region Of
Interest



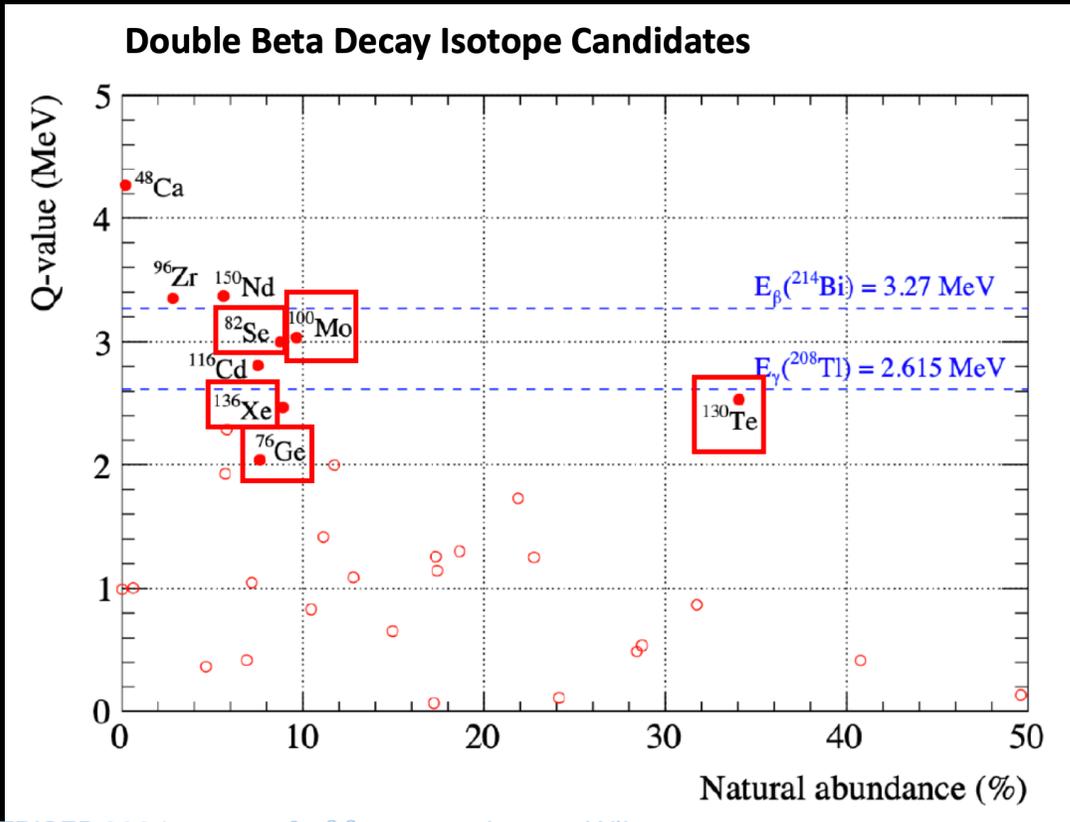
EXAMPLE:

Backgrounds = 70 counts / 2.5keV
 ROI = 10keV wide
 Background count = 280 counts
 Poisson uncertainty = $\sqrt{280} = 16.7$

Choose your Isotope

High Q value:

- Generally better phase space
- Above many low energy backgrounds



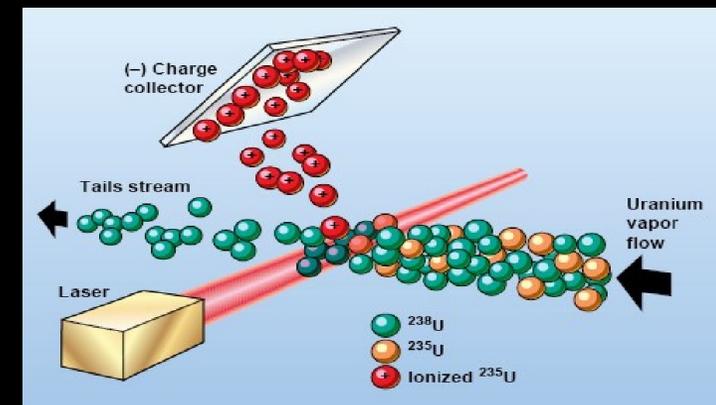
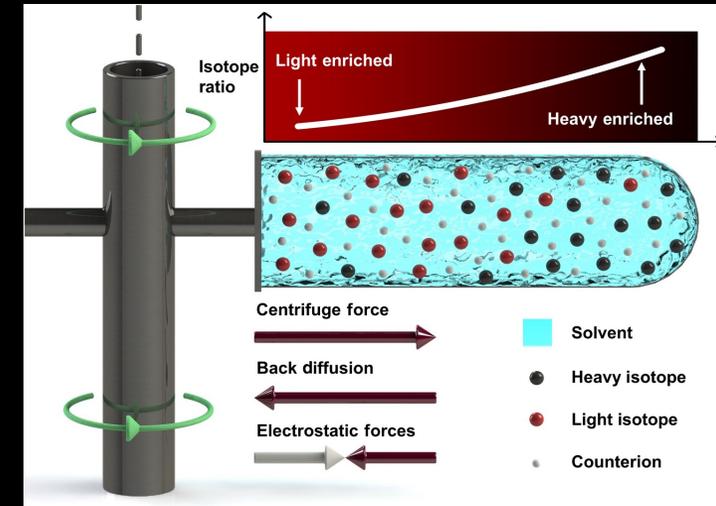
| $\beta\beta$ Decay Reaction | Isotopic Abundance [atomic %] | Q-value [keV] |
|---|----------------------------------|------------------|
| $^{48}\text{Ca} \rightarrow ^{48}\text{Ti}$ | 0.2 | 4274 |
| $^{76}\text{Ge} \rightarrow ^{76}\text{Se}$ | 7.6 | 2039 |
| $^{82}\text{Se} \rightarrow ^{82}\text{Kr}$ | 8.7 | 2996 |
| $^{96}\text{Zr} \rightarrow ^{96}\text{Mo}$ | 2.8 | 3348 |
| $^{100}\text{Mo} \rightarrow ^{100}\text{Ru}$ | 9.6 | 3034 |
| $^{116}\text{Cd} \rightarrow ^{116}\text{Sn}$ | 7.5 | 2814 |
| $^{124}\text{Sn} \rightarrow ^{124}\text{Te}$ | 5.8 | 2288 |
| $^{128}\text{Te} \rightarrow ^{128}\text{Xe}$ | 31.8 | 866 |
| $^{130}\text{Te} \rightarrow ^{130}\text{Xe}$ | 34.2 | 2528 |
| $^{136}\text{Xe} \rightarrow ^{136}\text{Ba}$ | 8.9 | 2458 |
| $^{150}\text{Nd} \rightarrow ^{150}\text{Sm}$ | 5.6 | 3368 |

High Isotopic Abundance:

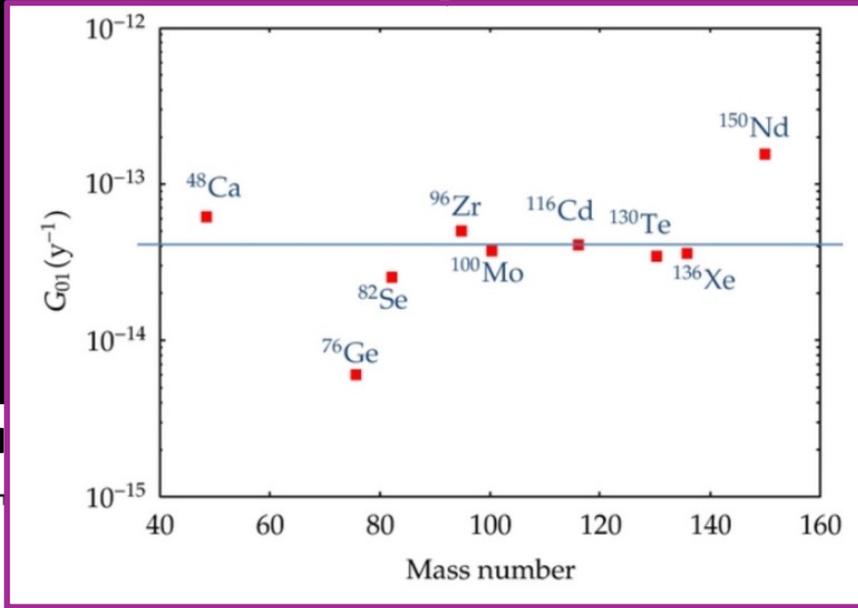
- More isotope per \$\$\$
- Isotopic enrichment is challenging
(money time and politics!)

Isotope Enrichment

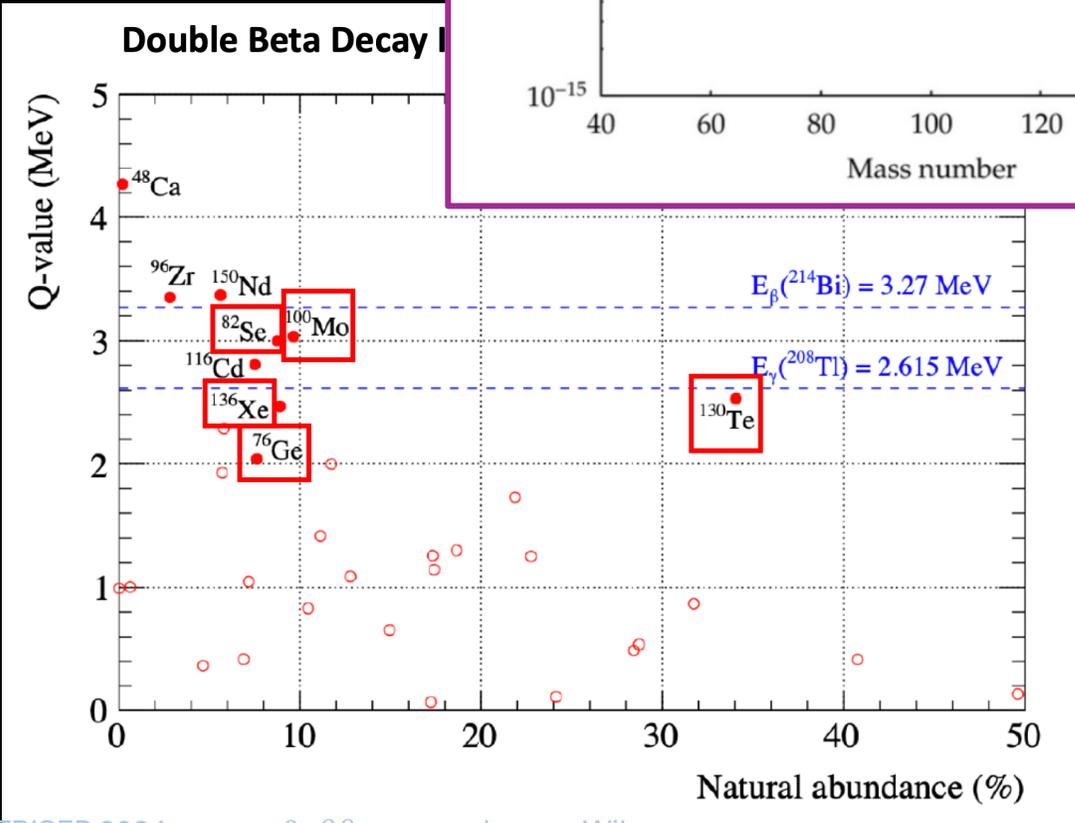
- If abundance is low, enrich in your desired isotope.
- Method depends on element.
 - Can you make it gaseous? Soluble in liquid?
- Centrifugal force:
 - gas centrifuge – Xenon, GeF_4 or GeH_4 , SeF_6 , MoF_6
 - Liquid solution centrifuge
- Atomic vapor laser isotope separation (AVLIS):
 - Inject laser energy at the precise frequency to ionize only the specific isotope
 - Separate ions from atoms with EM field



Choose your Isotope



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Correlation between Q-value and Phase Space Factor (not exact – other factors at play)

Choose your Isotope

Source = Detector

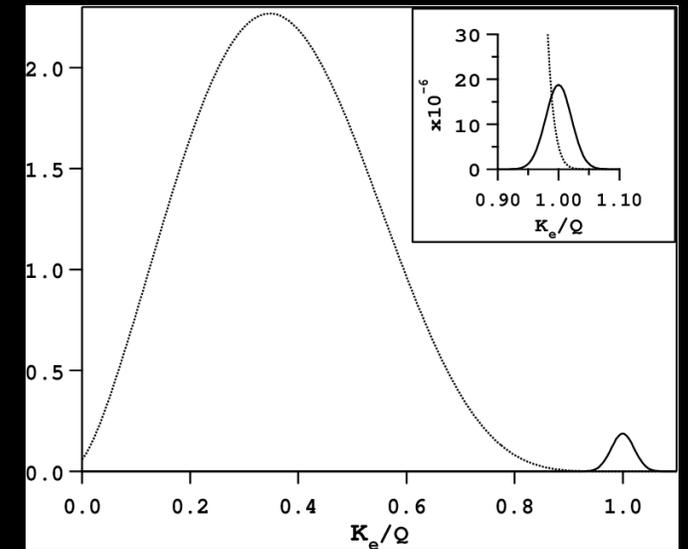
- $\sim MeV$ β s don't travel far so restricted to thin films if detectors separate from source
- Need to 'see' the $\beta\beta$ and accurately record their energy
 - Detection Efficiency
 - Energy Resolution
- Even better
 - Can you be sure it was a $\beta\beta$ event? → Tracking would be nice
 - Can you be sure it was a decay of your isotope? → Tagging of the decay product would be very nice

Backgrounds

- $2\nu\beta\beta$ decays $\Delta E, b$
- Internal radiological backgrounds b
- Surface backgrounds $\sim b$
- External radiological backgrounds c

- Cosmogenic b, c
- Neutrinos and Neutrino-genic b, c

$$T_{1/2} \propto \frac{M \cdot \epsilon \cdot \sqrt{t}}{\sqrt{(b \cdot M + c) \Delta E}}$$

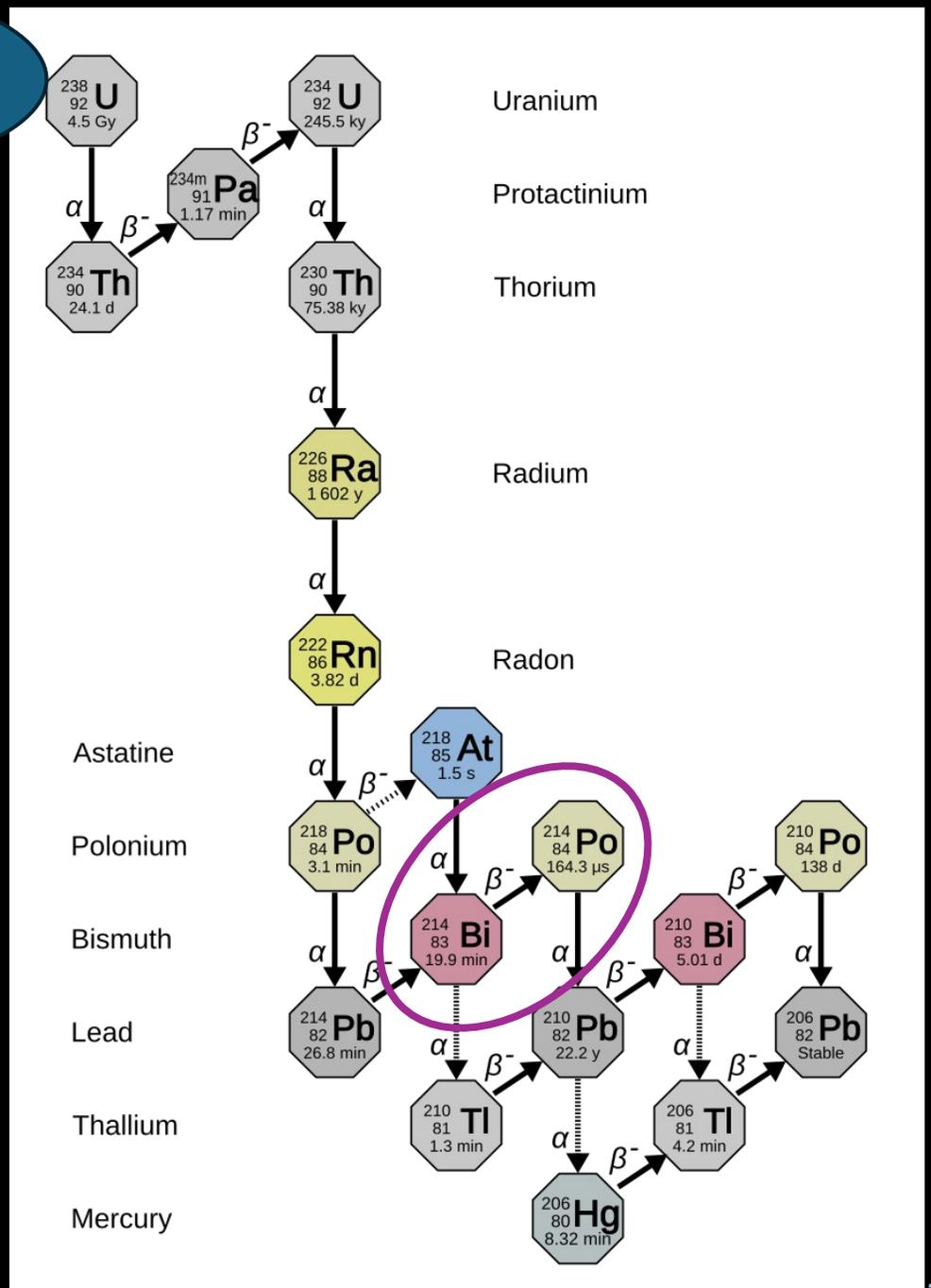


^{238}U chain

Remember ^{238}U is a $\beta\beta$ decay candidate

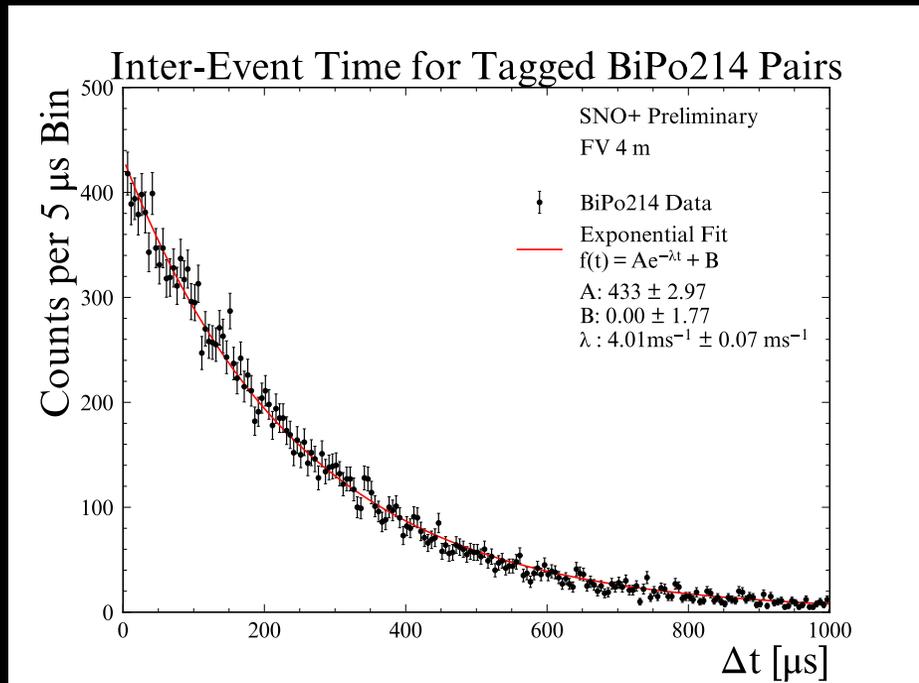
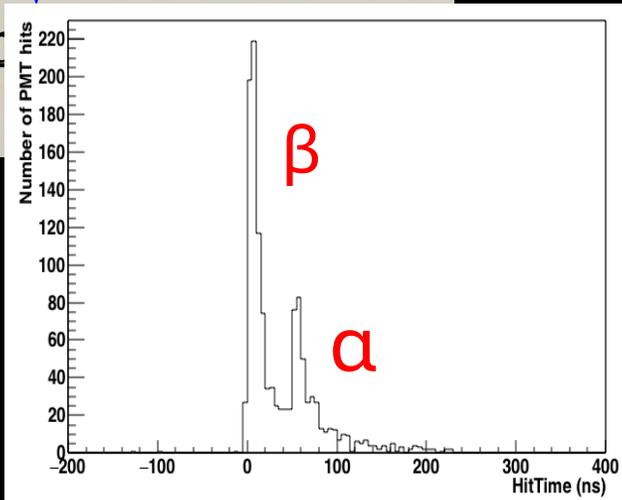
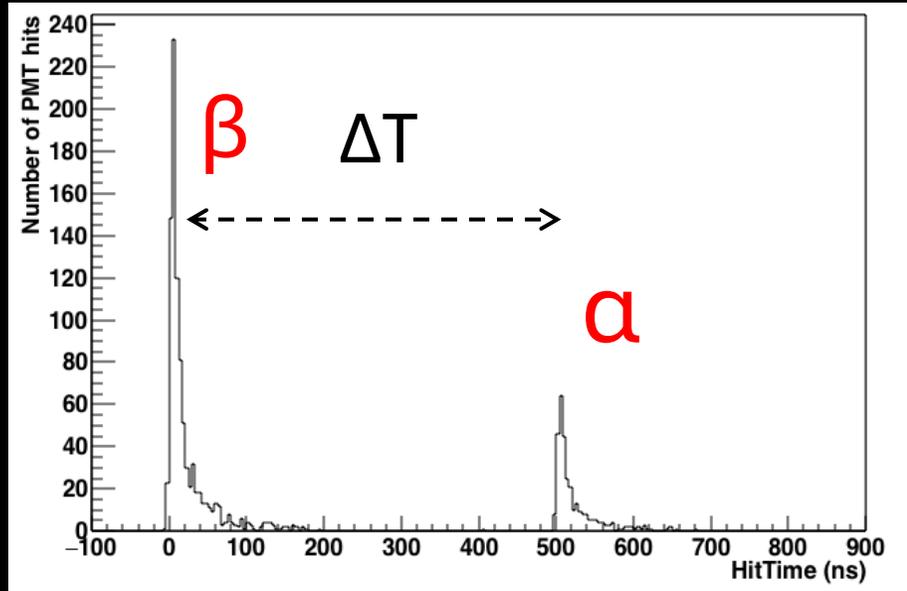
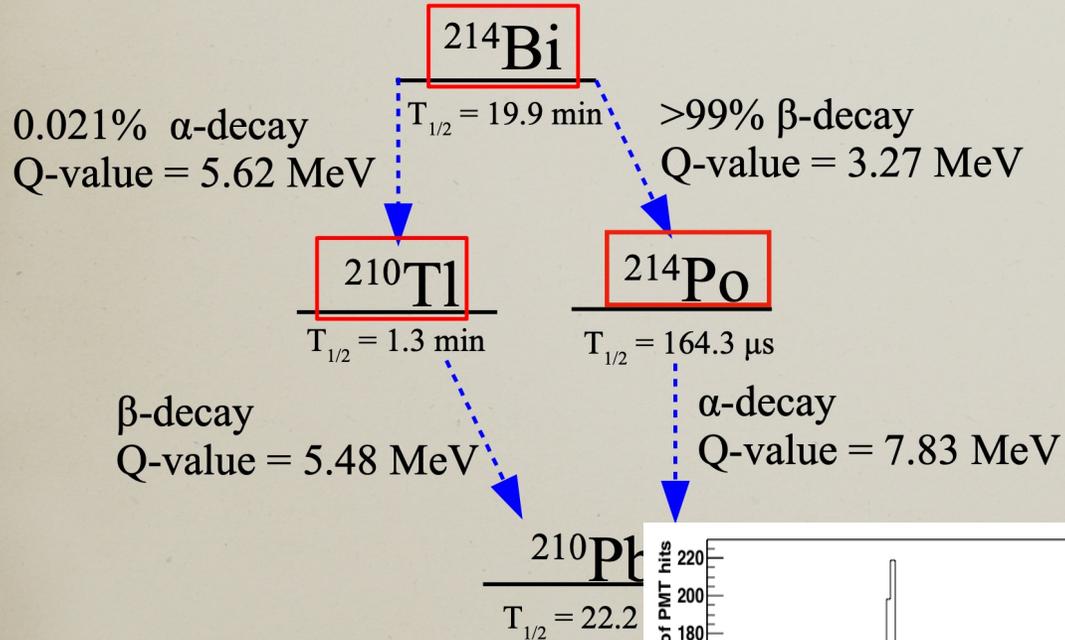
Naturally occurring (few ppm in rock, soil, water), long lived $T_{1/2} = 4.5 \times 10^6$ years

- α -decays
- β -decays
- Accompanying γ s
- Very short decay steps can be used for 'tagging': ^{214}Po $T_{1/2} = 164 \mu\text{s}$



BiPos

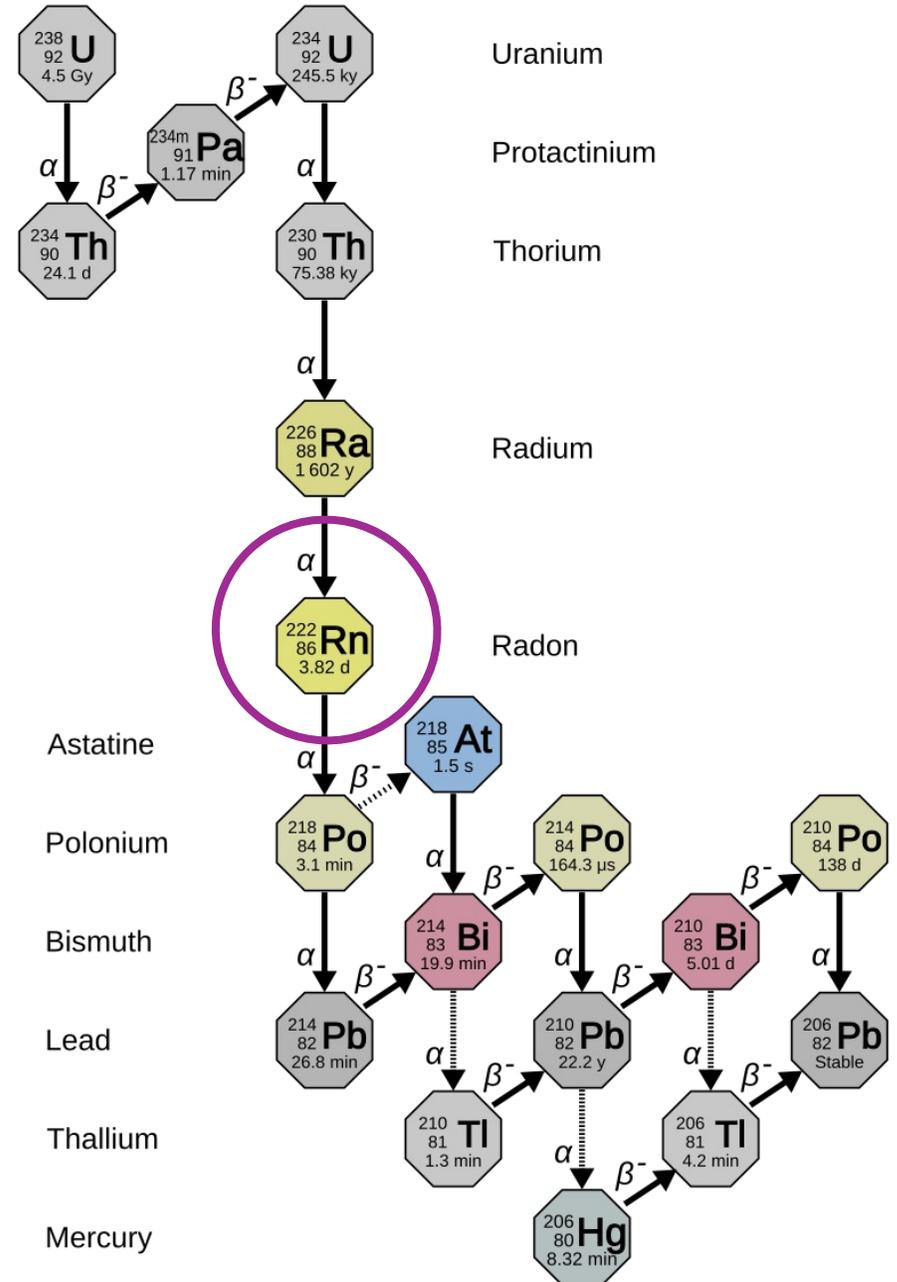
^{238}U via $^{214}\text{BiPo}$



^{238}U chain

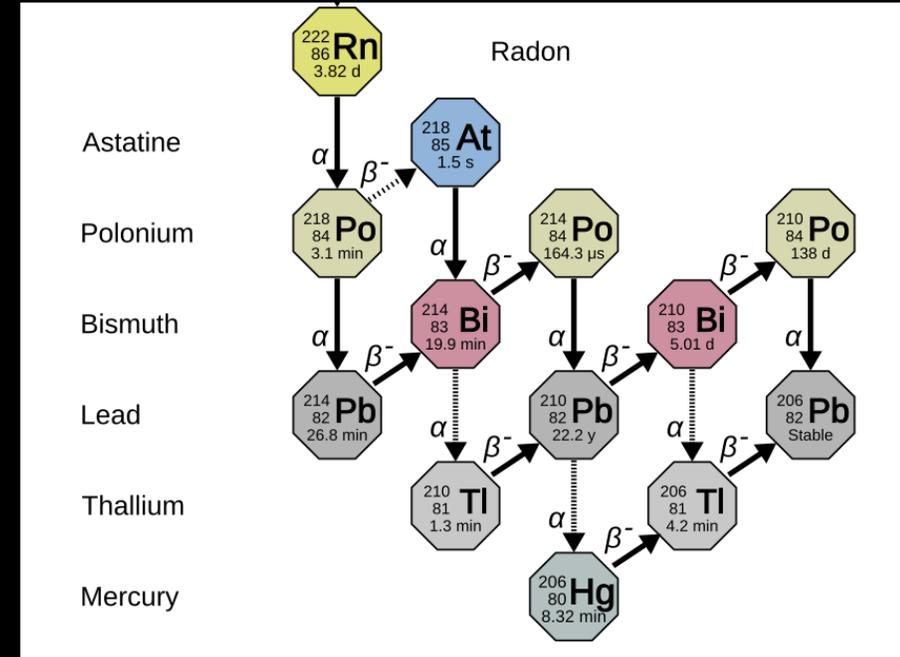
Naturally occurring (few ppm in rock, soil, water), long lived $T_{1/2} = 4.5 \times 10^6$ years

- α -decays
- β -decays
- Accompanying γ s
- Very short decay steps can be used for ‘tagging’
- Radon gaseous and short lived
 ^{222}Rn $T_{1/2} = 3.82$ days



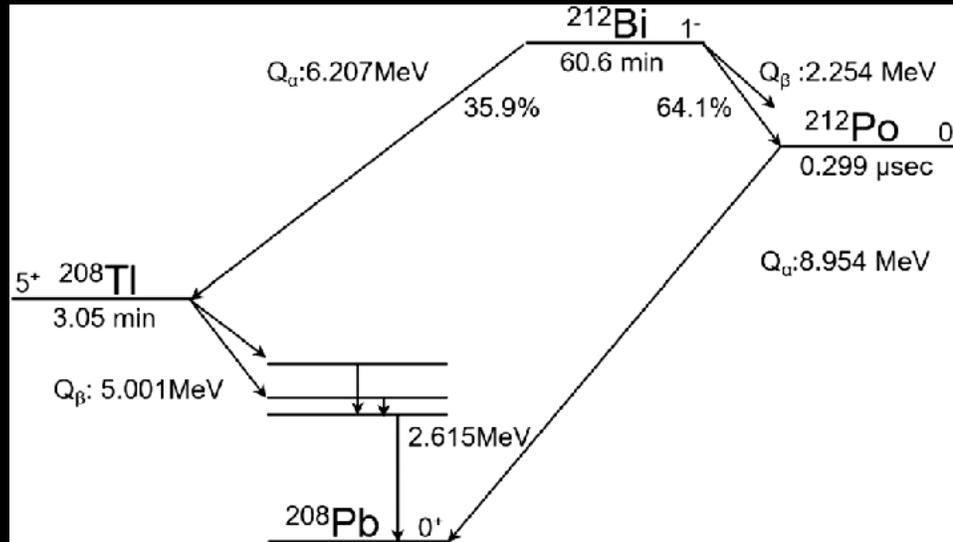
Radon

- ^{222}Rn $T_{1/2} = 3.82$ days
- Produced in the ^{238}U decay chain, can then **emanate** out of solid detector components into a liquid or gaseous region
- Or radon in air can **dissolve** into a liquid
- Both can break ‘equilibrium’
 - Different activity in the top and bottom part of the chain
- Radon decays in air, can **implant** daughters into solid materials
 - Those radioactive daughters can later **leach** out into liquids

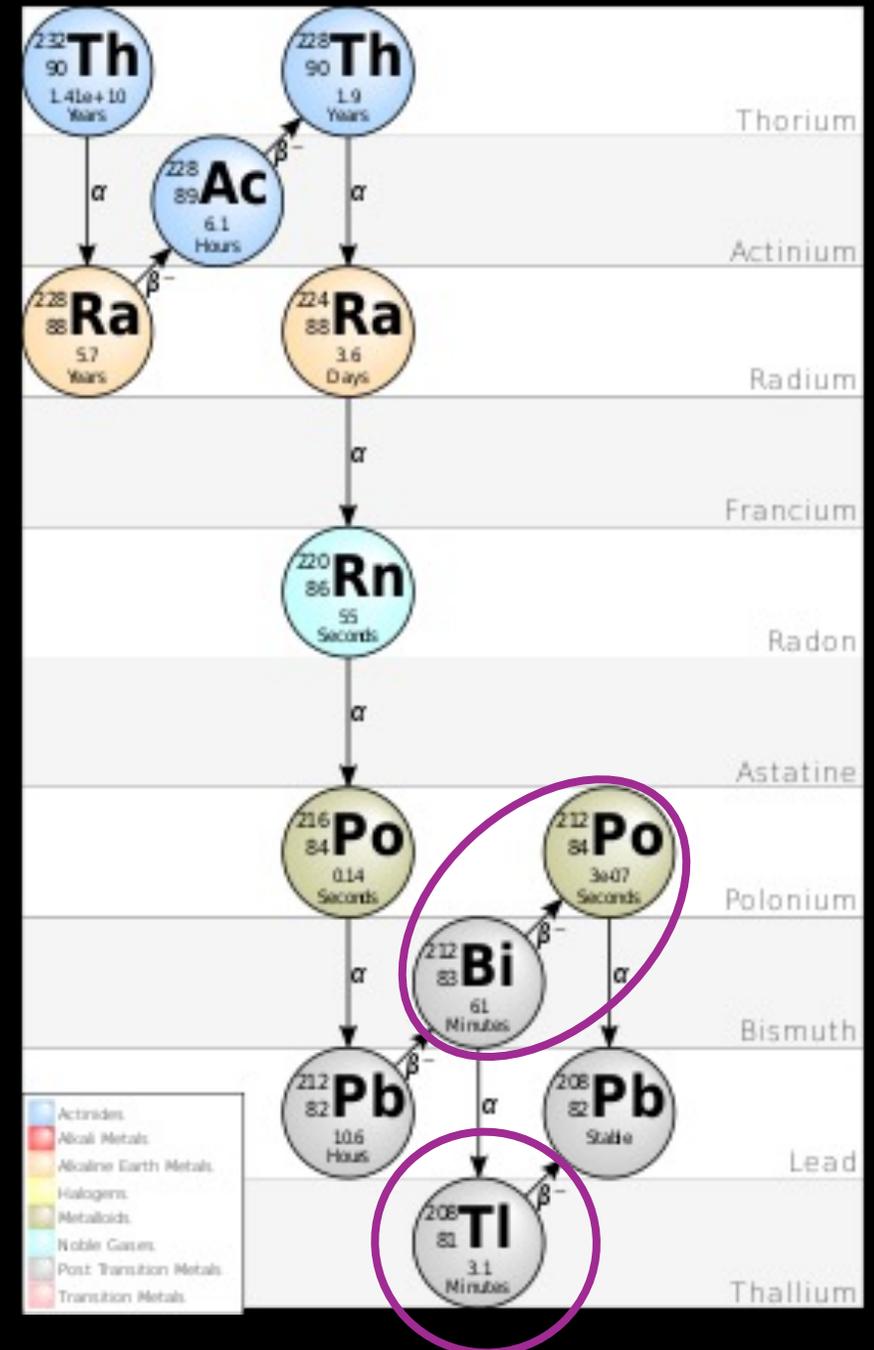


^{232}Th chain

- Also naturally occurring
- Highest ‘naturally occurring’ gamma
 - ^{208}Tl $E = 2.615\text{MeV}$



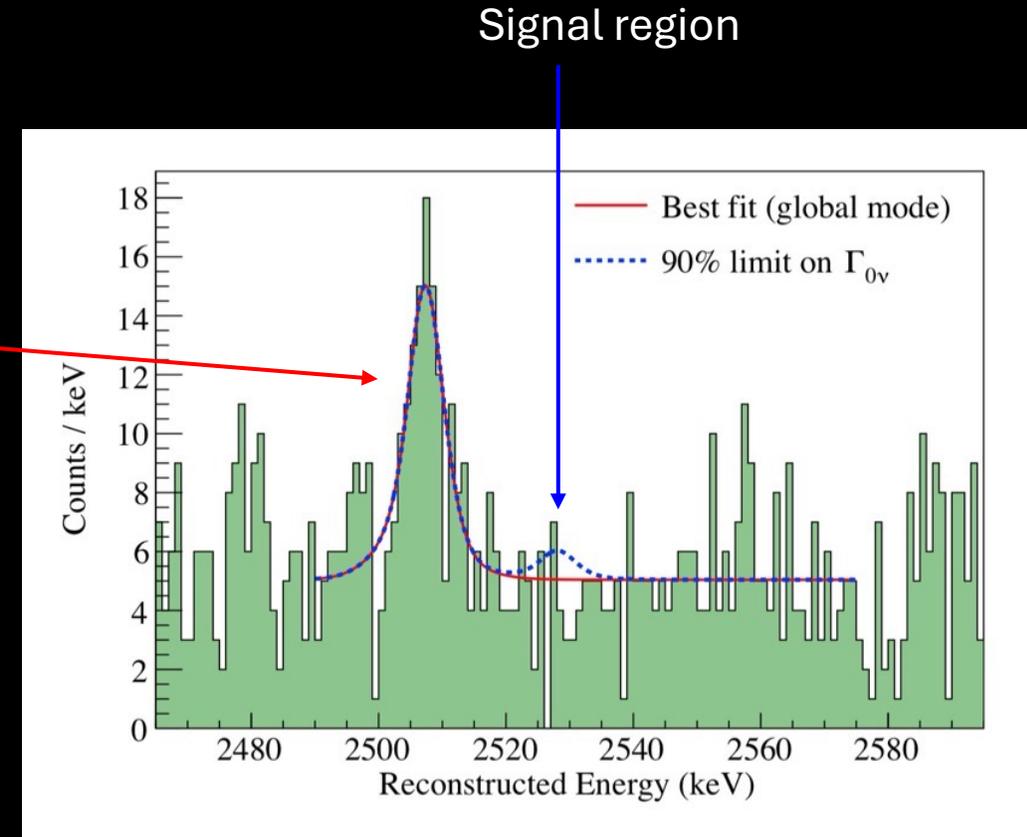
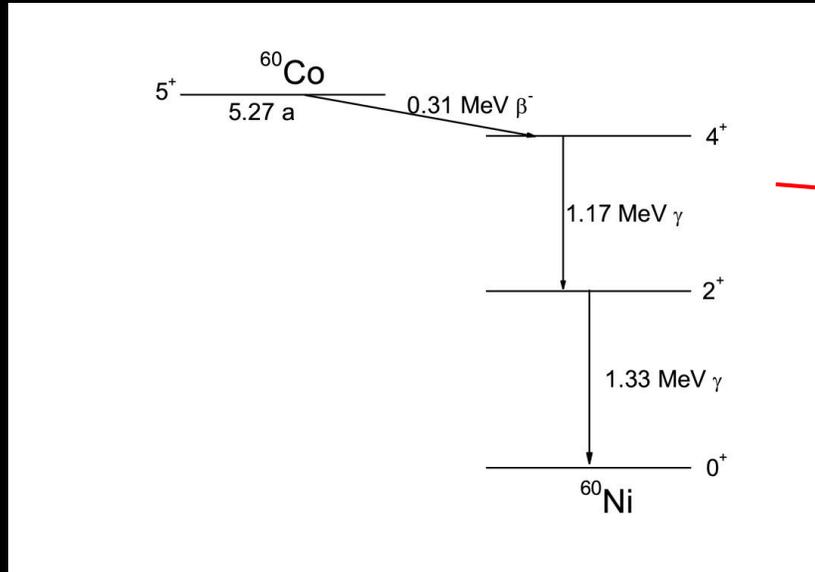
- ^{212}Po $T_{1/2} = 0.3\mu\text{s}$
- Can also be BiPo ‘tagged’ but more challenging as shorter half-life than $^{214}\text{BiPo}$ s



Radioactive Isotopes

- Most 'dangerous' depends on detector and Q-value

e.g. $^{60}\text{Co} \rightarrow 2.5\text{MeV}$ visible gammas



CUORE spectrum

^{130}Te Q-value = 2.528 MeV

Backgrounds

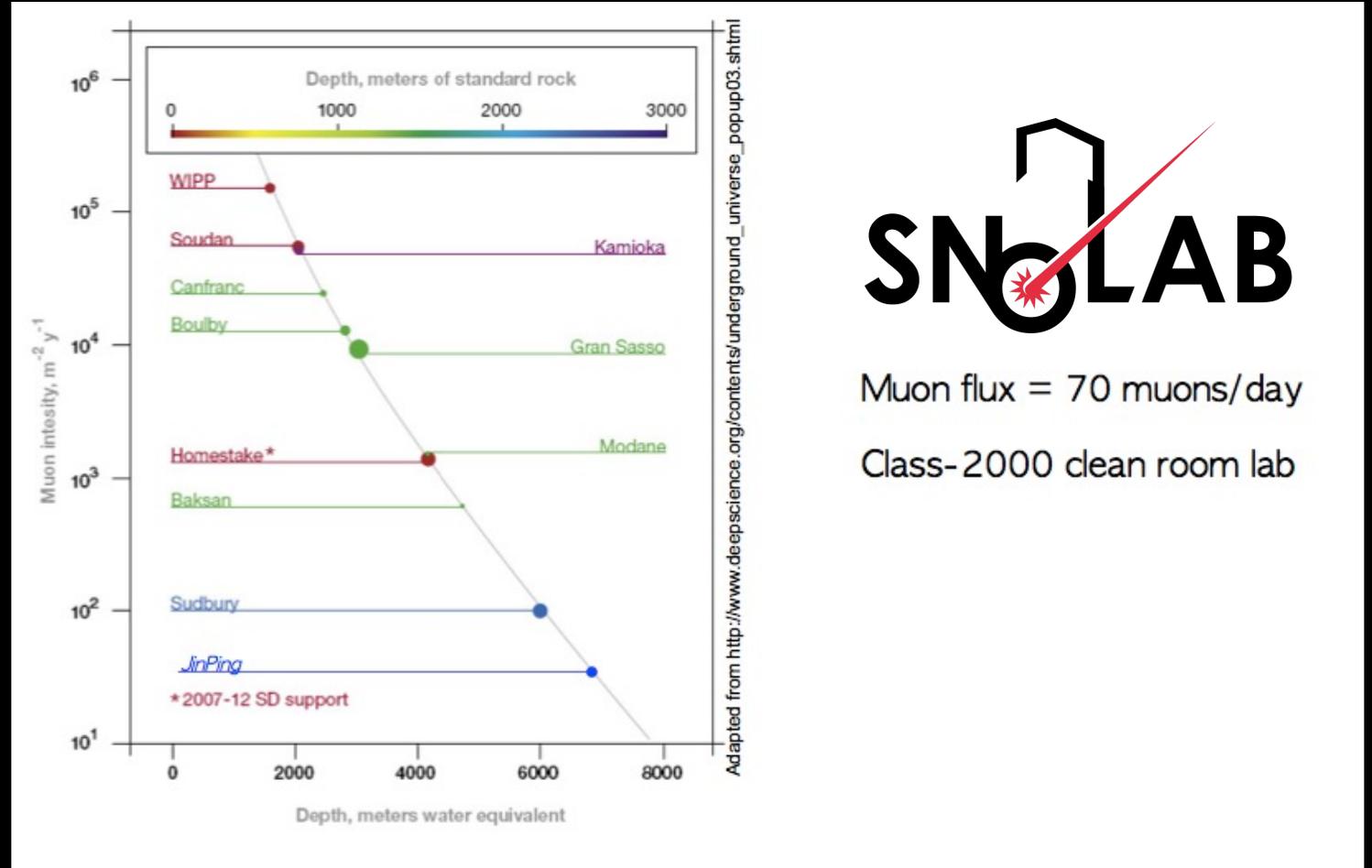
- $2\nu\beta\beta$ decays ΔE
- Internal radiological backgrounds b
- External radiological backgrounds c

- Cosmogenic b, c
- Neutrinos and Neutrino-genic b, c

$$T_{1/2} \propto \frac{M \cdot \epsilon \cdot \sqrt{t}}{\sqrt{(b \cdot M + c) \Delta E}}$$

Cosmic Muons

- Muons produced in the atmosphere from cosmic ray interactions
- Deeper underground, lower muon flux
- Muons are generally easily vetoed
 - Characteristic high energy deposits
 - Veto detectors
- However...

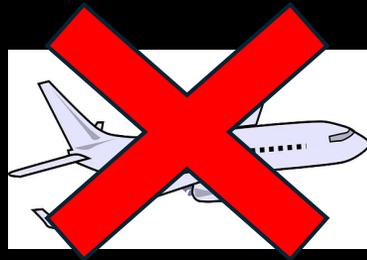


Muon flux = 70 muons/day

Class-2000 clean room lab

Cosmogenic Backgrounds

- Muons can interact with material in the detector producing n,p, radioactive isotopes
- Materials above ground experience higher activation rates
 - Source material
 - During construction
 - In transit



Isotopes produced with short (<1year) half-lives can be mitigated by allowing materials to ‘cool’ underground

- In-situ cosmogenic production
 - Can veto short-lived isotopes with time-cut after muon

Experiment Examples

- Not a complete list
- Use these examples to illustrate the different backgrounds and challenges

Liquid scintillator

^{136}Xe , ^{130}Te

KamLAND-Zen

SNO+

TPC

^{136}Xe

nEXO, NEXT

Cryogenic
Bolometer

^{130}Te , ^{82}Se

^{130}Te , ^{82}Se

CUORE, CUPID

Semi-conductors

^{76}Ge

LEGEND

Tracking
calorimeters

^{82}Se

SuperNEMO

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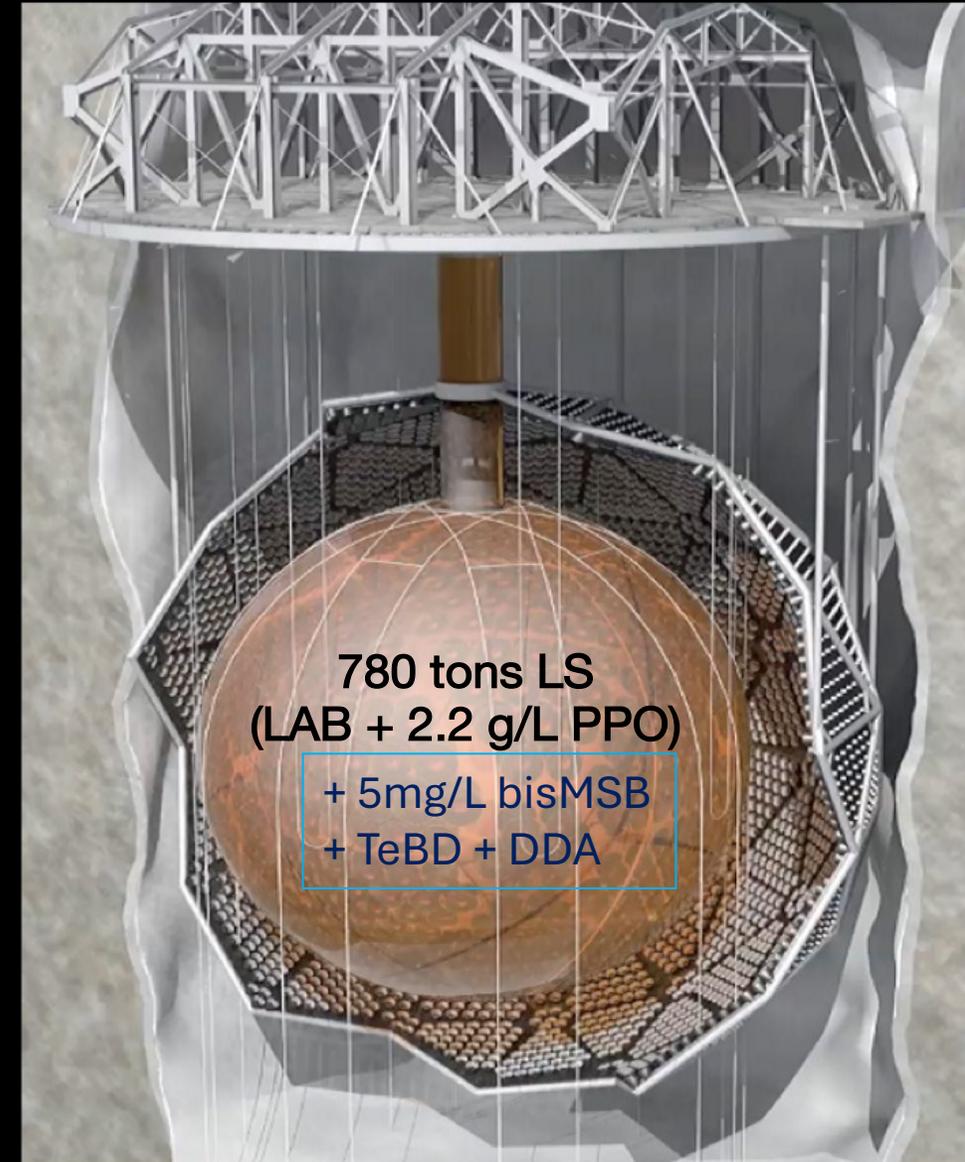
Tracking
calorimeters

^{82}Se

SuperNEMO

SNO+

- 2km underground (~6000 mwe)
- Observe events through scintillation light with ~9300 PMTs
 - $e^\pm, \gamma, \alpha, \mu$
- ^{130}Te – 34% nat abundance
- Highly scalable, cost effective (no enrichment required)
- Load natural Te into the scintillator (chemistry!)
 - ‘Source out’ measurements first
 - Initially add 0.5% by mass (3.9tonnes)
 - → 1%, 1.5%, 2.5% ...

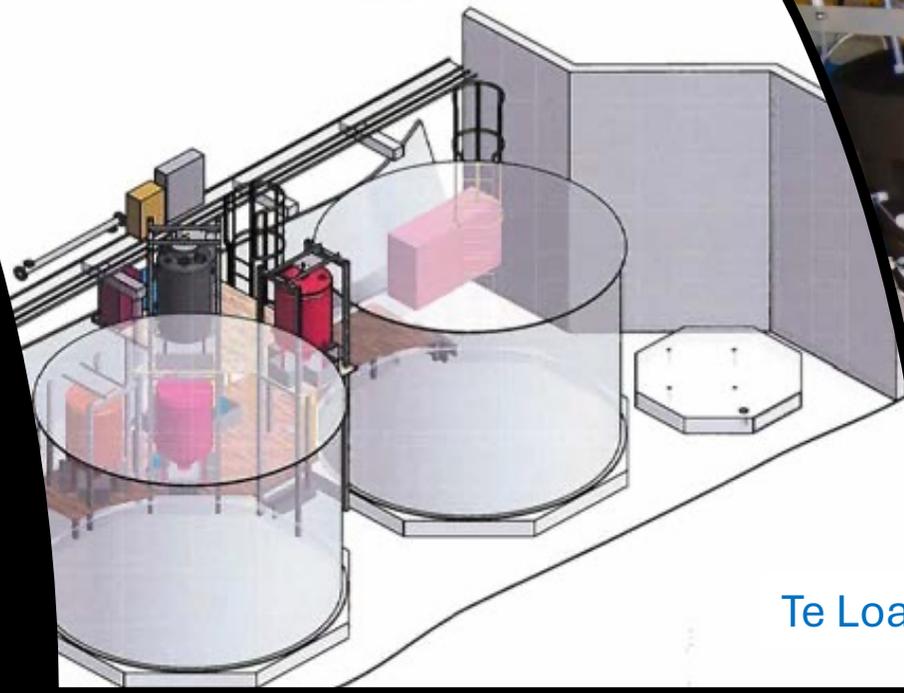


Te loading

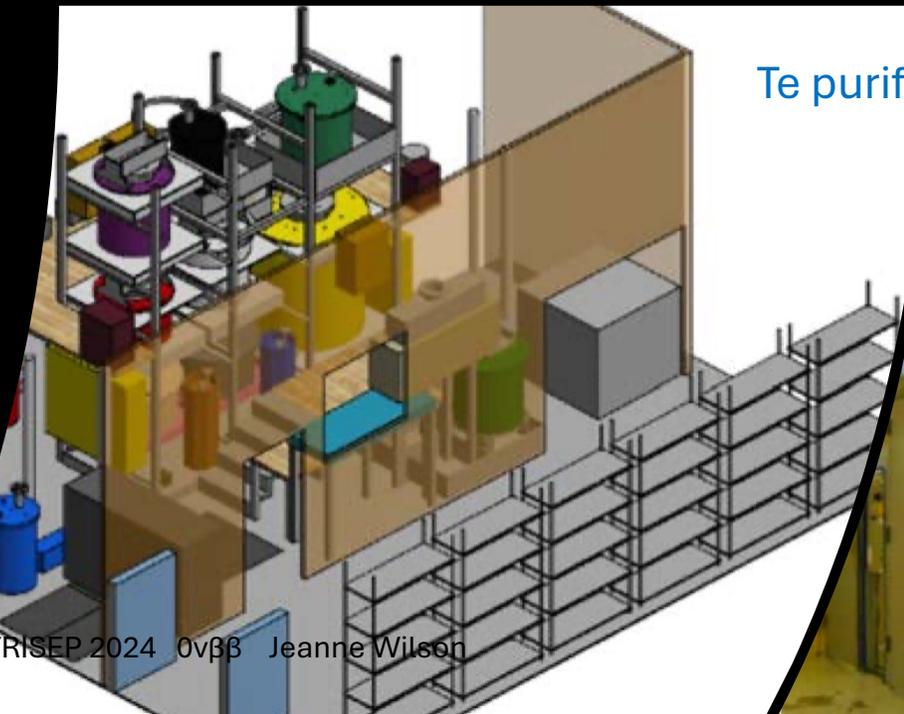
- ~8 tons of telluric acid (TeA) “cooling” underground
- Target purification for Te cocktail:

~ 10^{-15} g/g U

~ 10^{-16} g/g Th



Te Loading plant

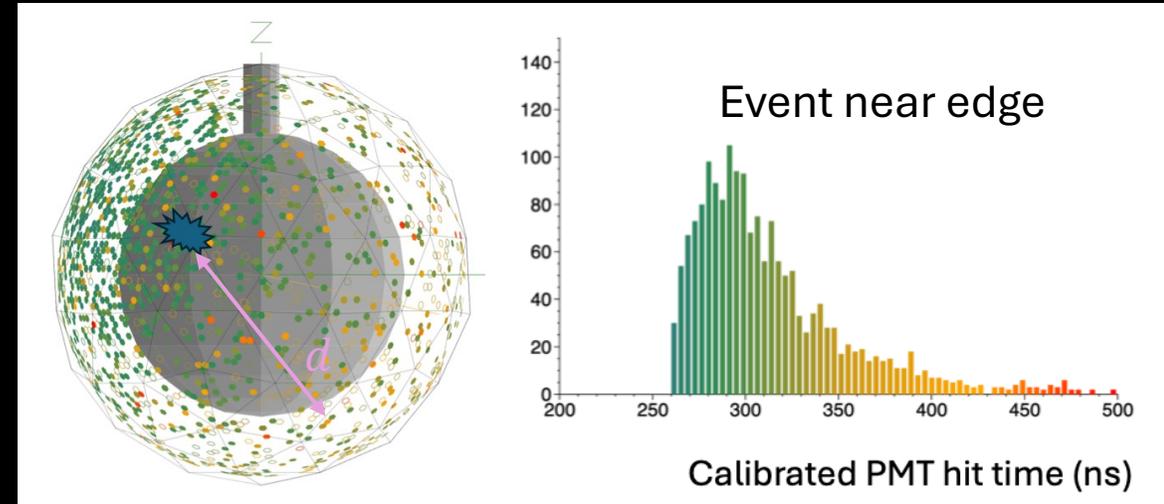
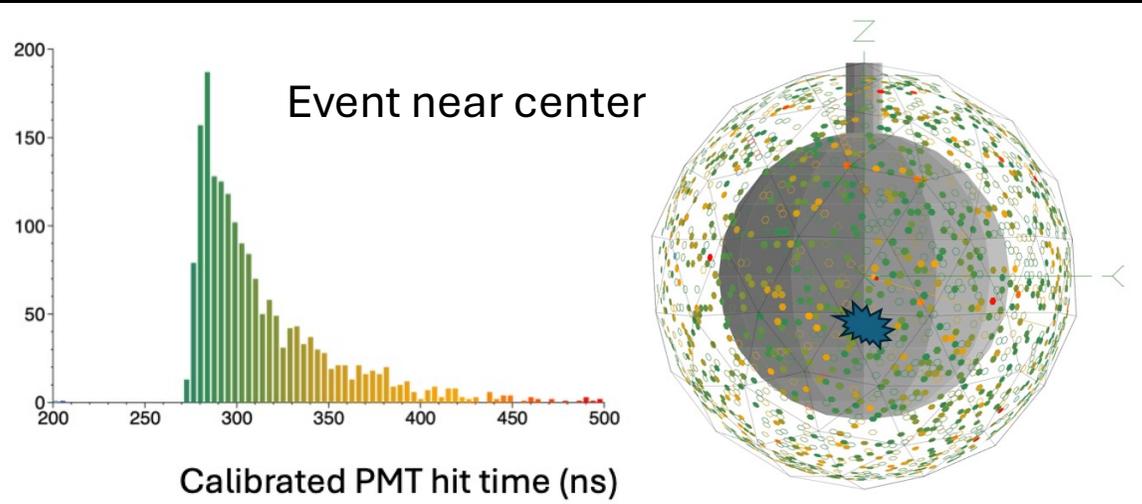


Te purification plant



Event Reconstruction

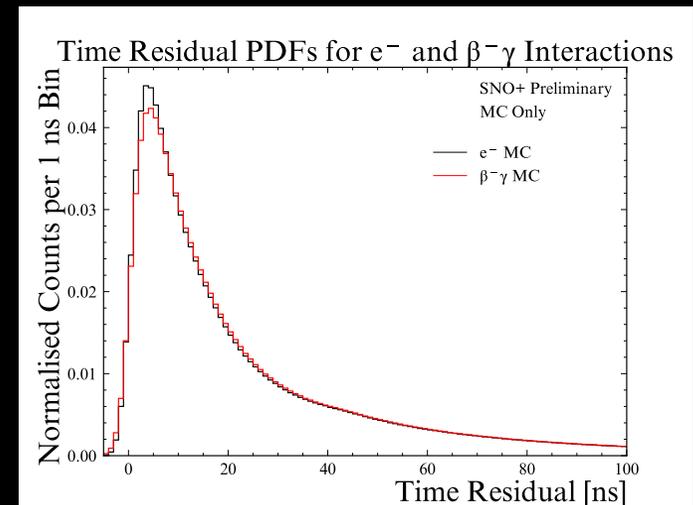
- ‘Events’ → scintillation light → photons → PMT hits
- $> 10,0000 \gamma/\text{MeV} \rightarrow \sim 300 \text{ hits}/\text{MeV}$



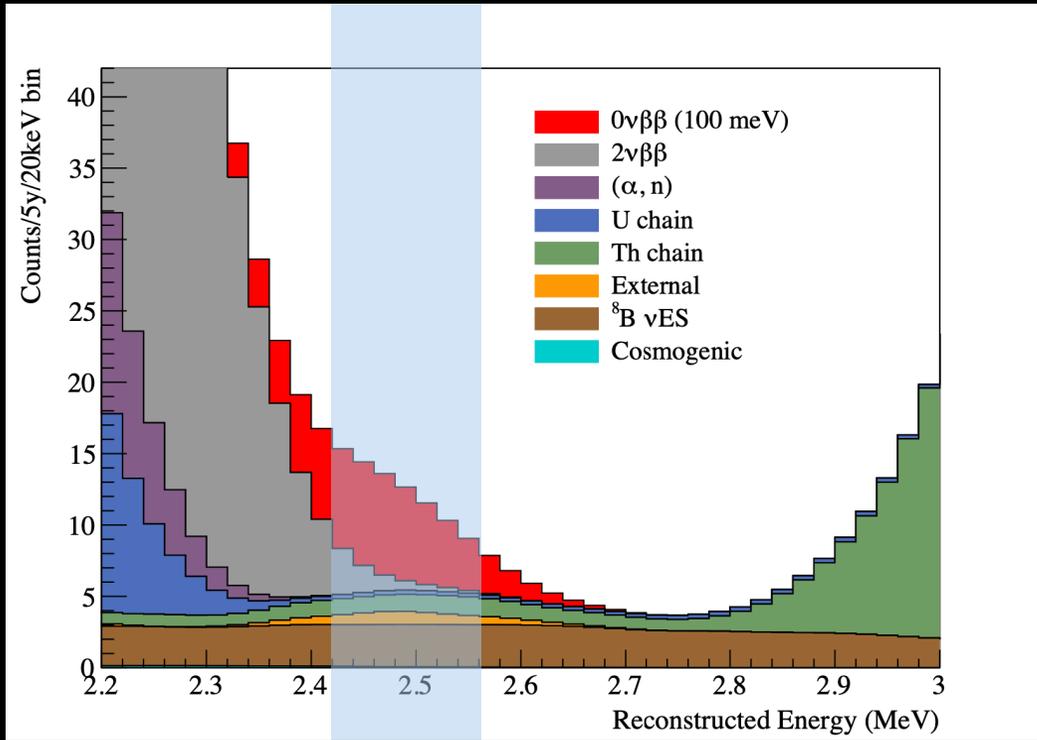
- Reconstruct position and energy of event from time and number of PMT hits

$$t_{res} = t_{hit} - t_{event} - d/c$$

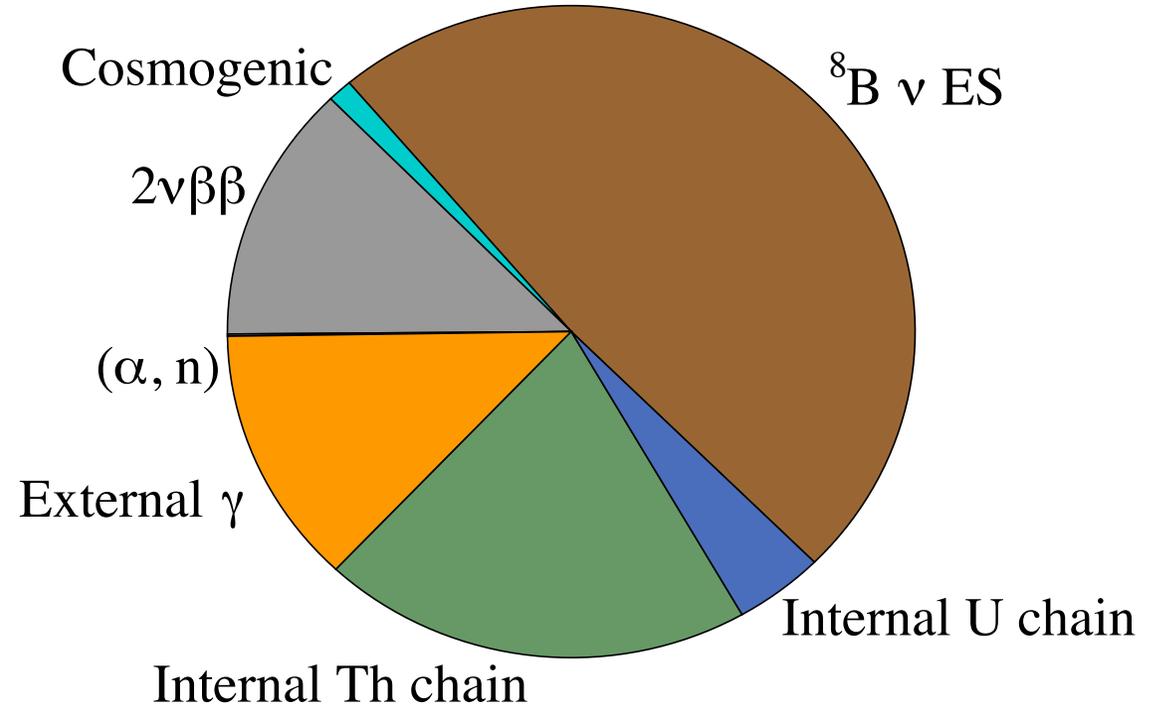
- Some sensitivity to event type through timing distribution



SNO+ 0.5% loading

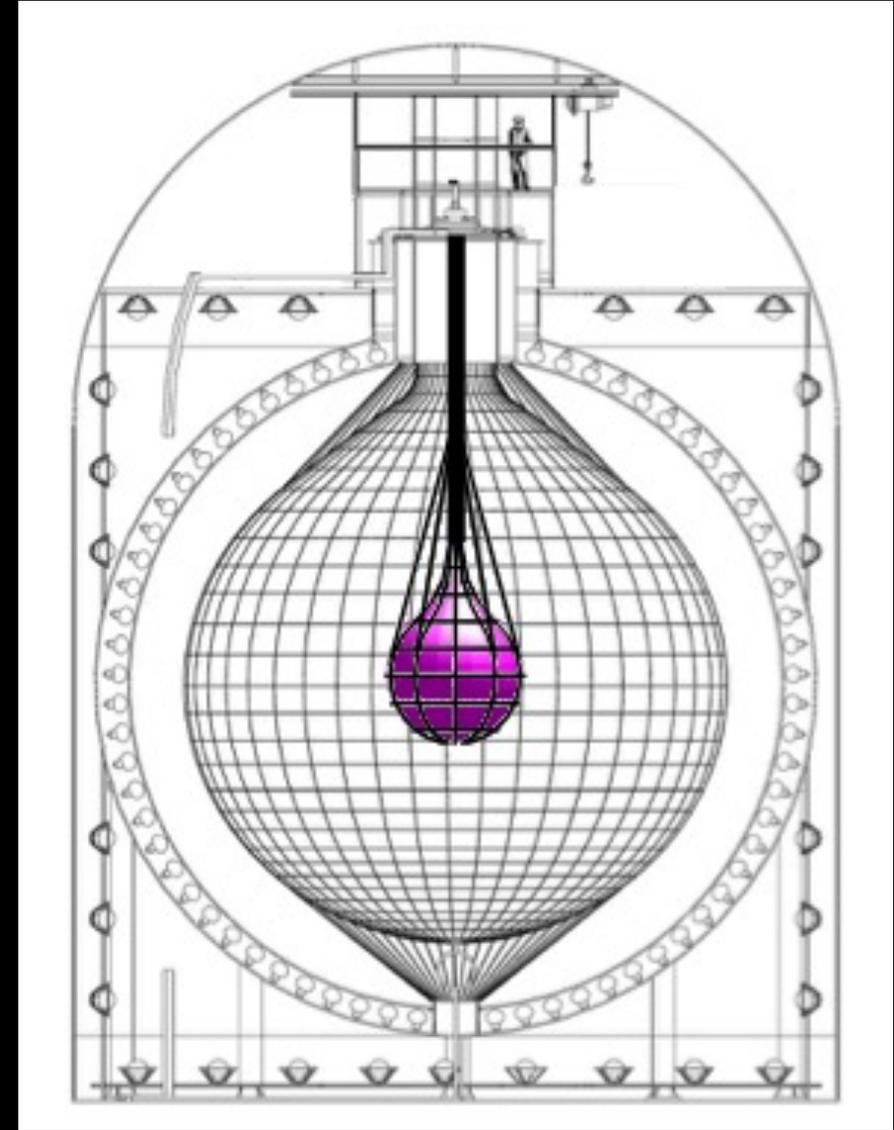


ROI: 2.42 - 2.56 MeV [-0.5 σ - 1.5 σ]
Counts/Year: 9.47



KamLAND-Zen

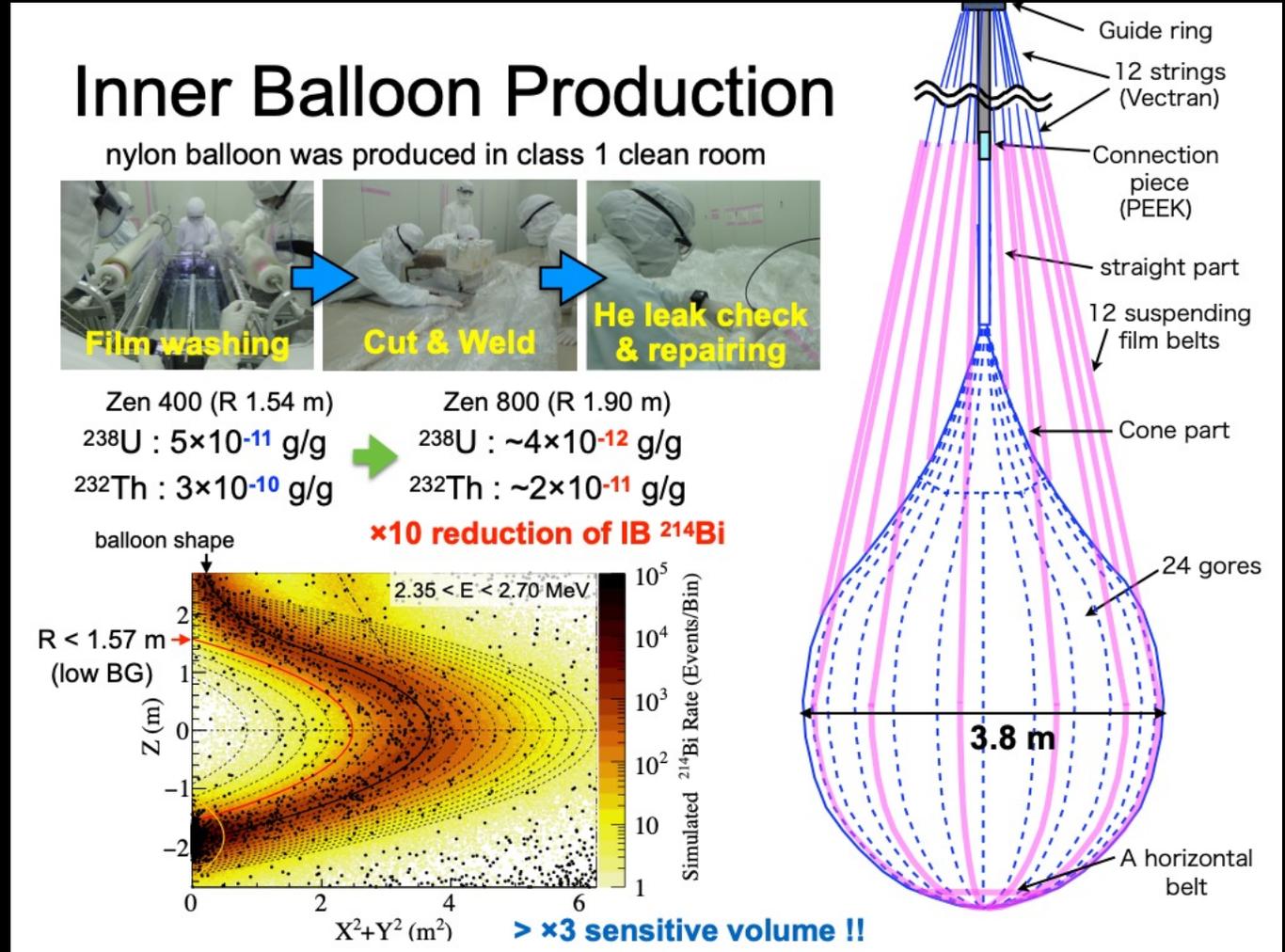
- 1000-ton pure liquid scintillator
 $U, Th < 10^{-17} g/g$
- ~745kg of ^{136}Xe (91% enrichment)
loaded into inner balloon
- ~8000 photons/MeV from Liquid
scintillator



KamLAND-Zen backgrounds 1

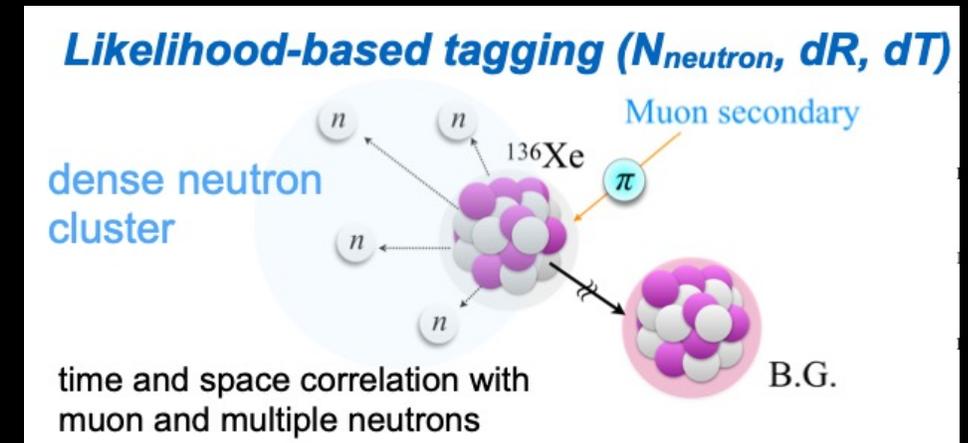
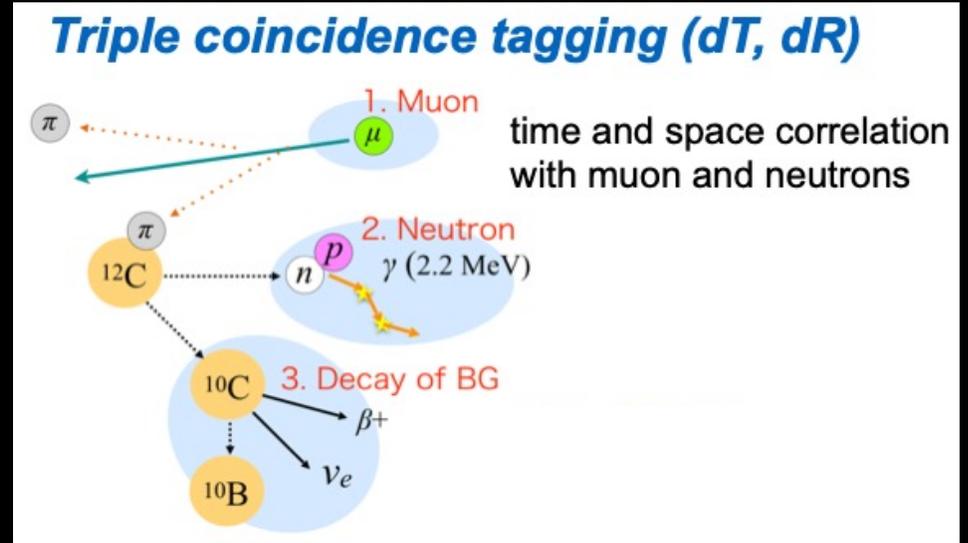
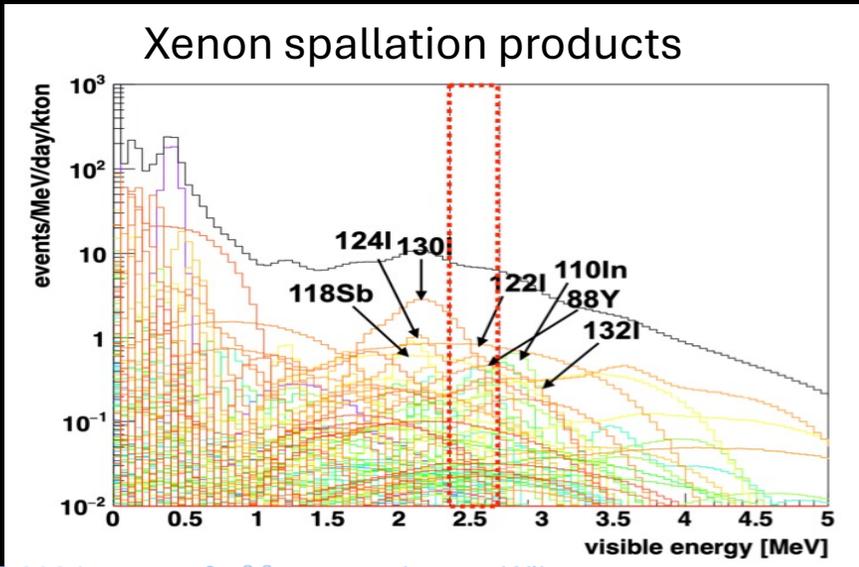
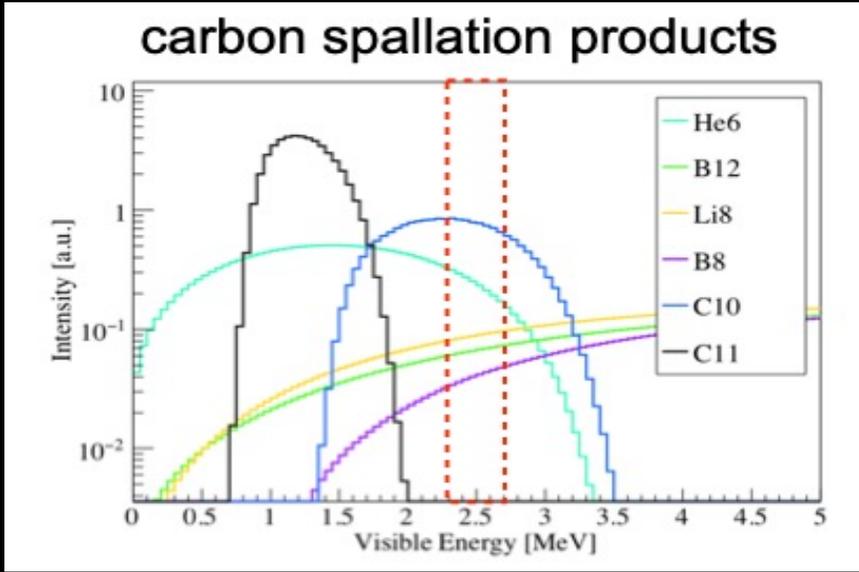
Slide from I Shimizu, Neutrino 2024

Mitigating backgrounds from the balloon



KamLAND-Zen backgrounds 2

2700 m.w.e.
over-burden

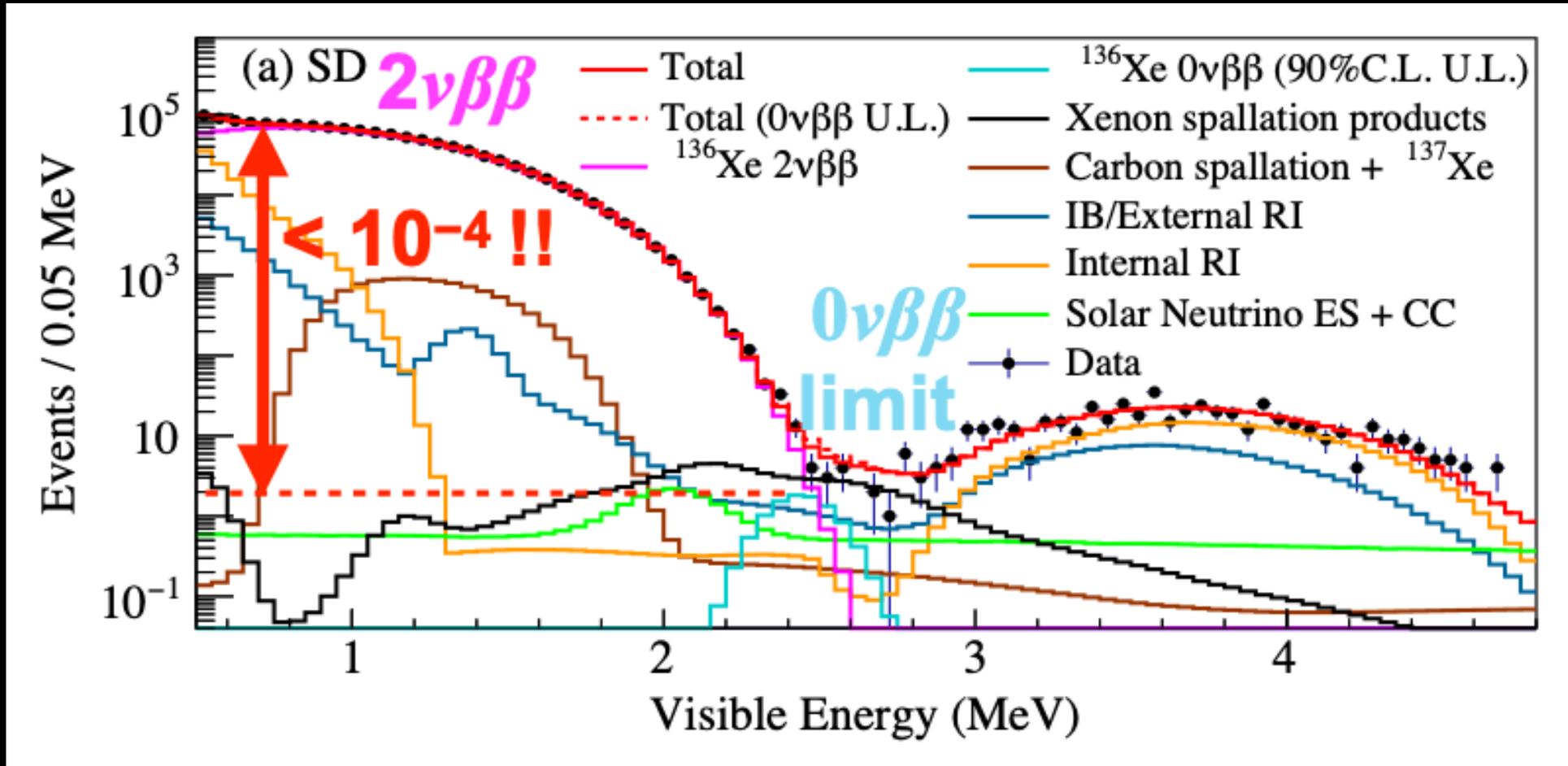


KamLand-Zen latest results

1131 days of data

Best fit = 0 events , 90% CL < 10 events

$$T_{1/2}^{0\nu} > 3.8 \times 10^{26} \text{ years}$$



Experiment Examples

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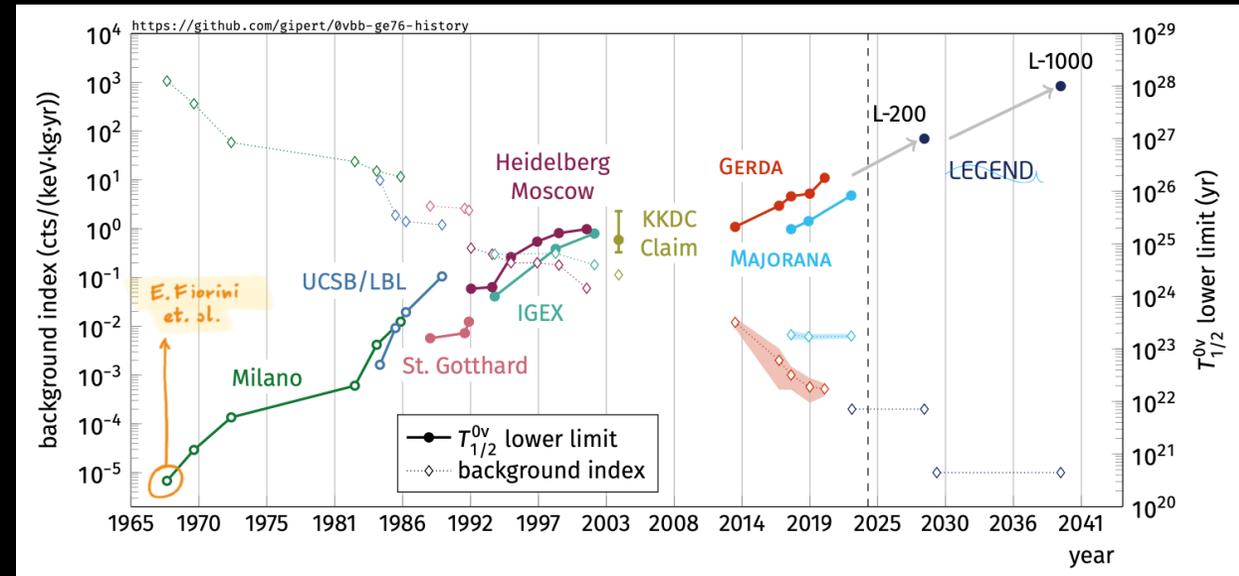
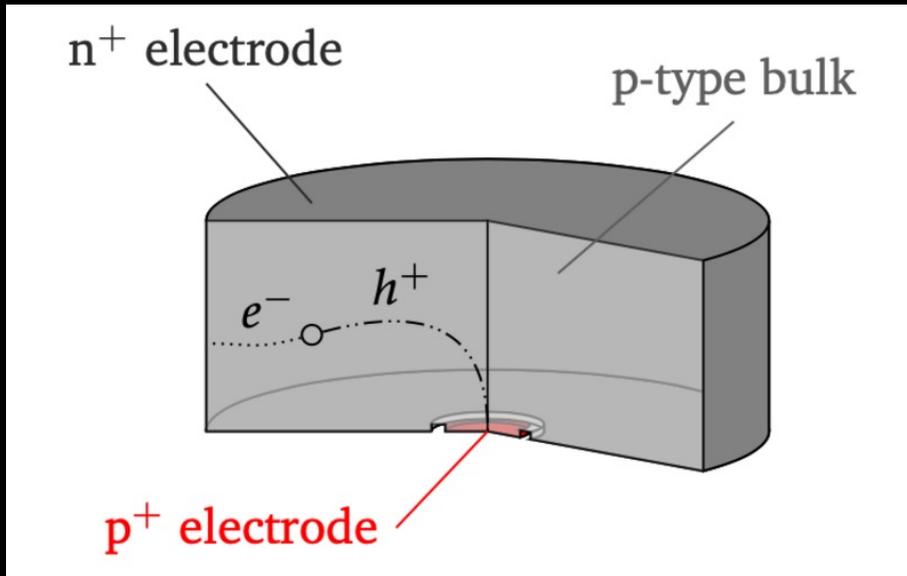
Tracking
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^{82}Se

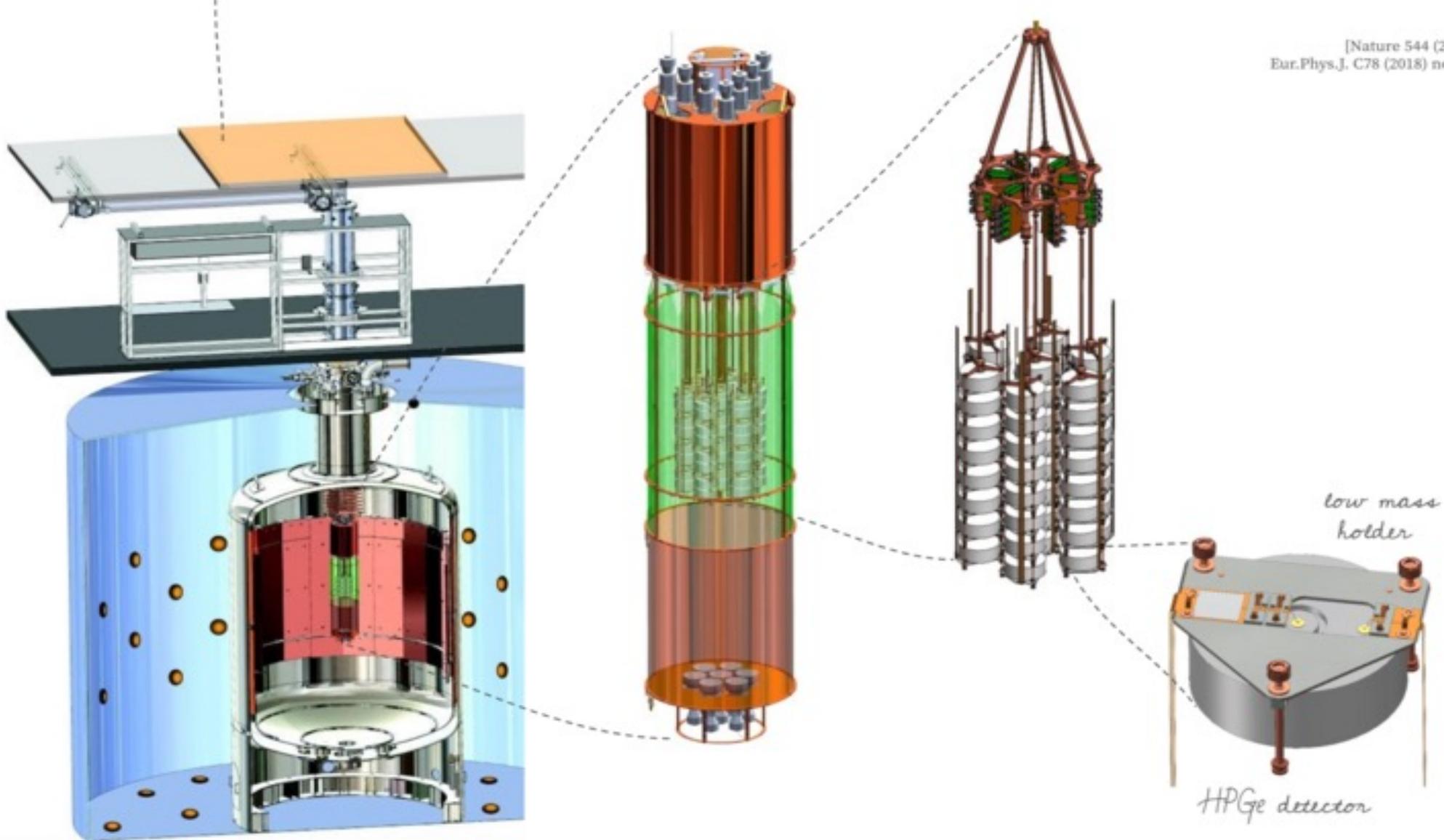
SuperNEMO

LEGEND

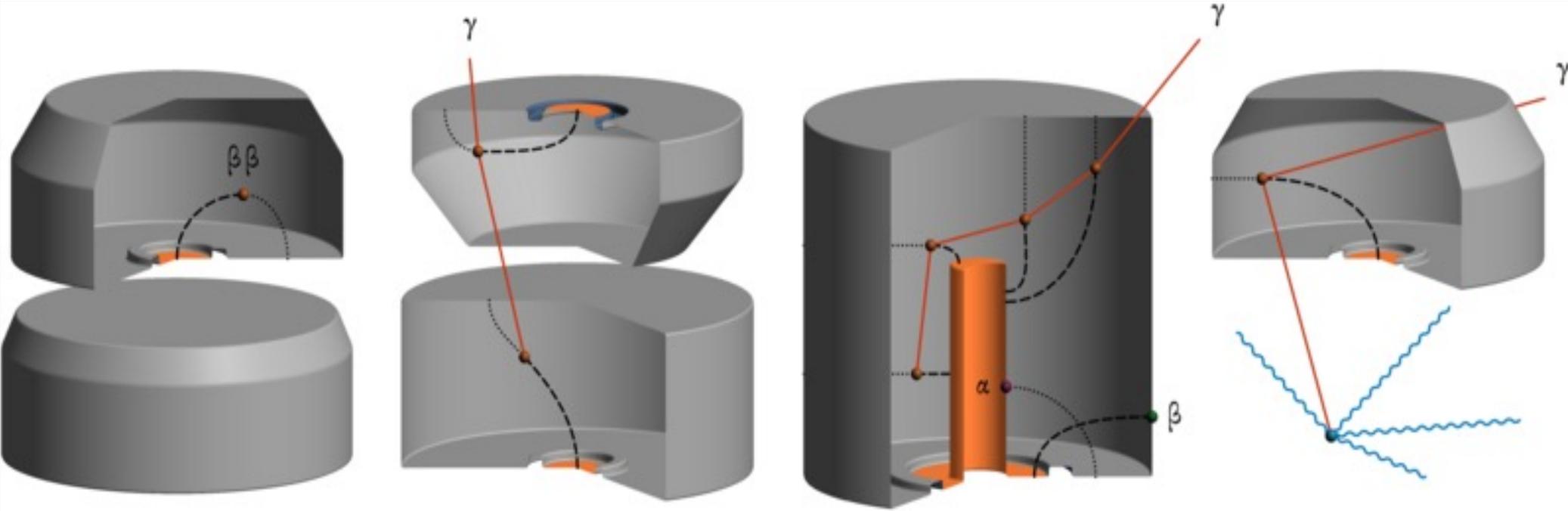
- High Purity Germanium detectors enriched in ^{76}Ge
- Solid state semi-conductors with outstanding energy resolution
- Very pure – low backgrounds
- HPGe commonly used for very low background screening
- Long-standing history for $0\nu\beta\beta$ searches



LEGEND



Background suppression



Single site $\beta\beta$ event

Multi-detector γ event

Multiple interactions γ event and α, β surface events

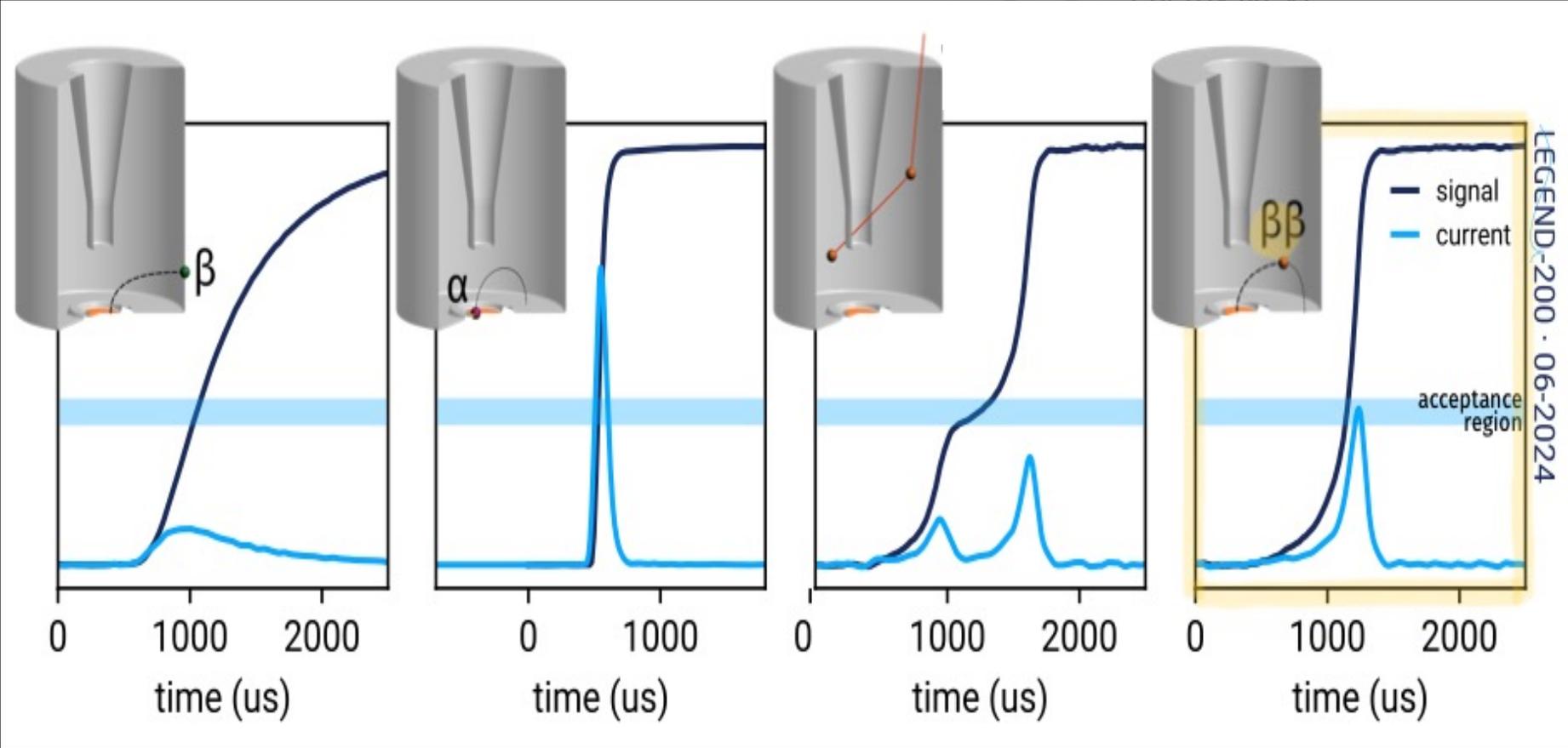
γ event, vetoed by activity in LAr

segmentation

Pulse shape discrimination

External veto

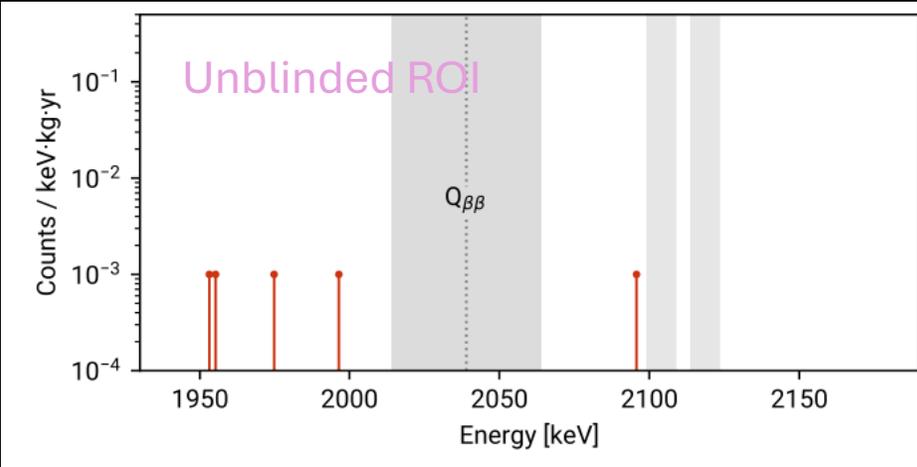
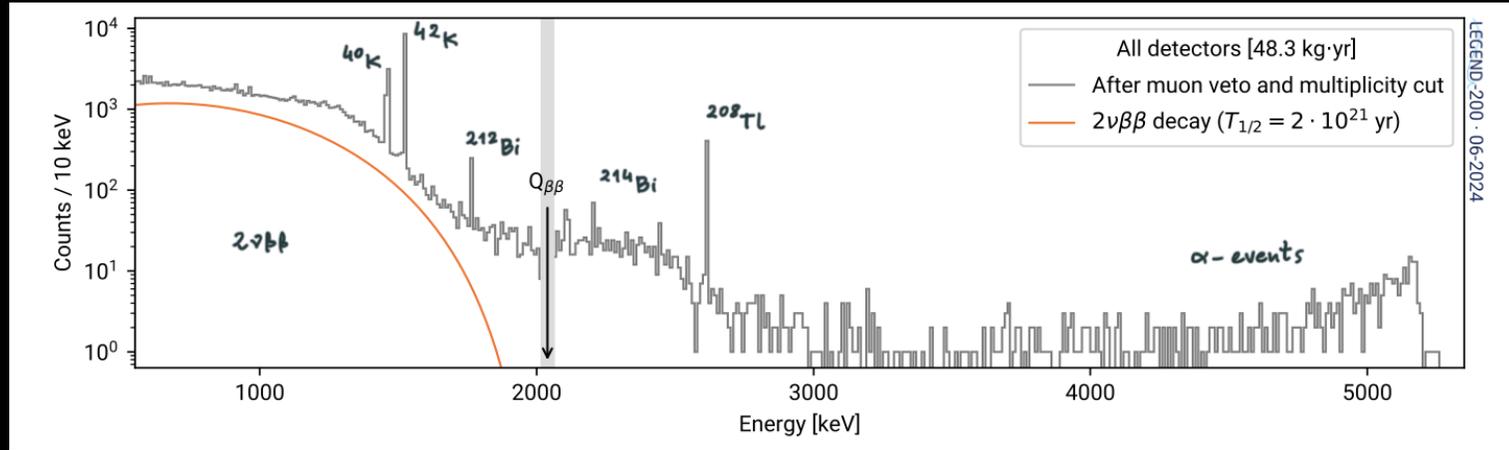
Background suppression



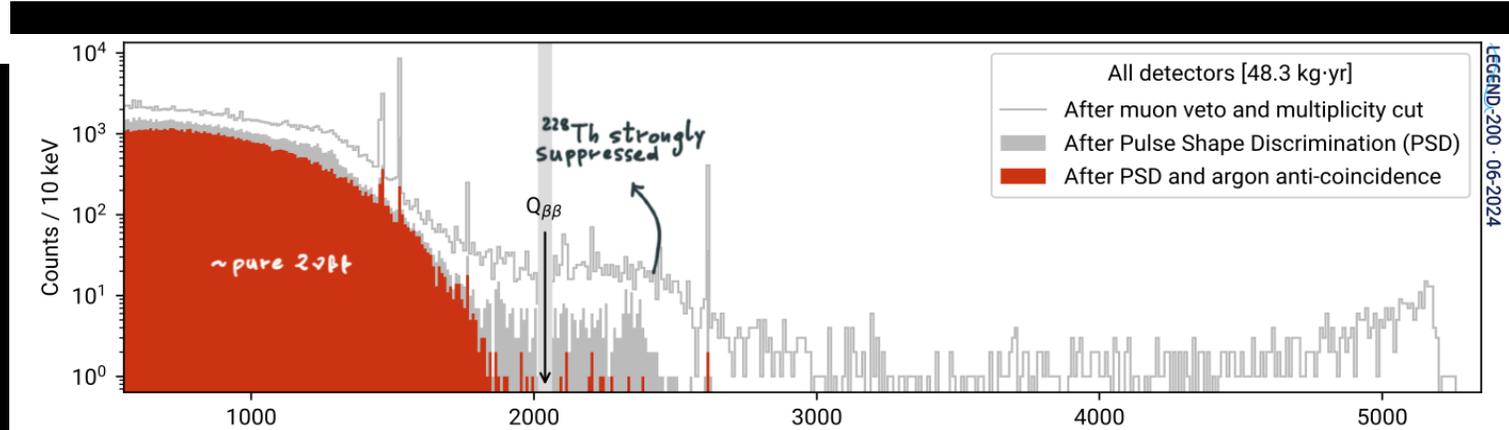
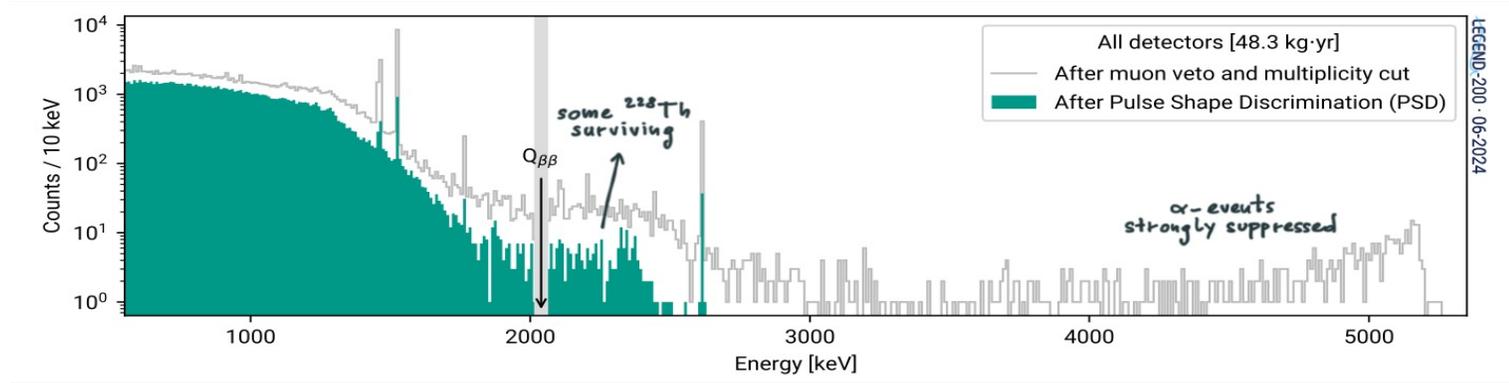
PSD – classify on
max current
Energy

LEGEND-200 data

After muon veto and multiplicity cut



After Argon anti-coincidence



Experiment Examples

- Not a complete list
- Use these examples to illustrate the different backgrounds and challenges

Liquid scintillator

^{136}Xe , ^{130}Te

KamLAND-Zen

SNO+

TPC

^{136}Xe

nEXO, NEXT

Cryogenic
Bolometer

^{130}Te , ^{82}Se

^{130}Te , ^{82}Se

CUORE, CUPID

Semi-conductors

^{76}Ge

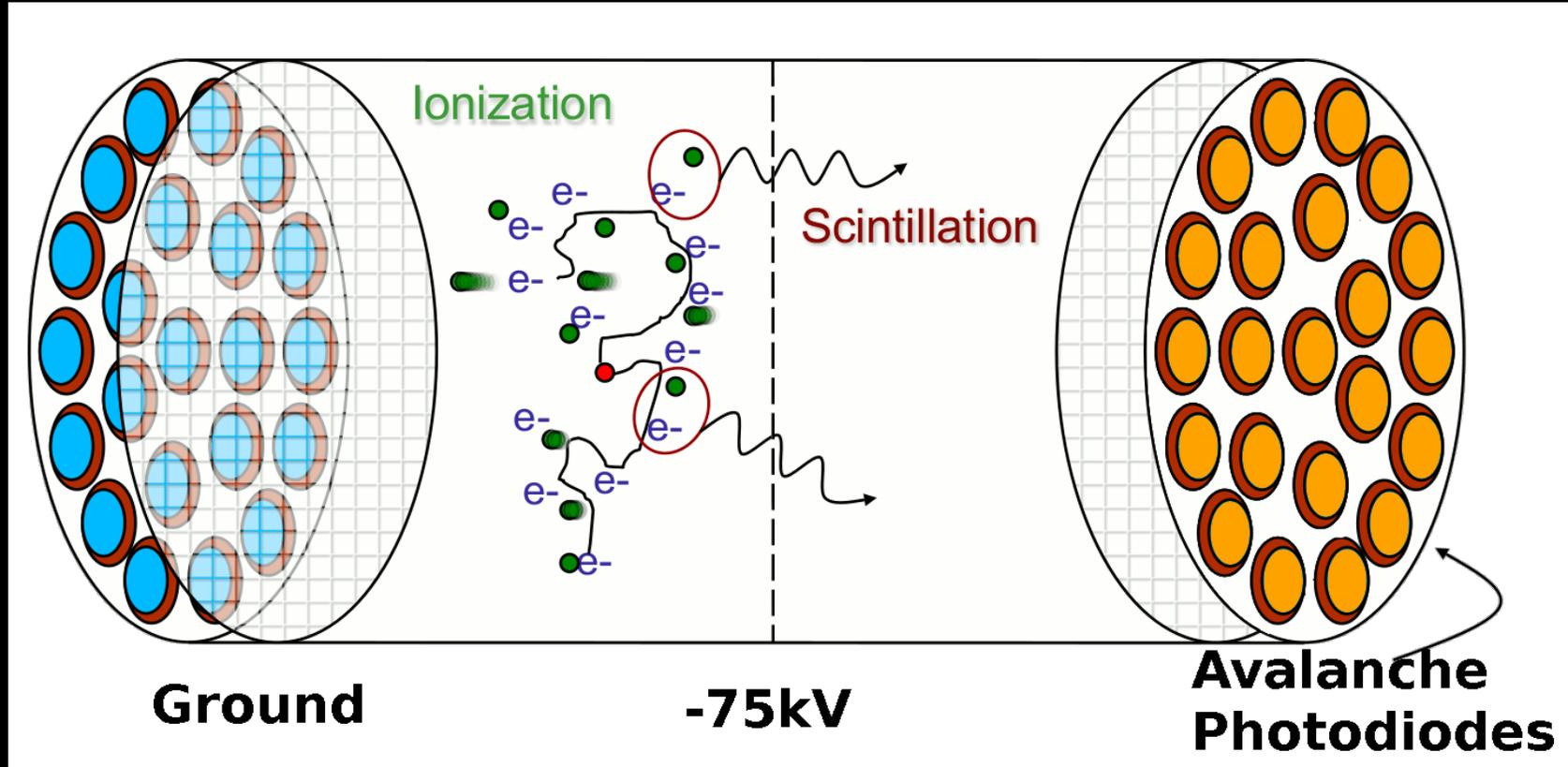
LEGEND

Tracking
calorimeters

^{82}Se

SuperNEMO

Xe TPCs



Charged particles produce light through scintillation and ionized track

Drift electrons to anodes – charge collection at wire grids

Simultaneous measurement of light and charge for better energy resolution and PID

Xe Liquid or Gas

- high pressure better as more isotope
- Requires cryogenics $\rightarrow \sim -95^\circ\text{C}$
- Enrichment of ^{136}Xe

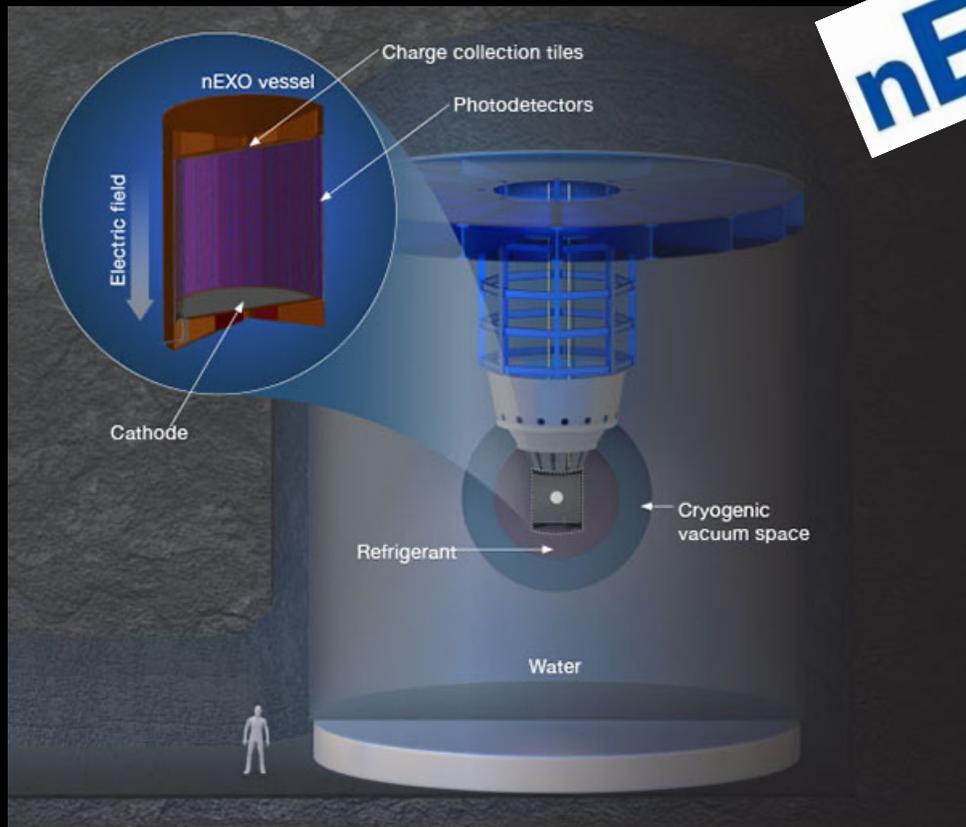
EXO-200

200kg Liquid Xe TPC (80% enrichment)

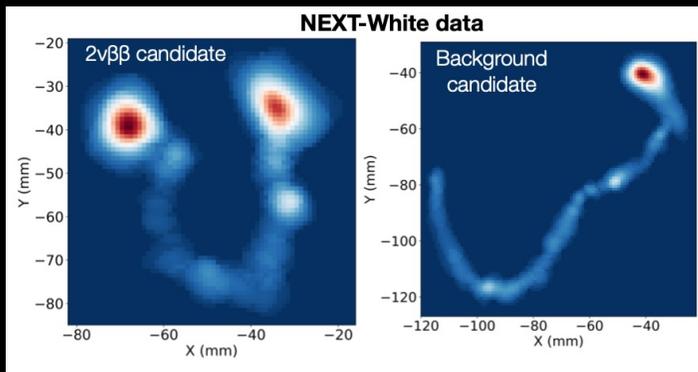
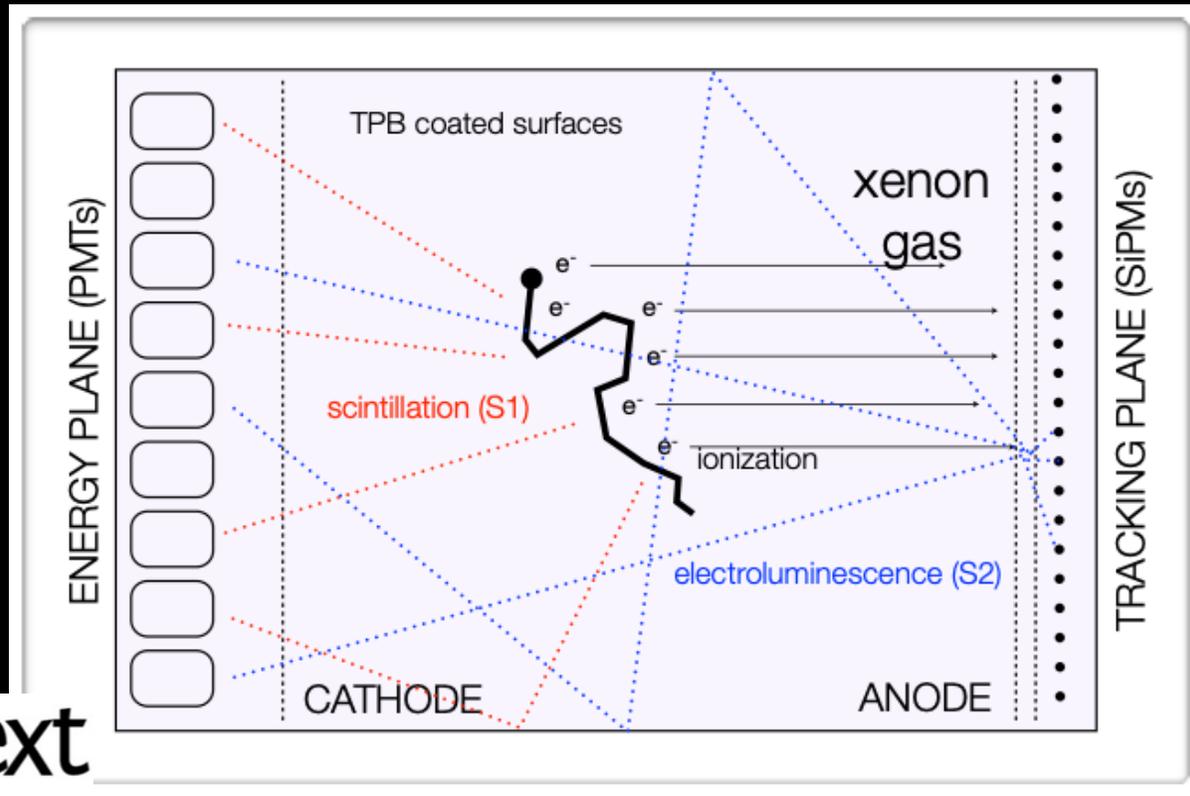
Central photo-cathode
Phys. Rev. Lett. 123, 161802

$T_{1/2} > 3.5 \times 10^{25} \text{ y}$ (90% C.L.)

Xe TPCs



<https://nexo.llnl.gov/nexo-overview>

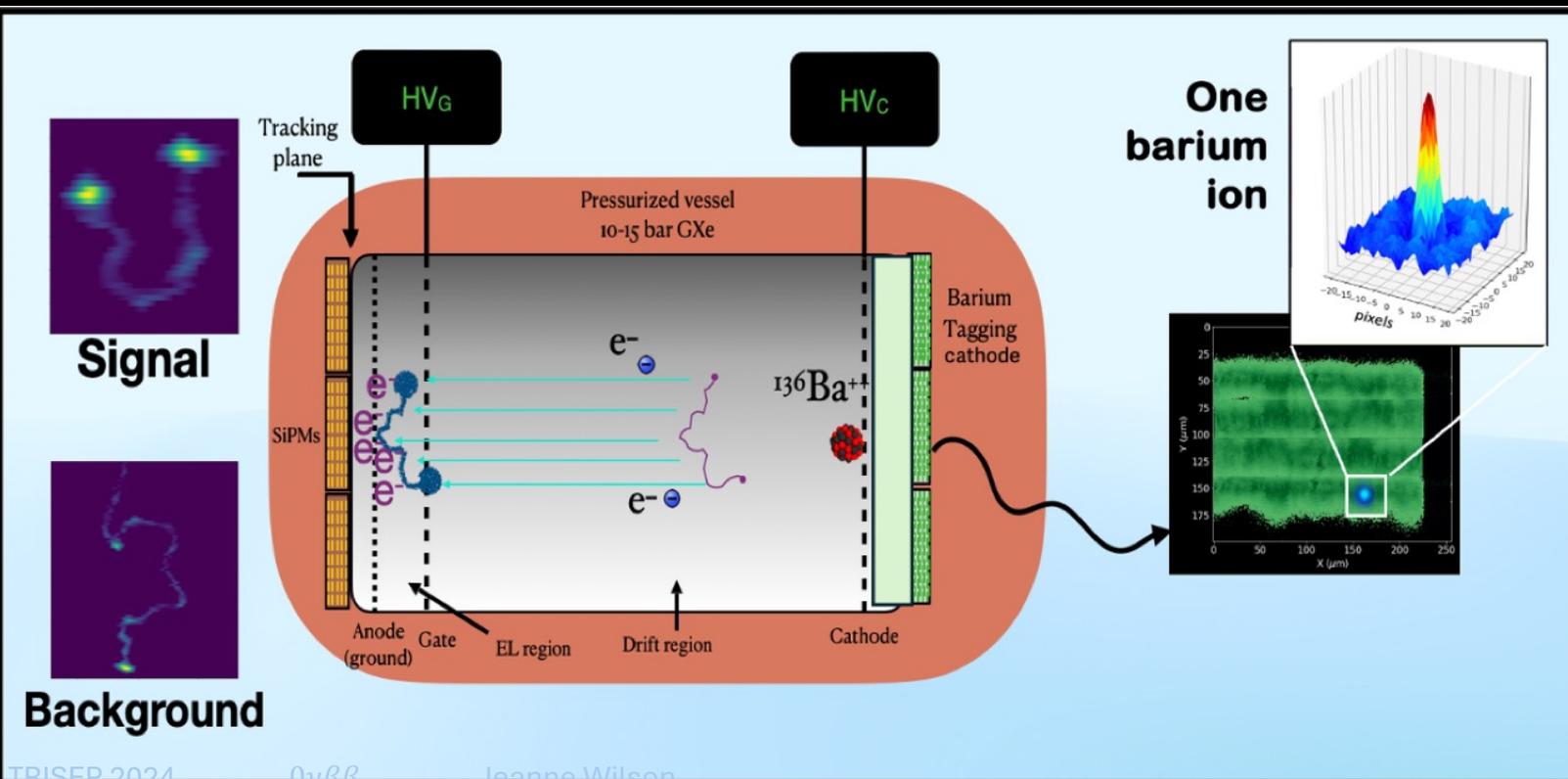
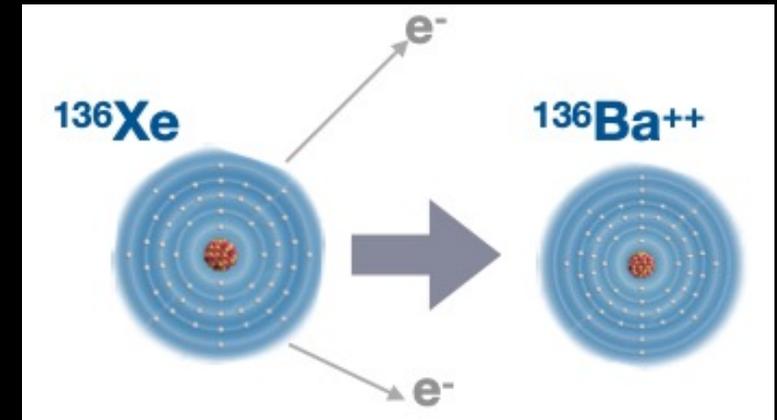


High pressure Xe gas TPC with electroluminescence

Topological signal/background separation

^{136}Xe daughter tagging

The Ba^{++} ion is only produced from $\beta\beta$ decay
If this can be tagged, distinguish $\beta\beta$ from all other radioactive events



Active R&D:

- Drift ++ ion to cathode
- Trap Ba – eg. cryogenic probe
- chemical sensors/ fluorescence

Eg <https://www.nature.com/articles/s41586-019-1169-4>

Experiment Examples

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calorimeters

^{82}Se

SuperNEMO

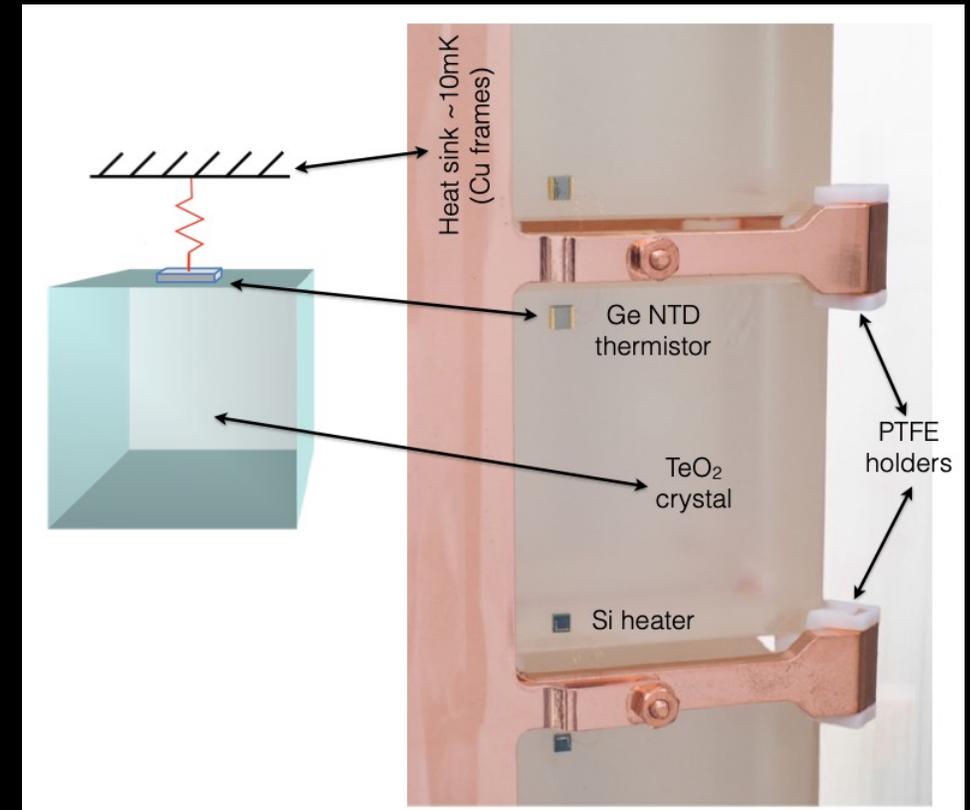
CUORE



- Closely packed array of 988 TeO_2 crystals (750g each) working as cryogenic calorimeters
- Absorbed energy converted into temperature variation of crystal, measured by thermistor
 - Energy resolution $\sim 0.3\%$ *FWHM*

Challenges:

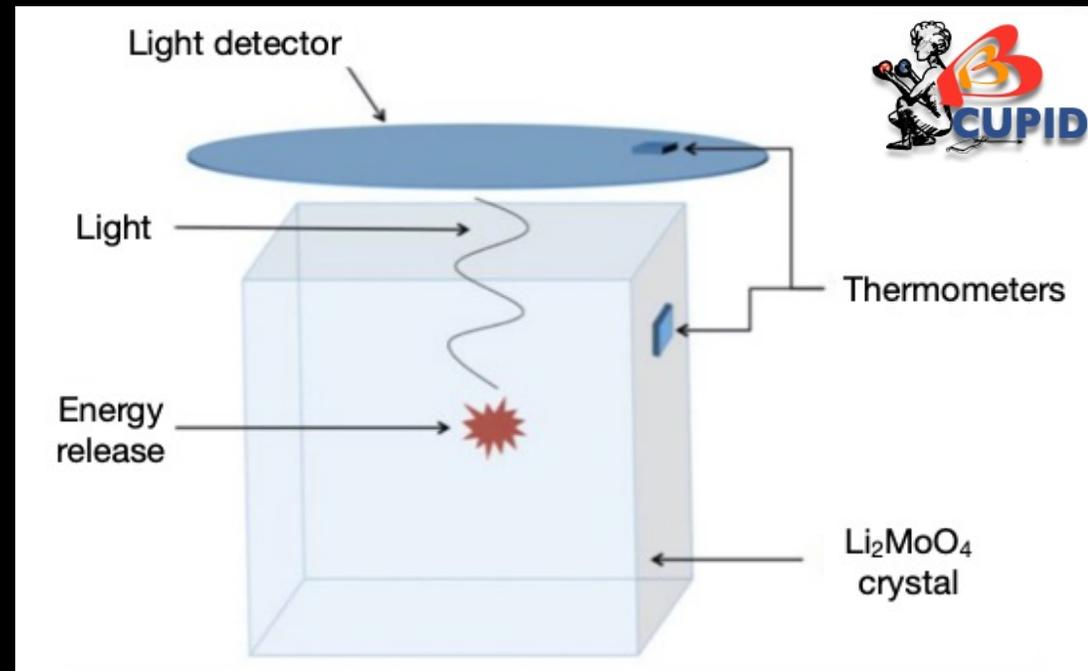
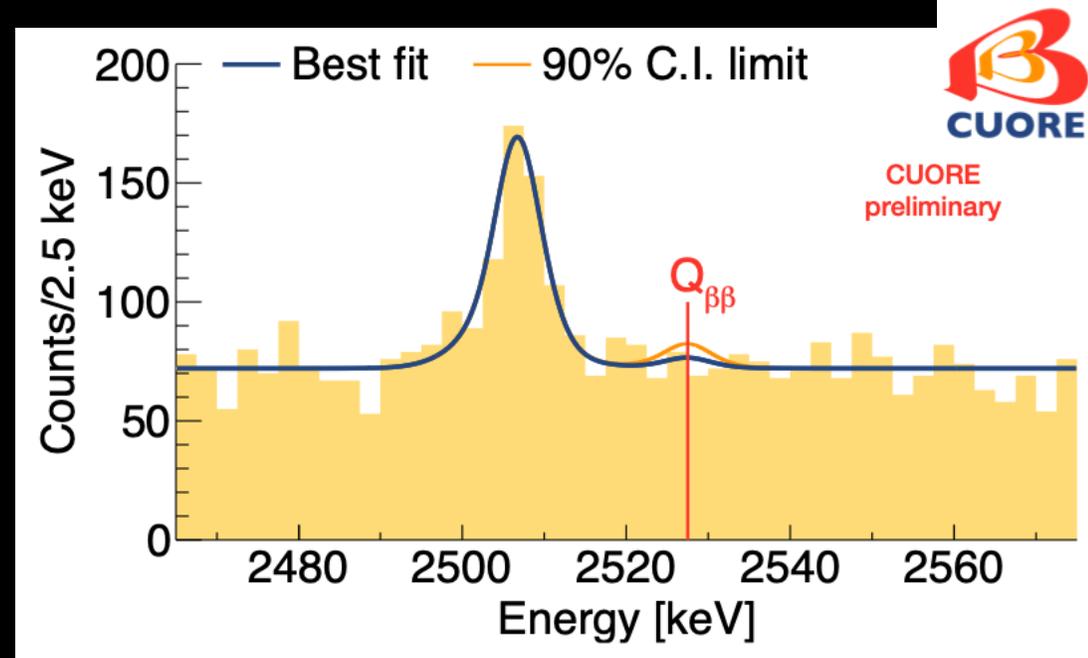
- operating temperature $\sim 10\text{mK}$!
- Surface backgrounds
- Sensitive to vibrations and seismic activity
 - Correlation between storms and low f noise
 - Sea waves!



CUPID

CUORE Upgrade with Particle Identification

- Li_2MoO_4 crystals enrich to 95% ^{100}Mo
- Higher $Q_{\beta\beta}$ for reduced γ/β backgrounds
- Both temperature and light detection for PID – rejection of surface α s



Experiment Examples

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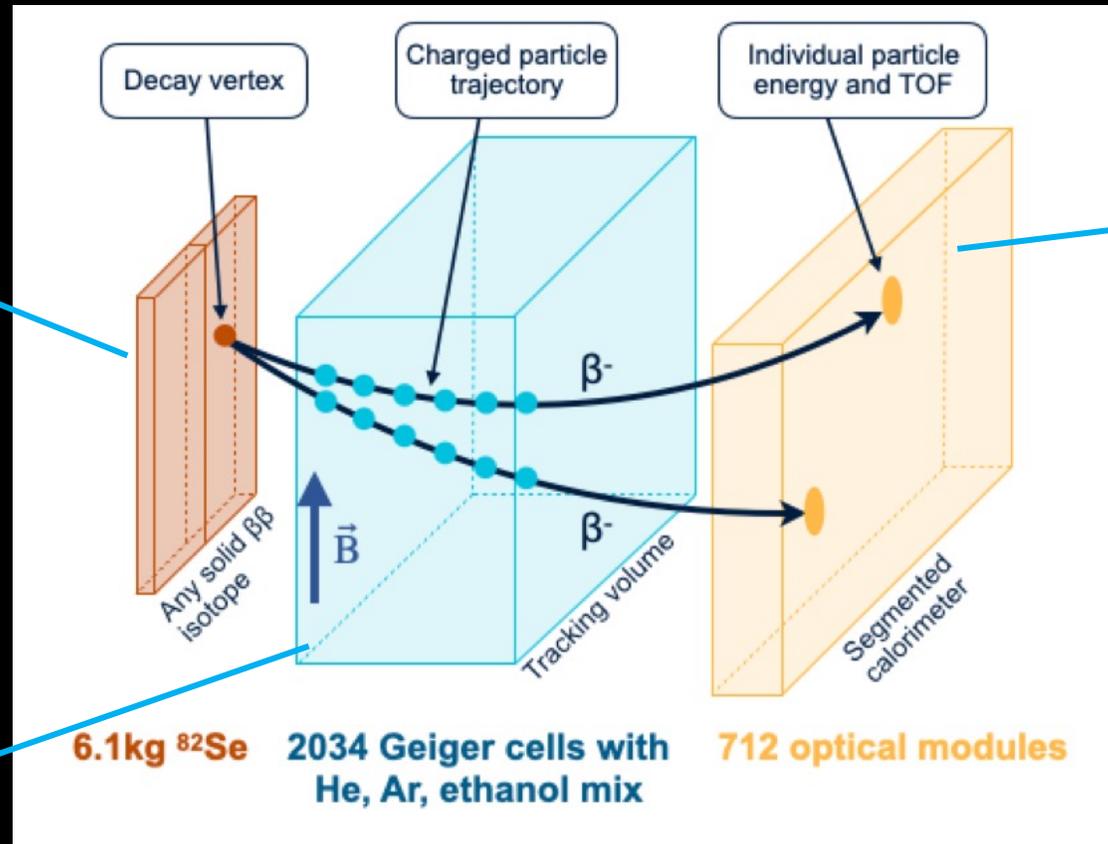
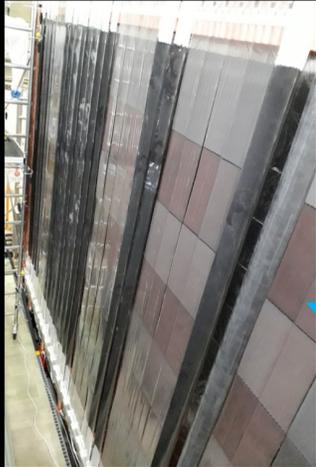
Tracking
calorimeters

^{82}Se

SuperNEMO

SuperNEMO

- An isotope agnostic technique to distinguish individual particles, and probe $0\nu\beta\beta$ mechanisms and nuclear effects

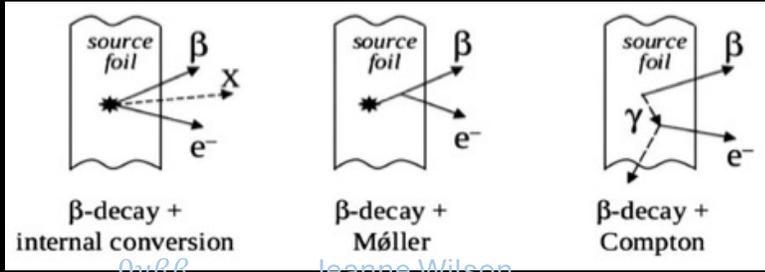
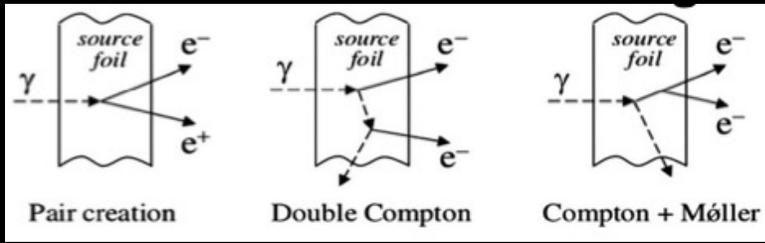
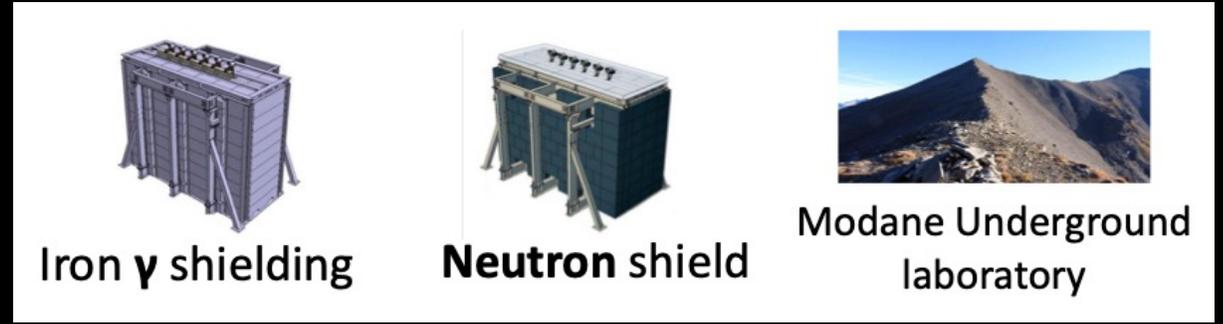


$1.8\% \sigma/E$ at 3MeV



SuperNEMO shielding

- Source \neq detector
- Great care with incoming backgrounds
 - U & Th in lab rock walls \rightarrow shielding
 - Radon in lab air \rightarrow anti-radon system



Experiments

- There are many experimental contenders
- Different strengths and weaknesses / challenges

- Require significant investment and international collaboration
- Complementarity important for discovery:
 - Different isotopes
 - Different techniques / locations

Top Trumps

- SNO+
- KamLAND-Zen
- LEGEND
- nEXO
- NEXT-HD
- NEXt-BOLD
- CUORE
- CUPID
- SuperNEMO
- AMORE
- PANDA-X
- Selena
- EXO-200
- Gerda
- Majorana demonstrator
- NEMO-3

<https://tinyurl.com/BBTopTrumps>



Name:

Isotope:

Method:

Main challenges:

Q-value / Phase Space:

Mass of Isotope:

Background Index:

Discovery Sensitivity:

Start of Data Taking:

Special Features:

<https://tinyurl.com/BBTopTrumps>



Summary – lecture 2

- How the rate of $0\nu\beta\beta$ relates to neutrino mass
 - Matrix element uncertainties
- How the rate of $0\nu\beta\beta$ relates to experiment design
 - Choice of isotope, mass
- Experimental challenges
 - Backgrounds! Backgrounds! Backgrounds !
- Experiment Examples
 - Liquid scintillator: isotope loading, reconstruction, background rejection
 - HPGe: PSD and energy resolution, readout
 - Xe TPCs: Track information, daughter tagging
 - Bolometers: cryogenics, surface backgrounds
 - Separate source, tracking + calorimetry: shielding and radon suppression