

# NEUTRINO SCIENCE 4

J. MANEIRA  
LIP, LISBON, PORTUGAL



SUSI 2024  
SNOLAB UNDERGROUND SCIENCE INSTITUTE  
JULY 22 - AUGUST 2, 2024 SUDBURY, CANADA

1. Neutrinos in the Standard Model.
2. Neutrino interactions, detectors. Solar and atmospheric neutrino problems.
3. Neutrino oscillations in 2 flavors. SNO and SK.
4. Neutrino oscillations in 3 flavors. Future experiments.
5. Theory and search for neutrino masses. Neutrinoless double-beta decay. Neutrinos in Cosmology and Astrophysics.

- Theory and experiment will be strongly mingled.
- Every lecture will have some of both.

- Finding evidence for oscillations
  - with atmospheric neutrinos: Super-Kamiokande
  - ... and early confirmations with terrestrial sources: K2K, MINOS
- Three-flavor neutrino mixing
  - Neutrino mass ordering
  - Pontecorvo-Maki-Nakagawa-Sakata (PMNS) matrix and three-flavor oscillations
  - CP violation and matter effects
- Current experimental status
- Future experiments

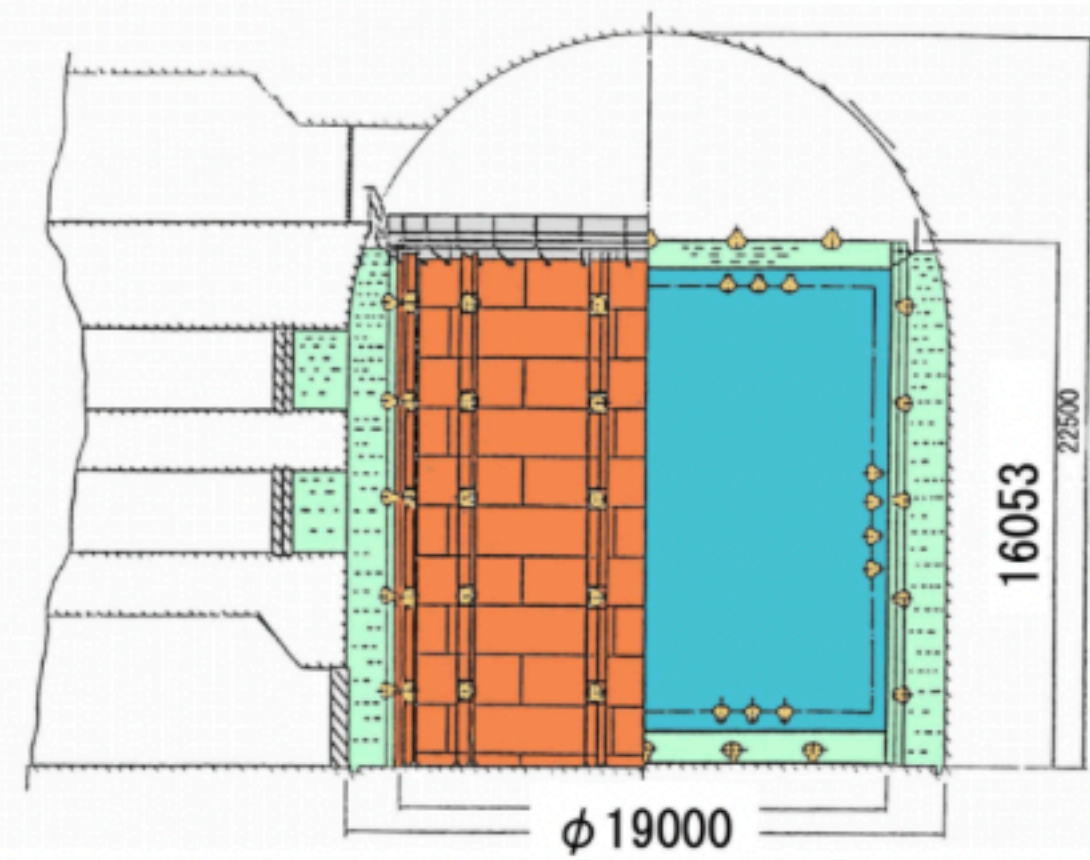
**SUPER-KAMIOKANDE**

# CHERENKOV DETECTORS IN JAPAN



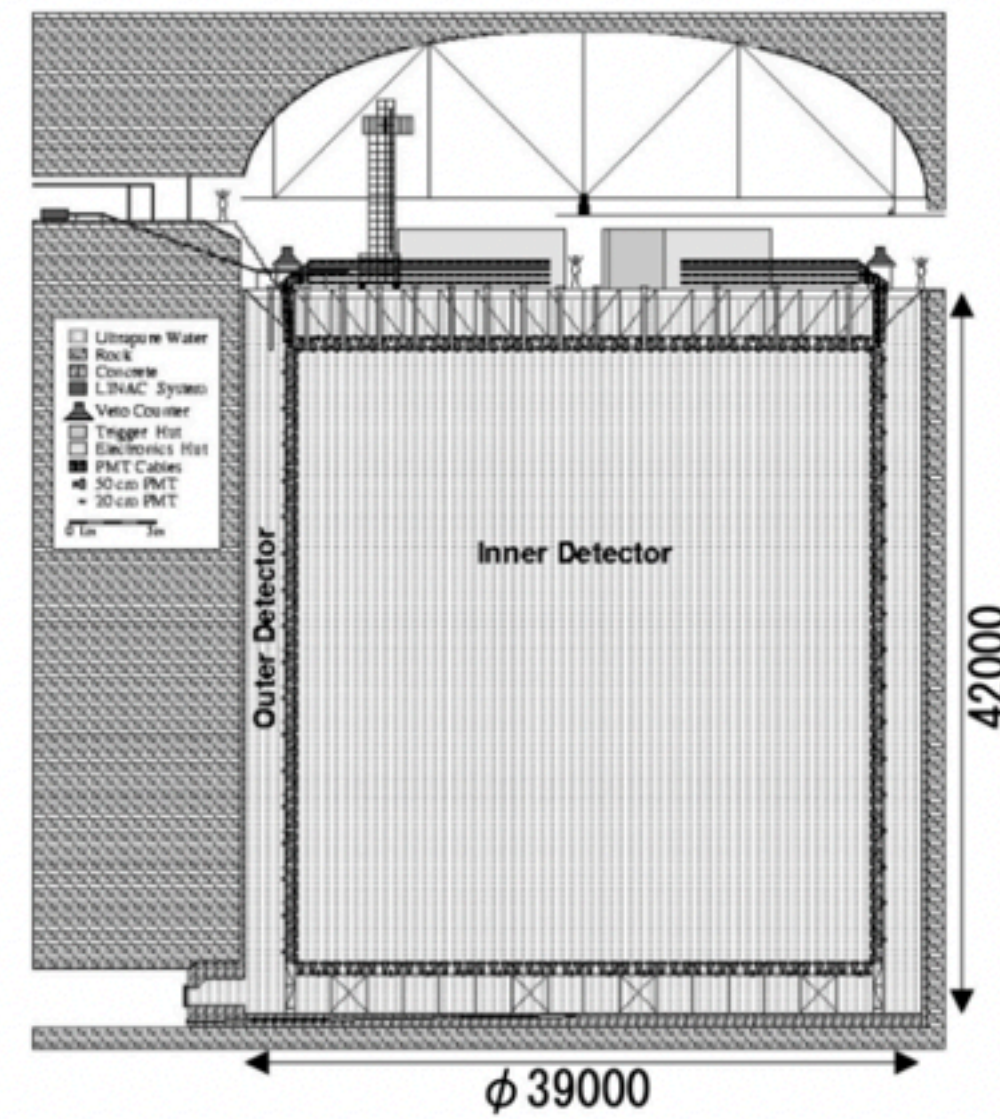
## Kamiokande

1983~1996



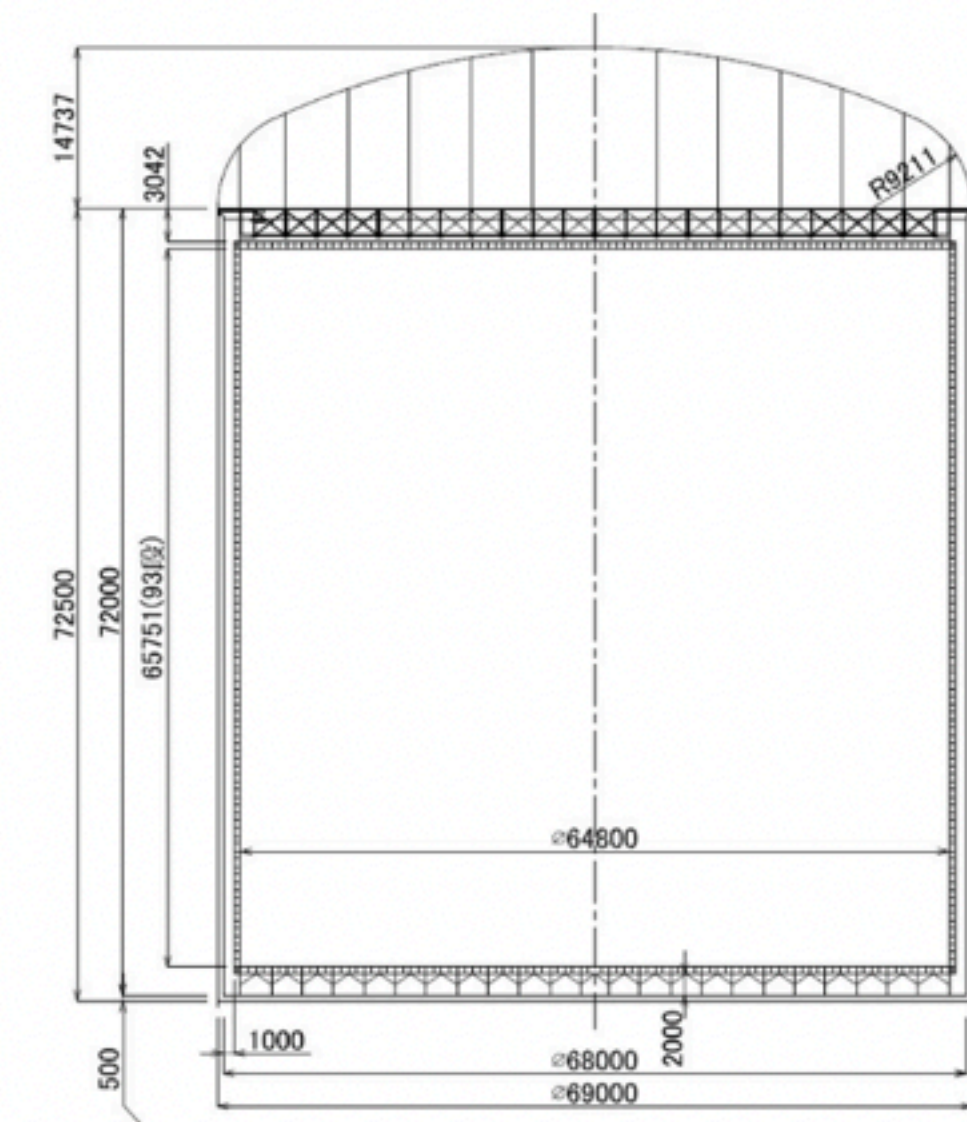
## Super-Kamiokande

1996~Present



## Hyper-Kamiokande

Aiming to start observation in 2027



19m diameter x 16m high

4500 ton  
(680~1040 ton) *Total mass*  
*Fiducial mass*

50 cm diameter / 948 PMTs

39m diameter x 42m high

50000 ton  
(22500 ton)

50cm diameter / 11146

68m diameter x 71m high

260000 ton  
(190000 ton)

50cm diameter / about 40000

# SUPER-KAMIOKANDE

- Largest detector sensitive to solar neutrino energies: 22.5 kton fiducial
- Recently published: complete analysis of SK phases I - IV: over 20 years of data!!
  - Significant improvements in energy reconstruction and uncertainties
- Since 2020: SK-V (prep for Gd), SK-VI (0.01% Gd), SK-VII (0.03% Gd)

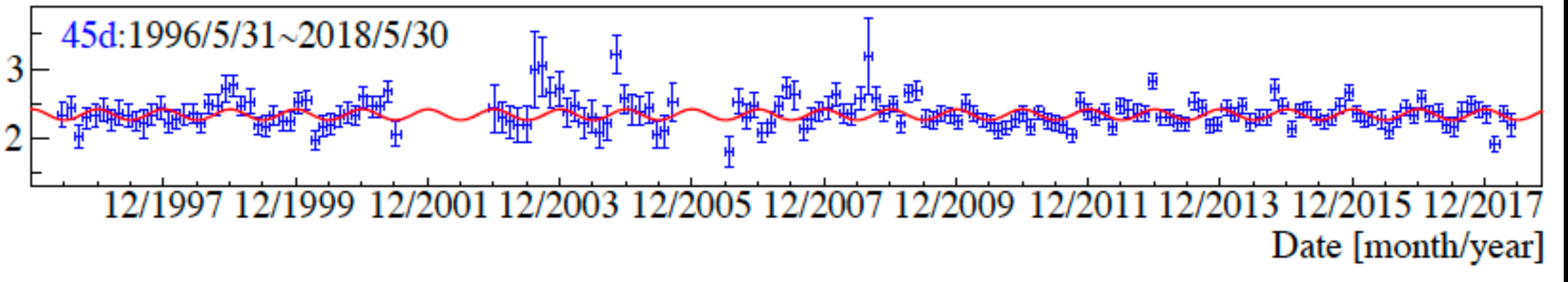
# SUPER-KAMIOKANDE SOLAR

Following slides from my recent talk at Neutrino 2024

# TIME VARIATIONS OF $^8\text{B}$ FLUX



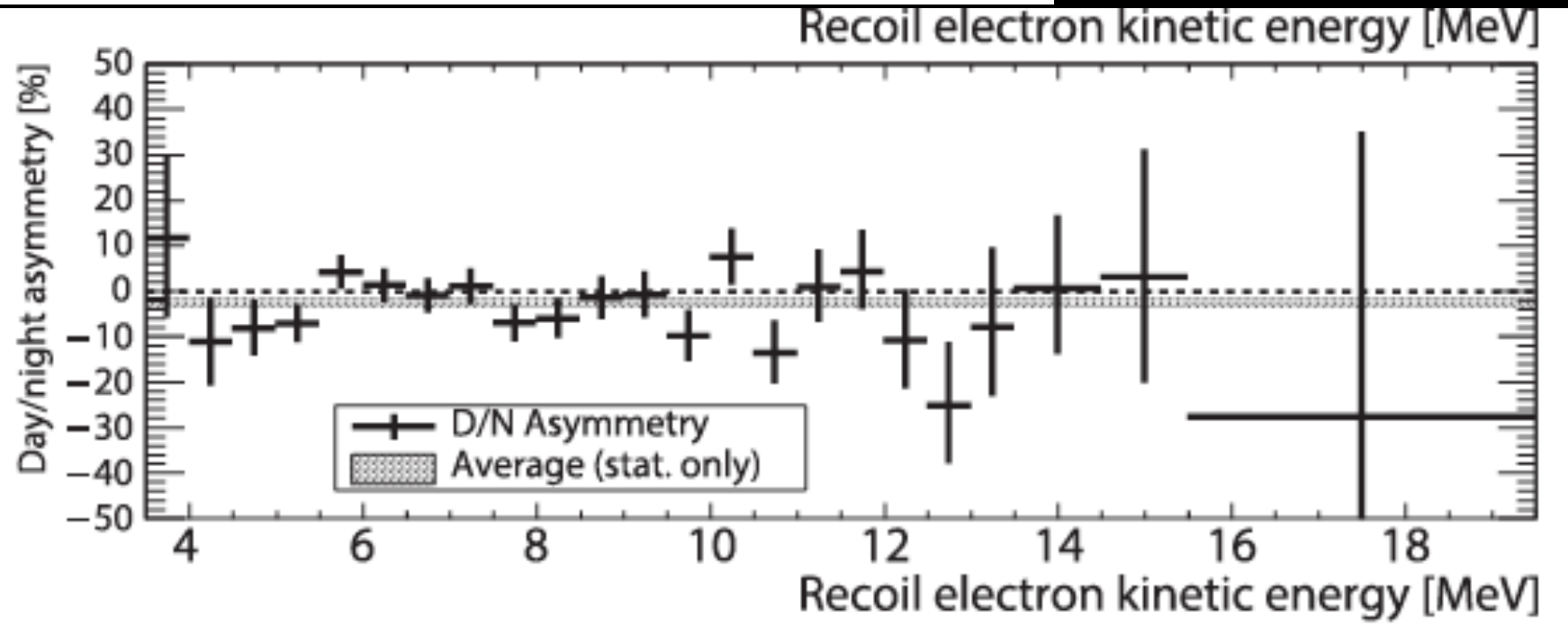
Phase	SK-I	SK-II	SK-III	SK-IV
Period (Start)	April '96	October '02	July '06	September '08
Period (End)	July '01	October '05	August '08	May '18
Livetime [days]	1,496	791	548	2,970
ID PMTs	11,146	5,182	11,129	11,129
OD PMTs	1,885	1,885	1,885	1,885
PMT coverage [%]	40	19	40	40
Energy thr. [MeV]	4.49	6.49	3.99	3.49



Very precise rate measurement, consistent among various phases

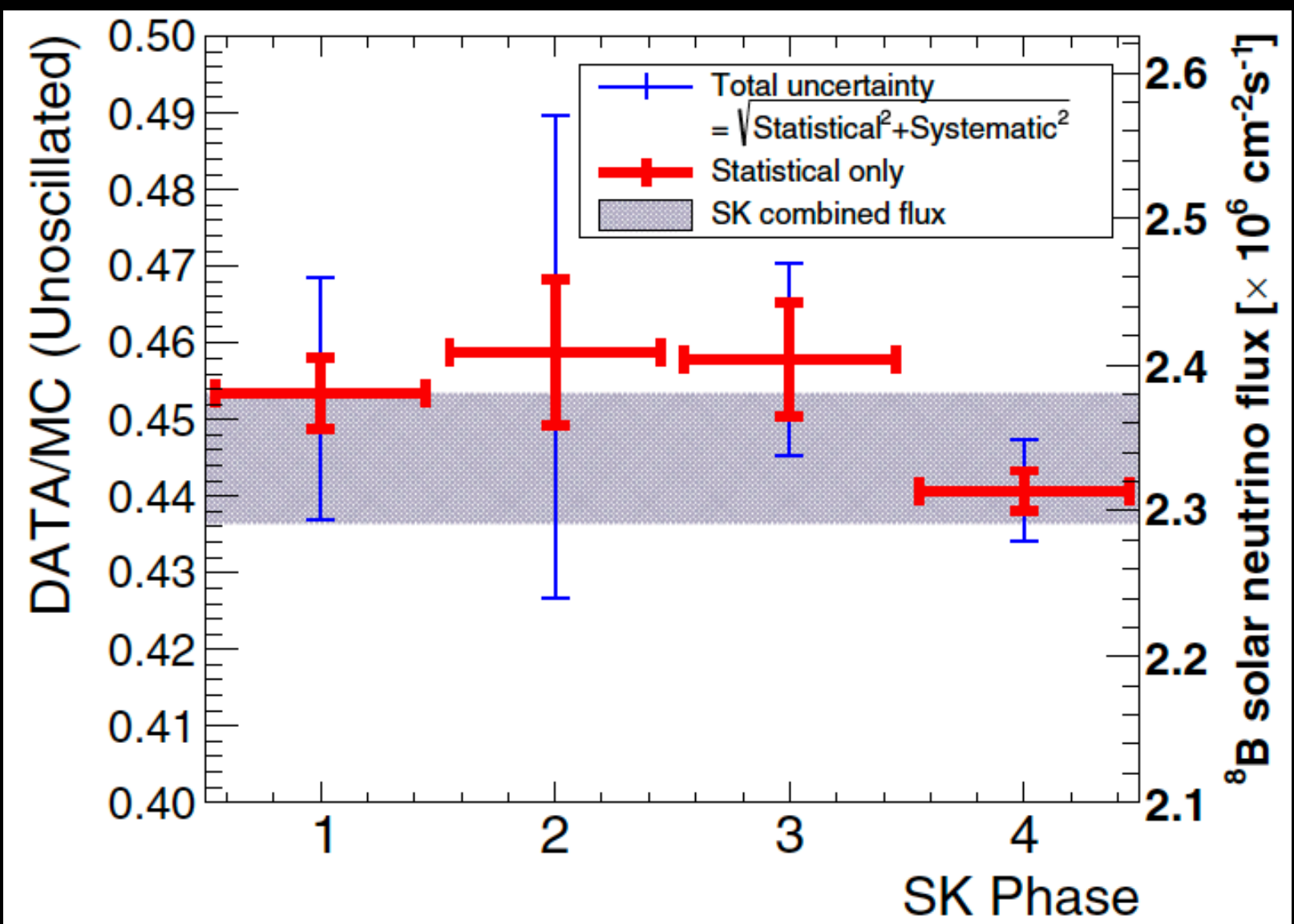
Day/night Asymmetry  
SK-IV only, calc.

$$A_{D/N}^{SK-IV, \text{ calc}} = -0.025 \pm 0.012(\text{stat.}) \pm 0.014(\text{syst.}).$$

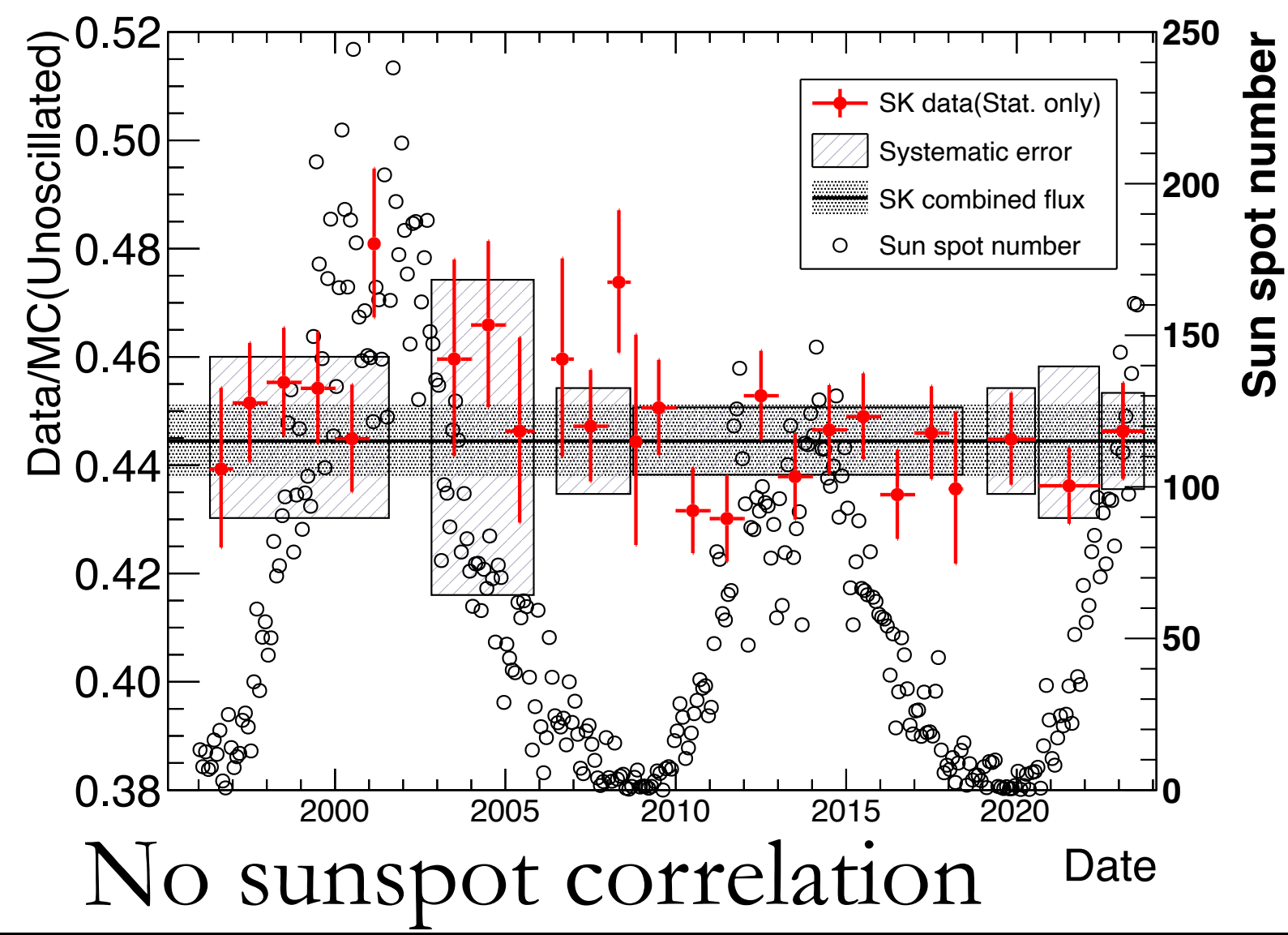


SK I-IV combined fit,  $> 3 \sigma$

$$A_{D/N}^{SK, \text{ fit}} = -0.0286 \pm 0.0085(\text{stat.}) \pm 0.0032(\text{syst.}).$$



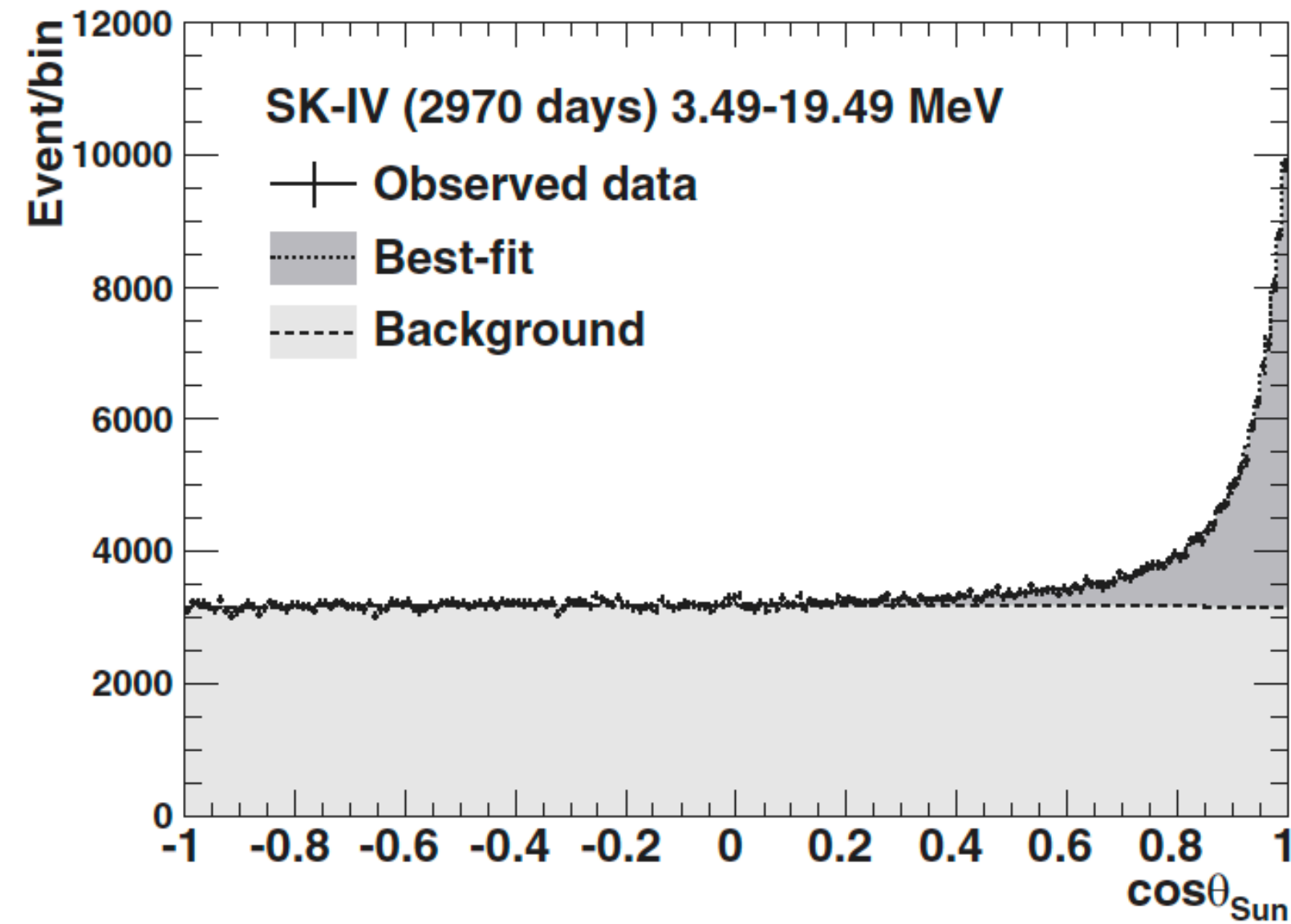
No statistically significant time variations beyond eccentricity and day/night (compatible with MSW oscillations)



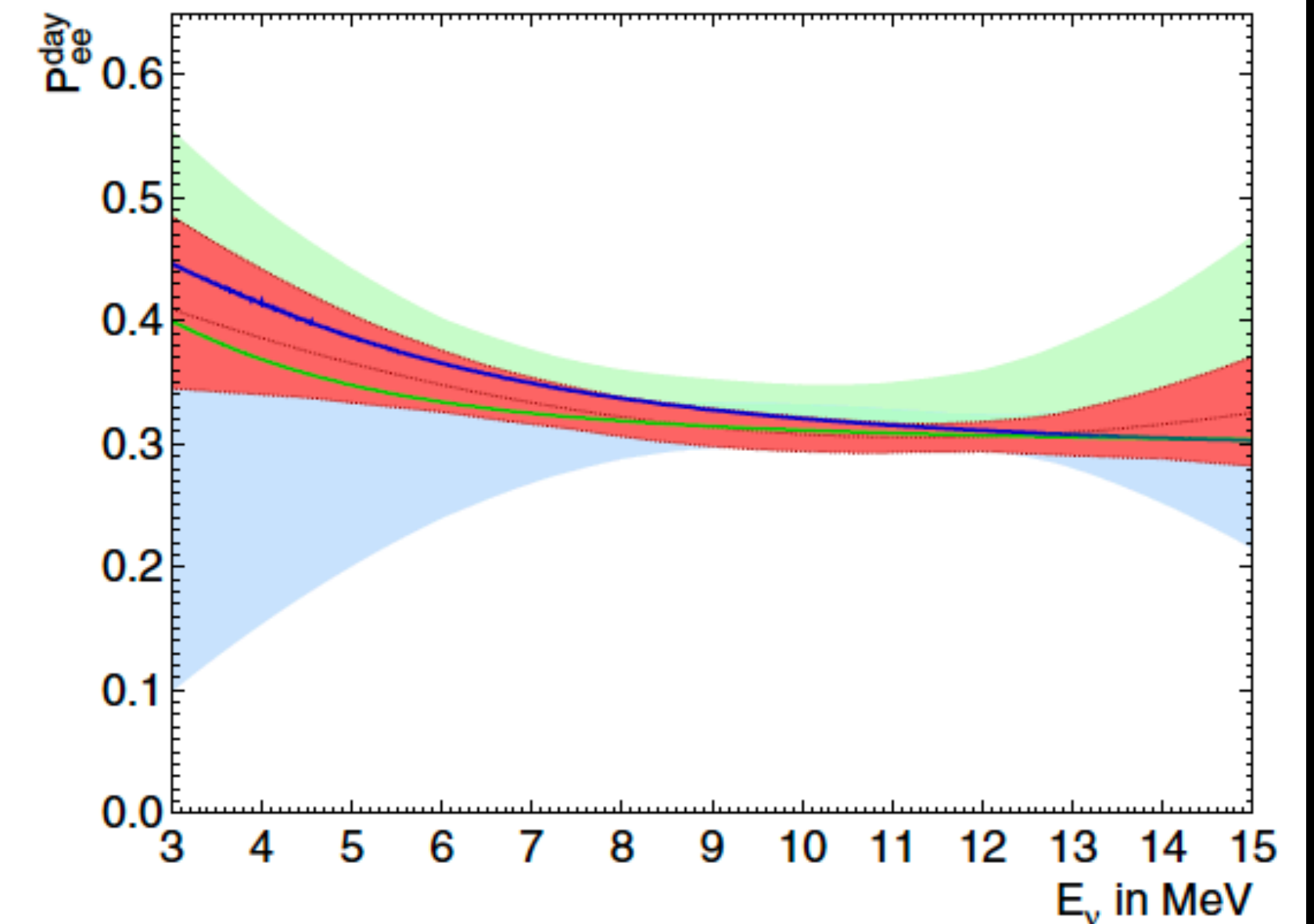
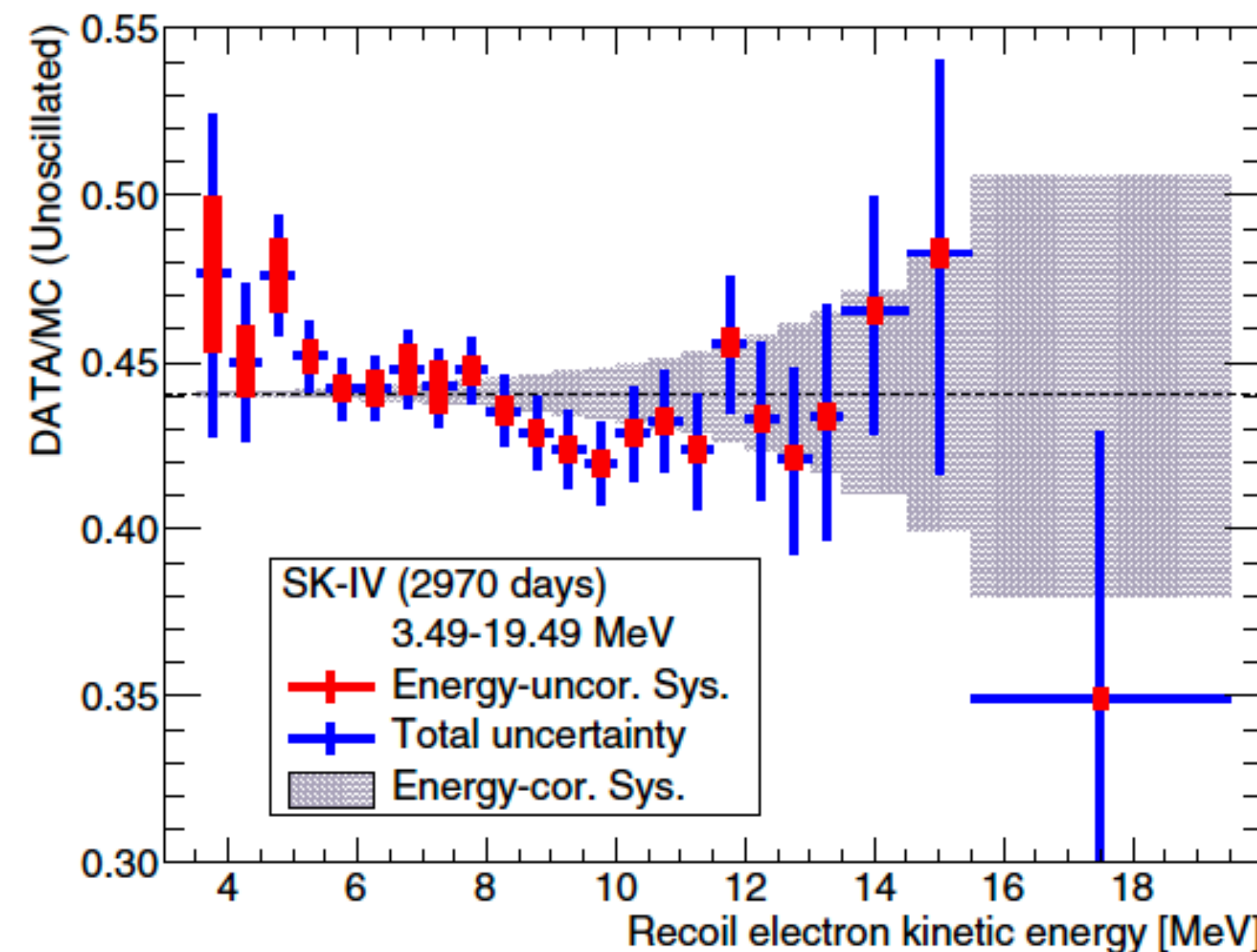
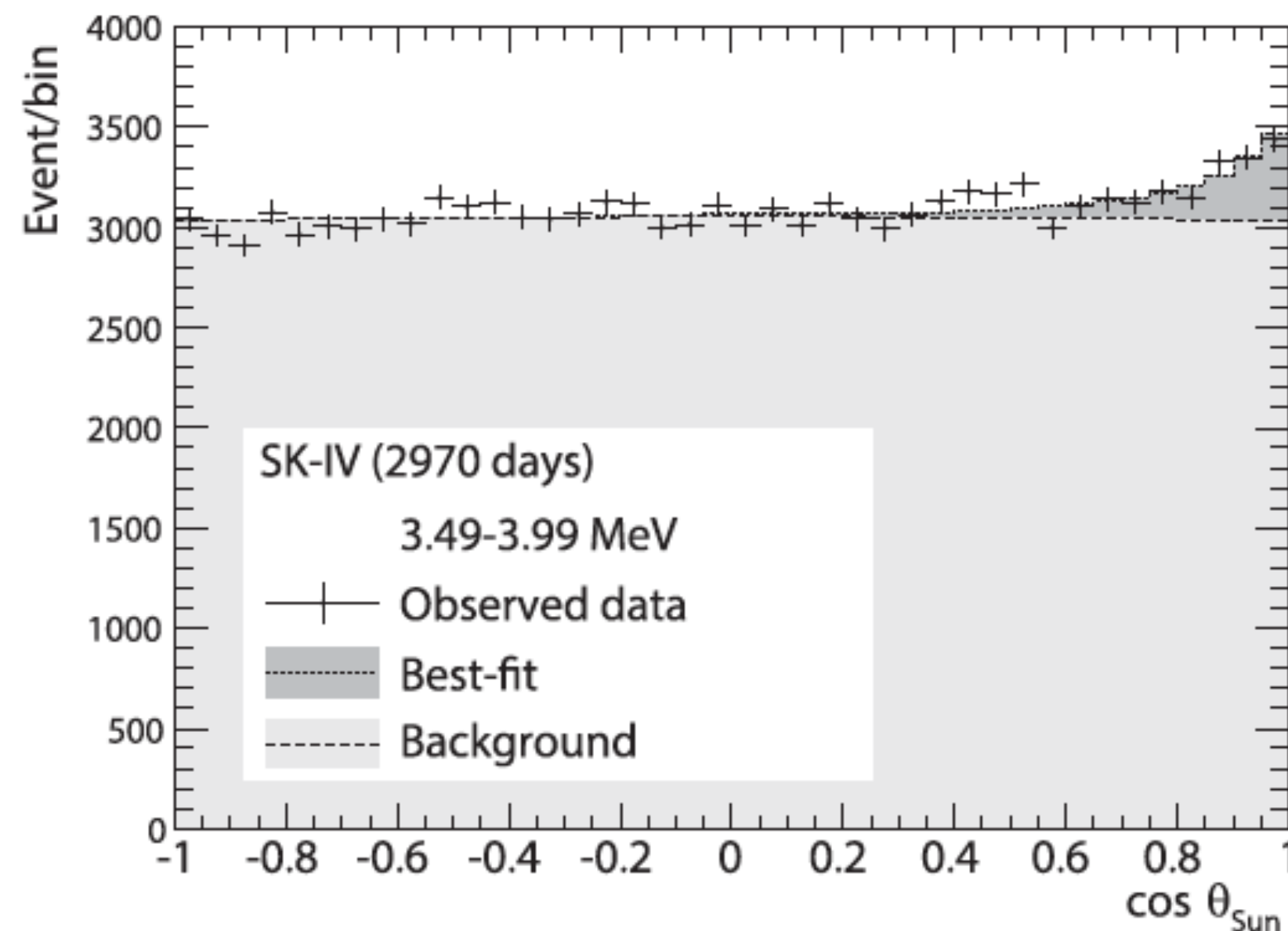
No sunspot correlation

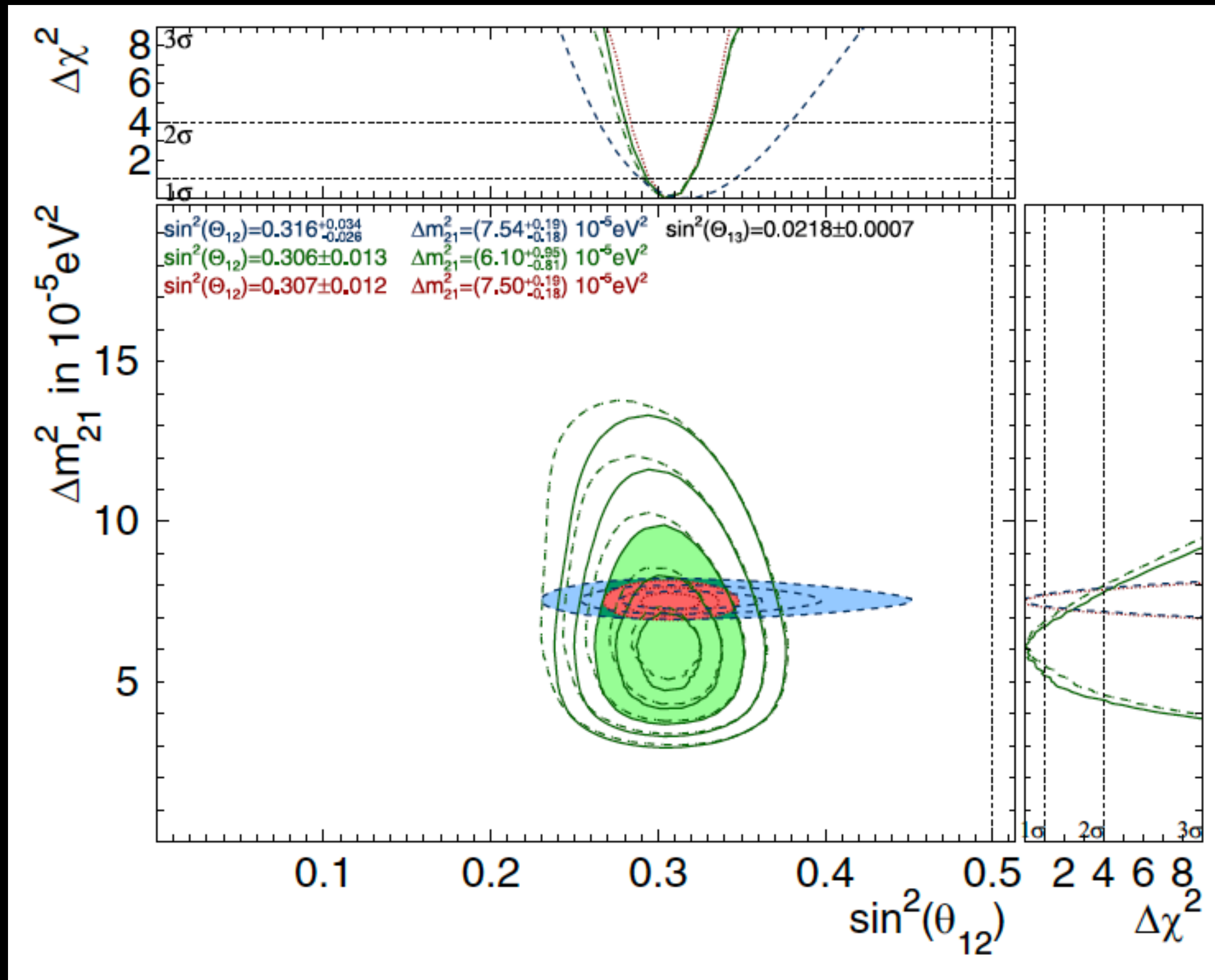


# $^8\text{B}$ SOLAR NEUTRINO SPECTRUM



- Impressive precision, clear observation at 3.5 MeV threshold
- Spectrum still compatible with flat survival probability, but predicted low energy upturn is favored at  $1.2 \sigma$ . Jointly with SNO data, at  $2.1 \sigma$ .





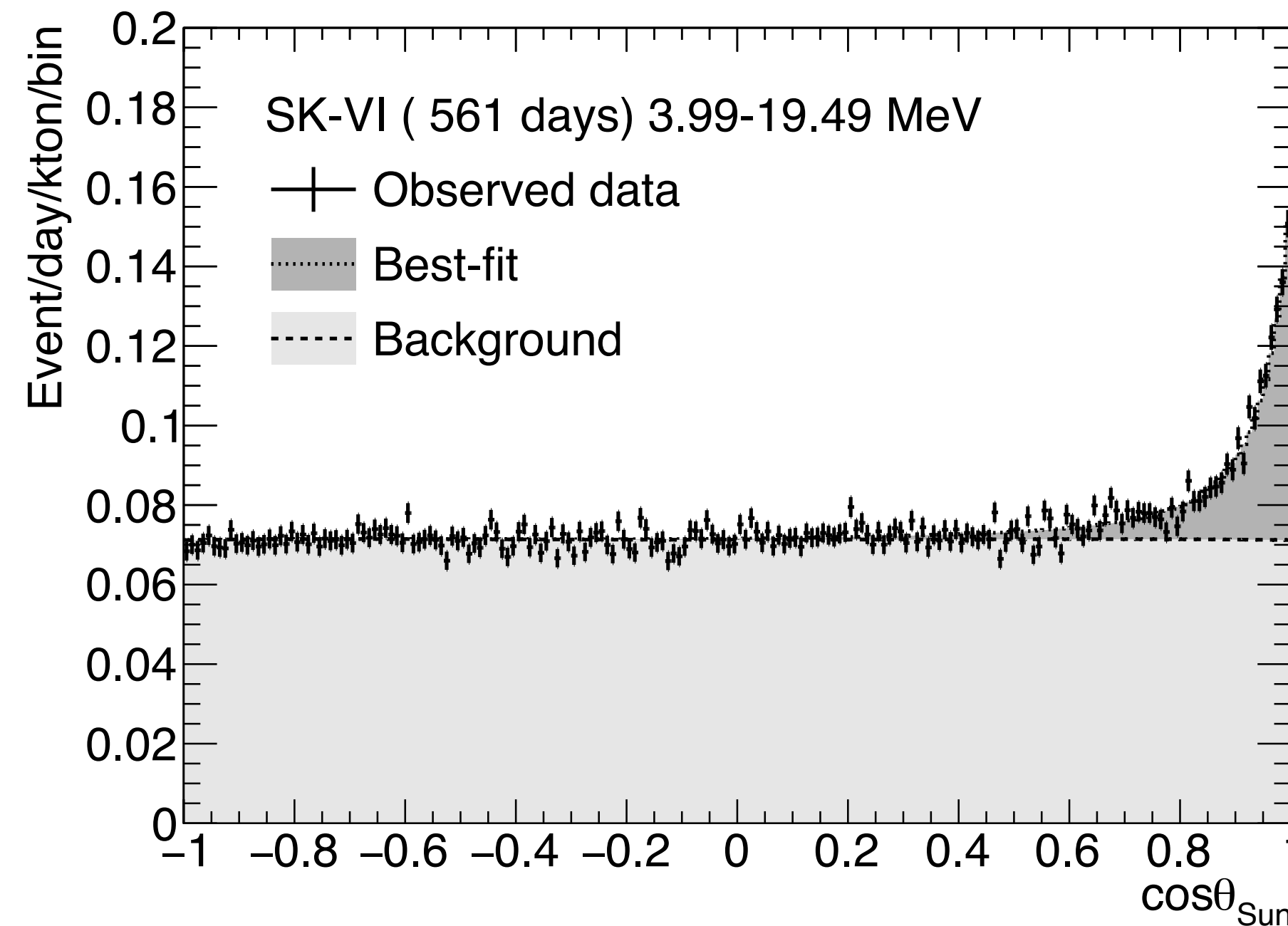
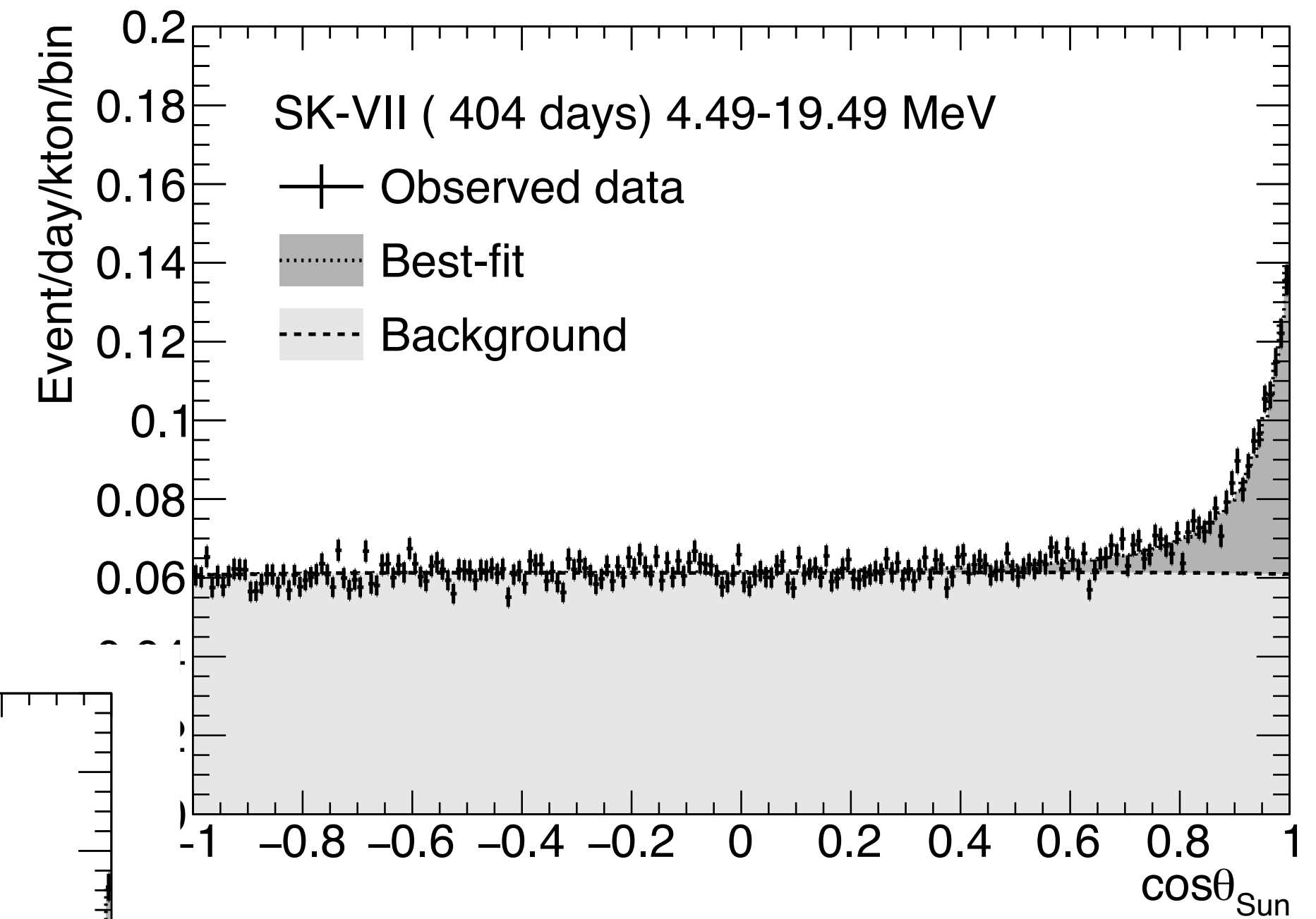
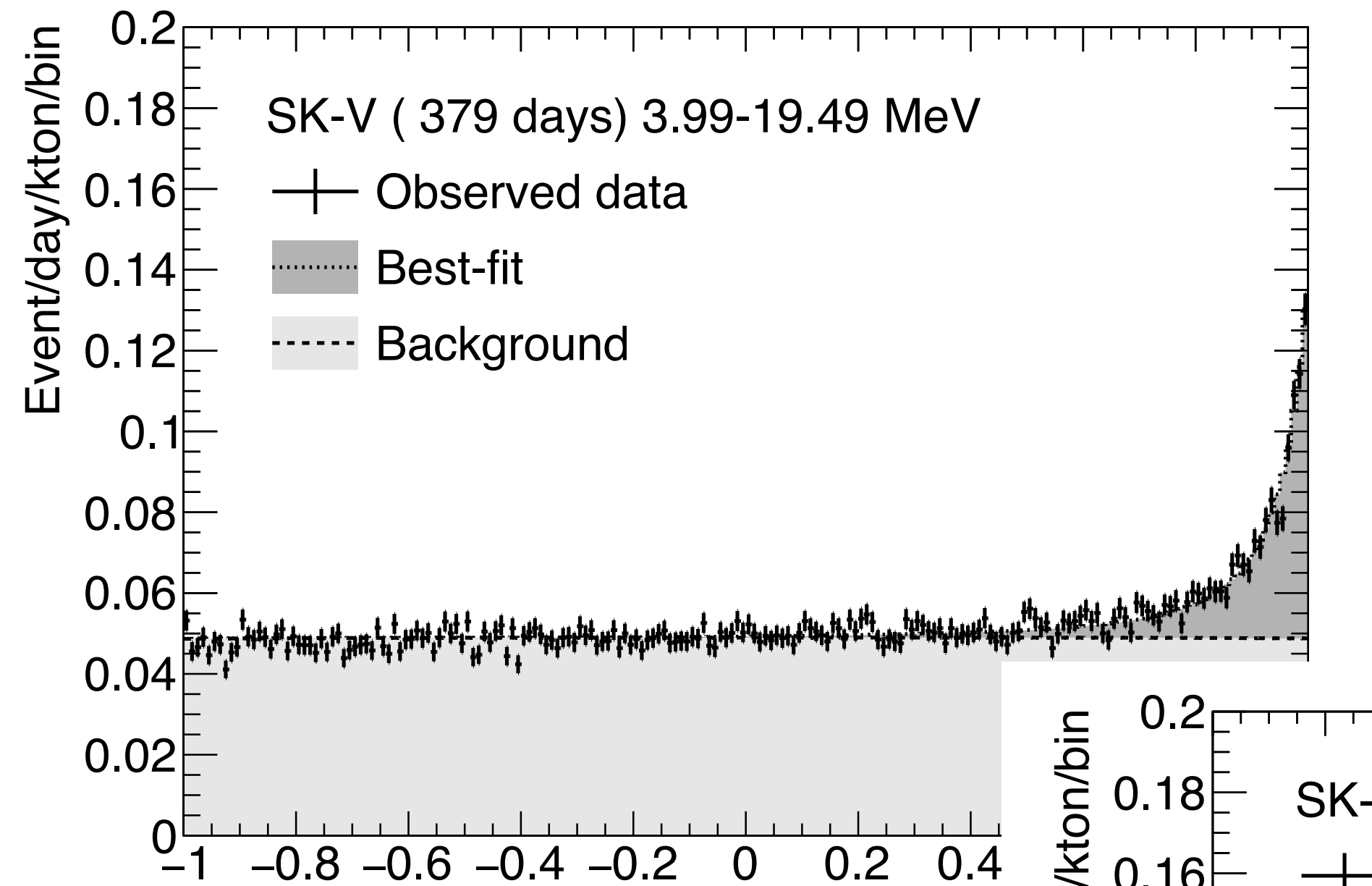
- Solar best-fit value updated to:

$$\Delta m_{21}^2 = 6.10^{+0.95}_{-0.81} \times 10^{-5} \text{eV}^2$$

- $\sim 1.5 \sigma$  away from KamLAND

SK fit, fixed  $\theta_{13}$

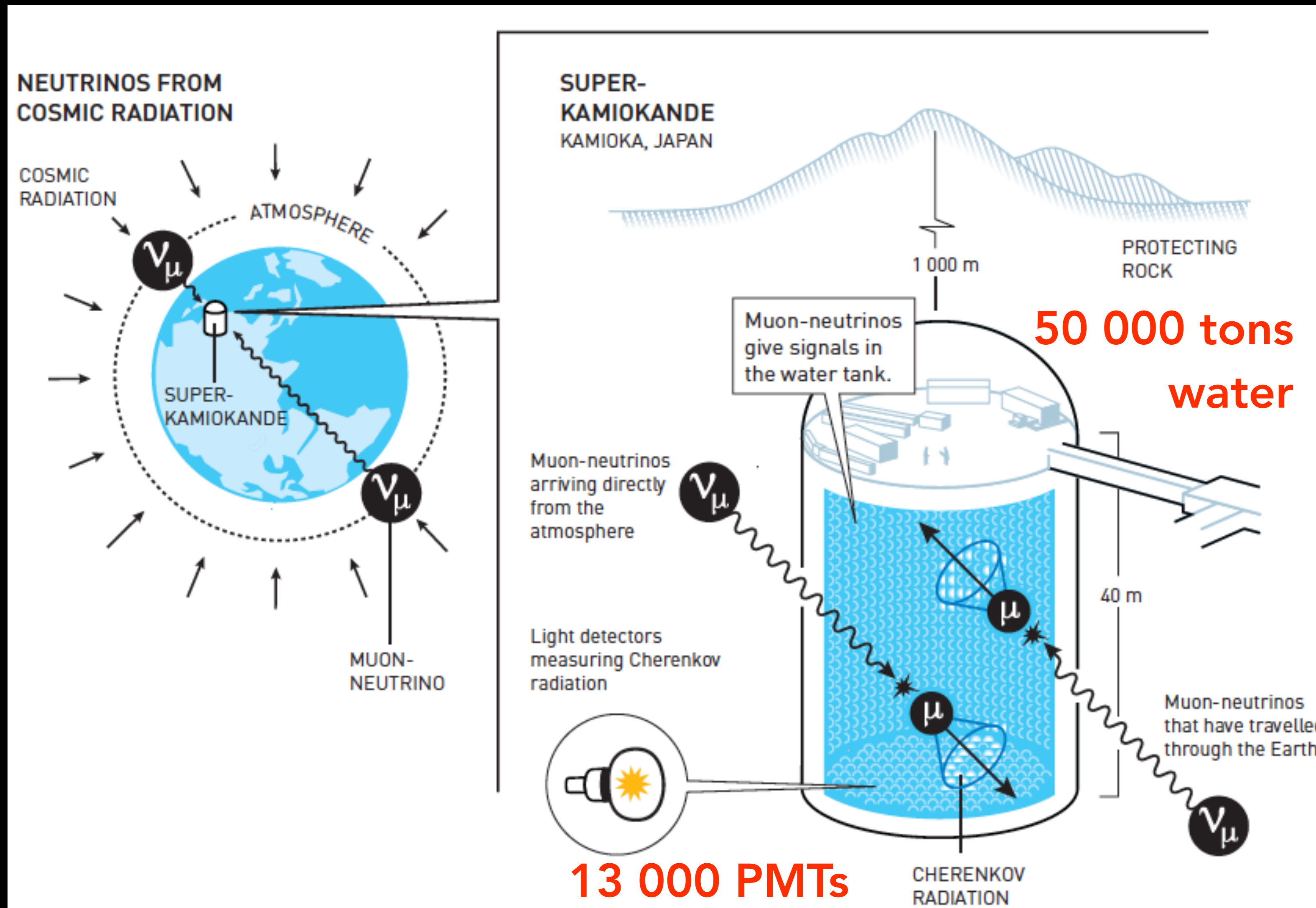
# NEW PHASES CONTINUE...



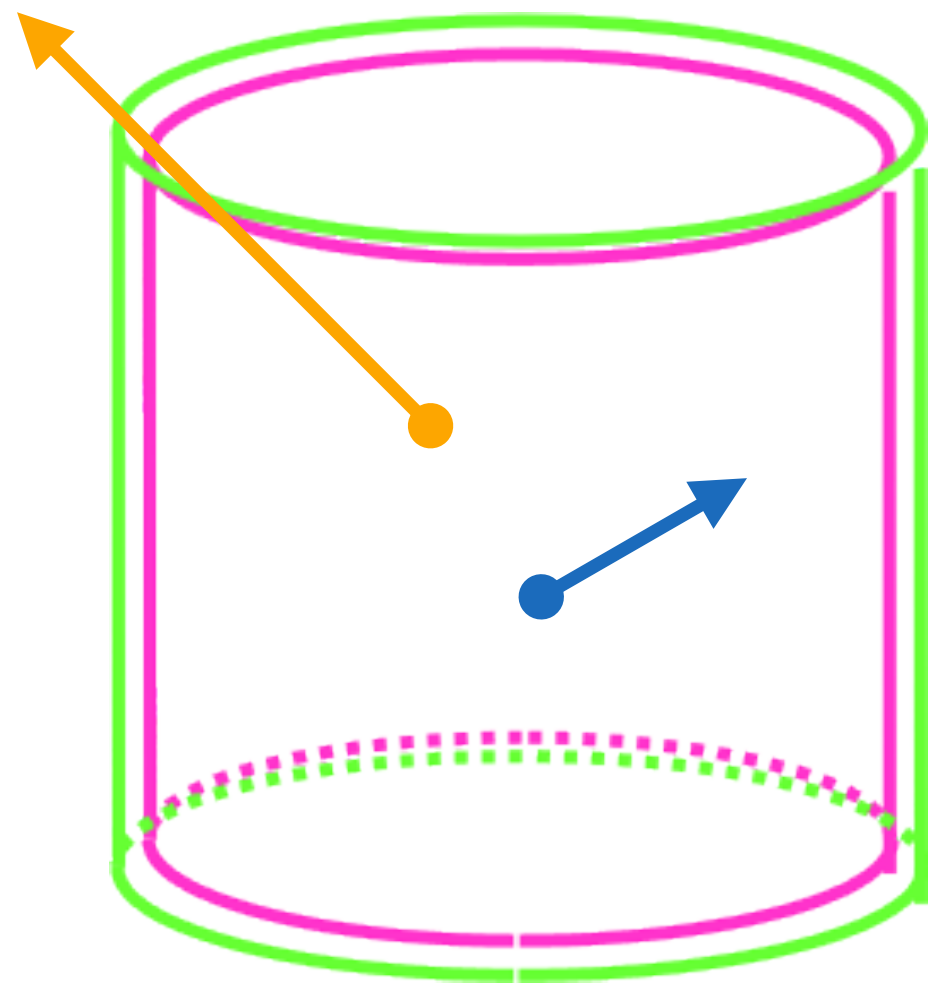
Higher backgrounds as expected, but 4 / 4.5 MeV threshold is clearly possible !

**SUPER-KAMIOKANDE  
ATMOSPHERIC**

# SK ATMOSPHERIC NEUTRINOS

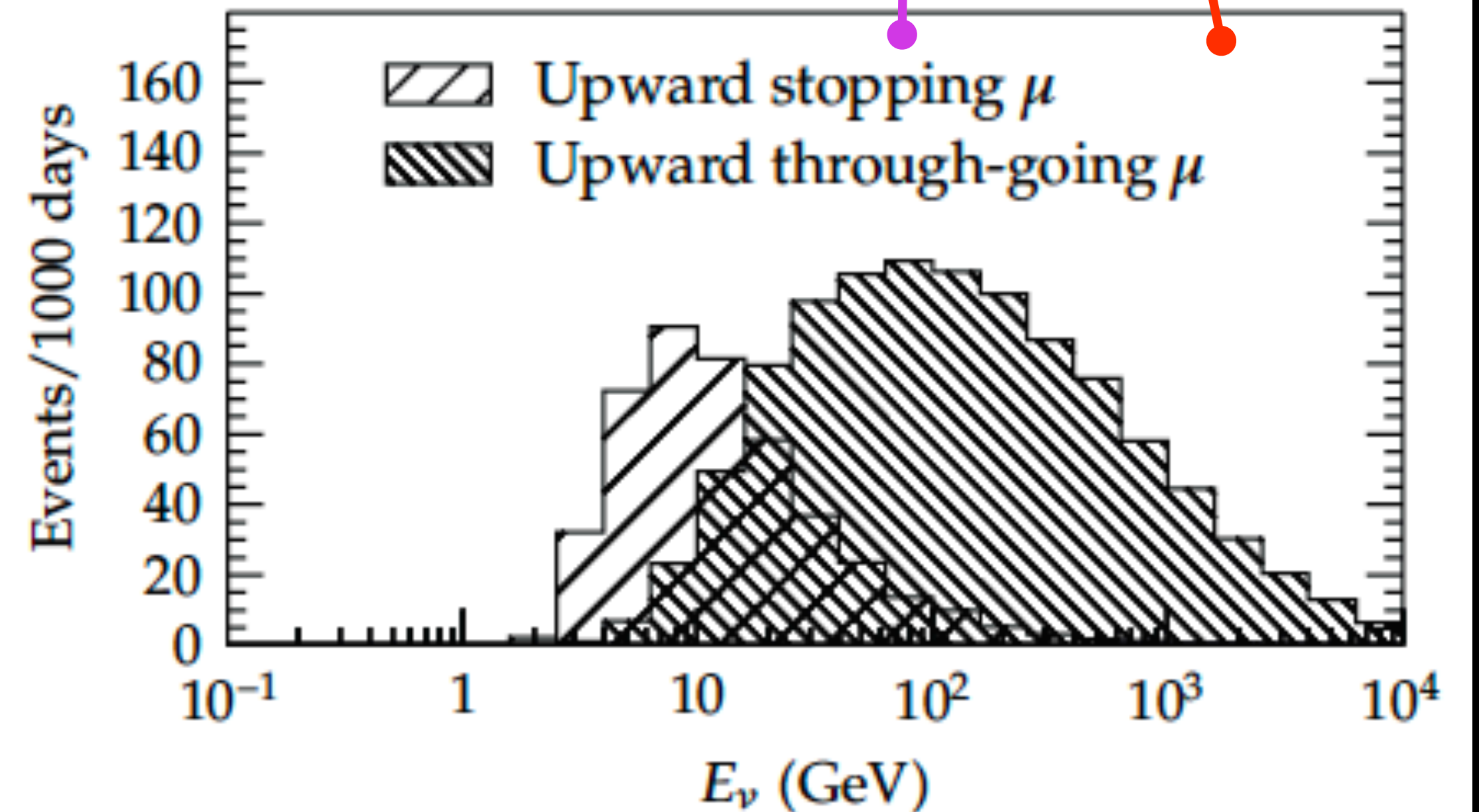
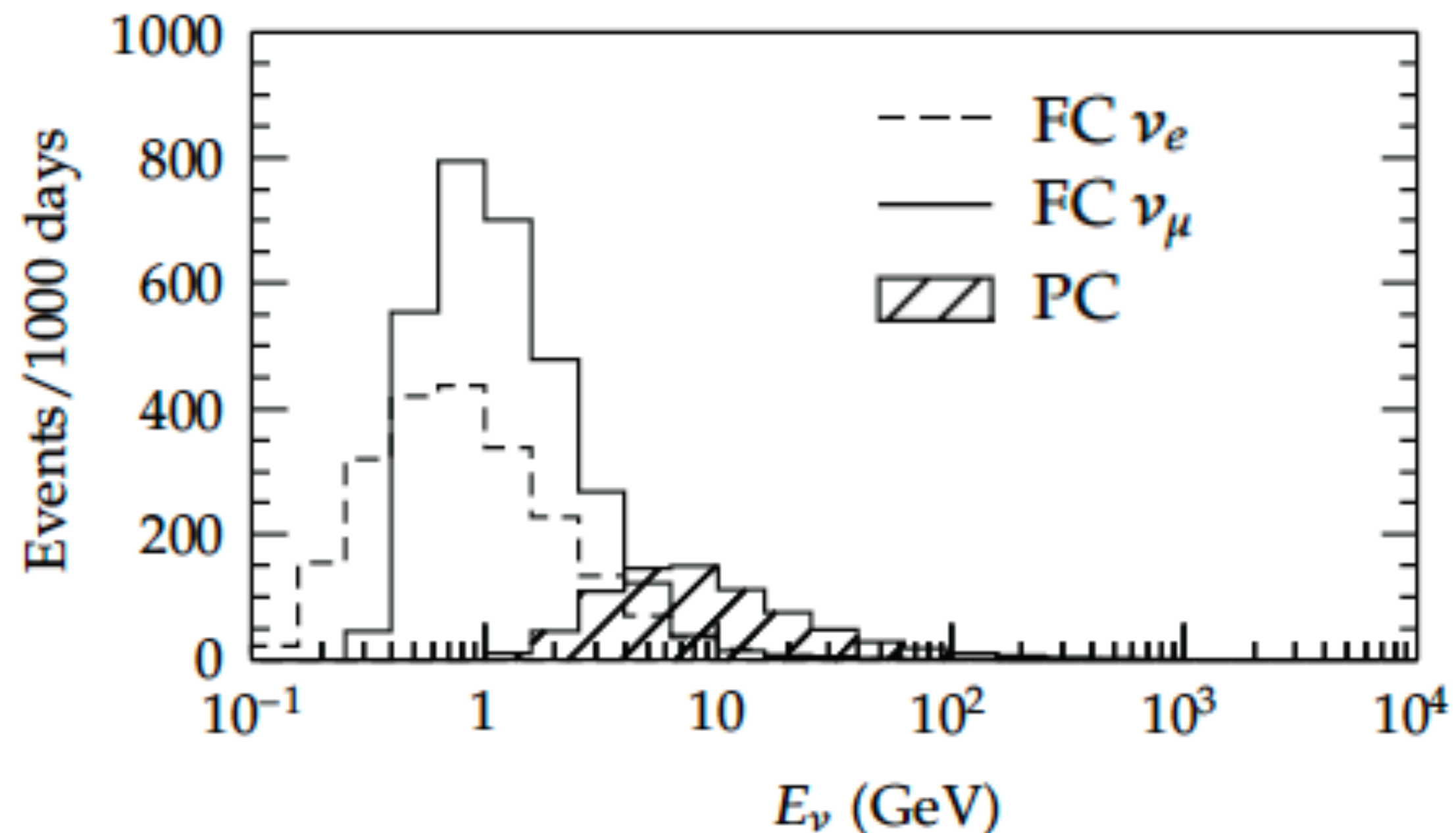
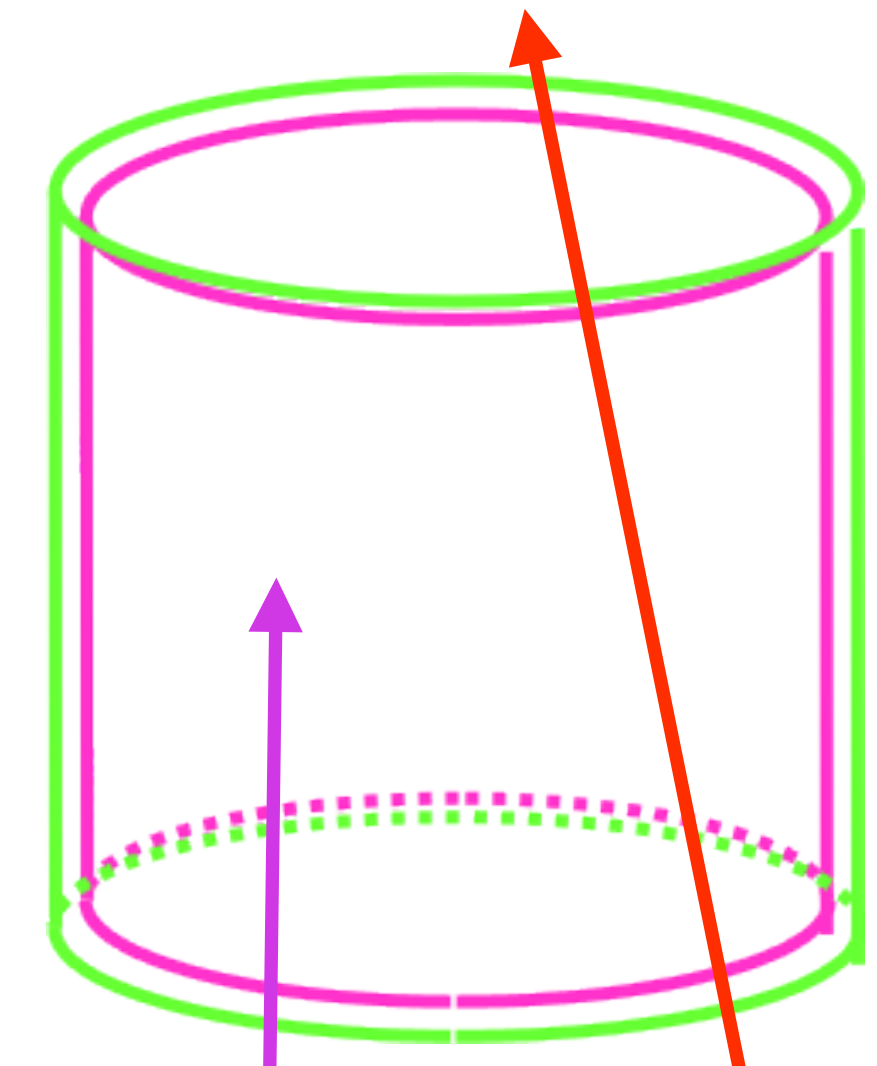


# SK - TYPES OF EVENTS



Range in detector strongly correlated to energy

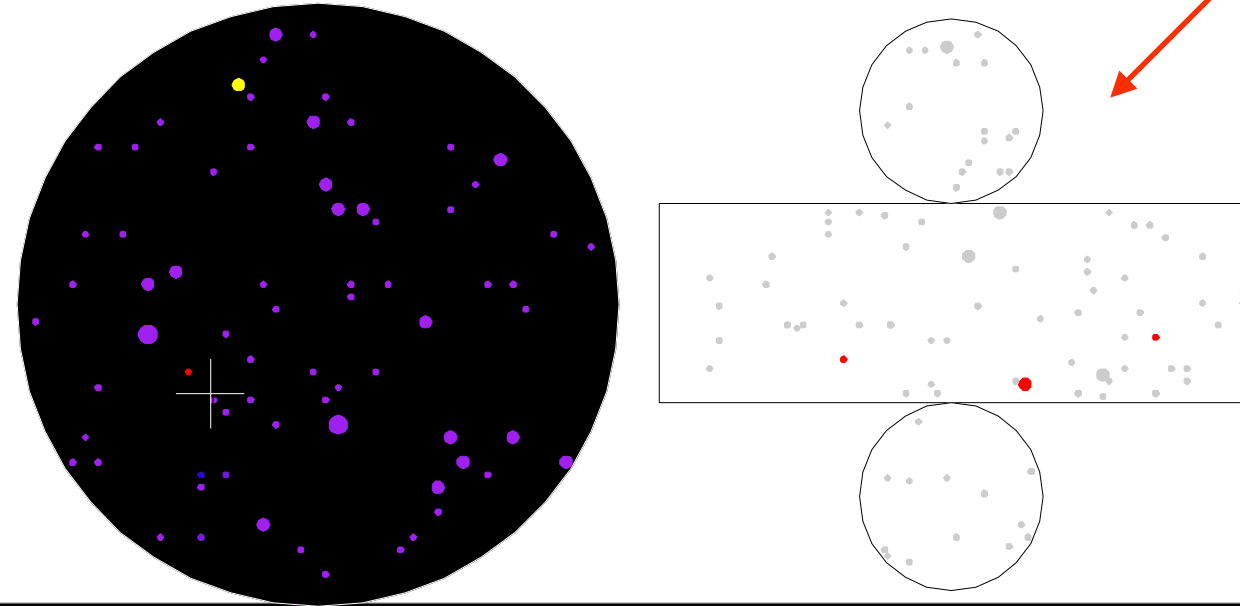
- Fully Contained
- Partially Contained
- Upward stopping  $\mu$
- Upward through/going  $\mu$



no signal in outer detector

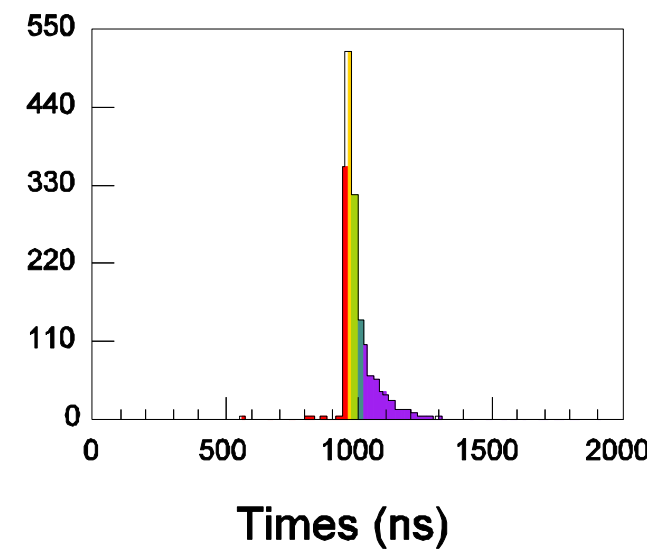
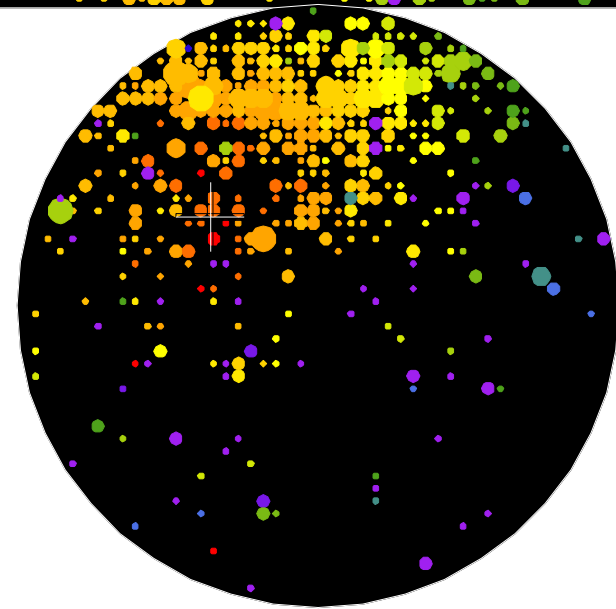
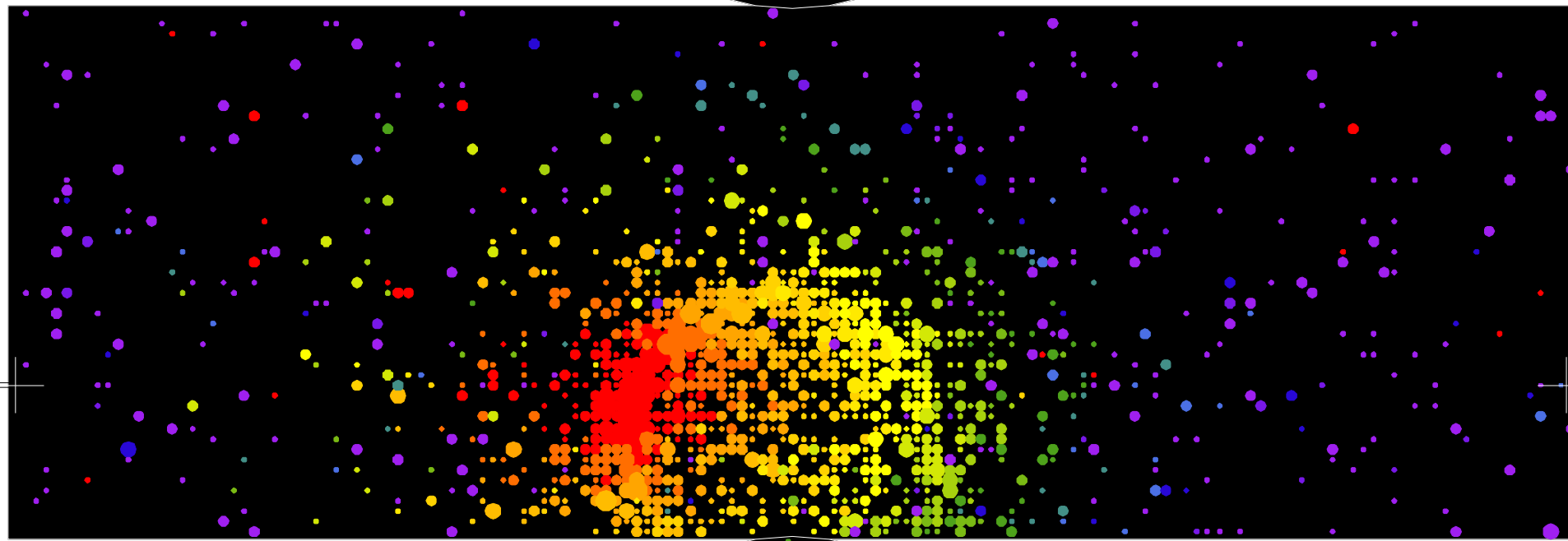
## Super-Kamiokande

Run 3013 Event 149004  
96-10-24:19:39:51  
Inner: 1763 hits, 4003 pE  
Outer: 3 hits, 5 pE (in-time)  
Trigger ID: 0x03  
D wall: 897.4 cm  
FC e-like,  $p = 463.8 \text{ MeV}/c$



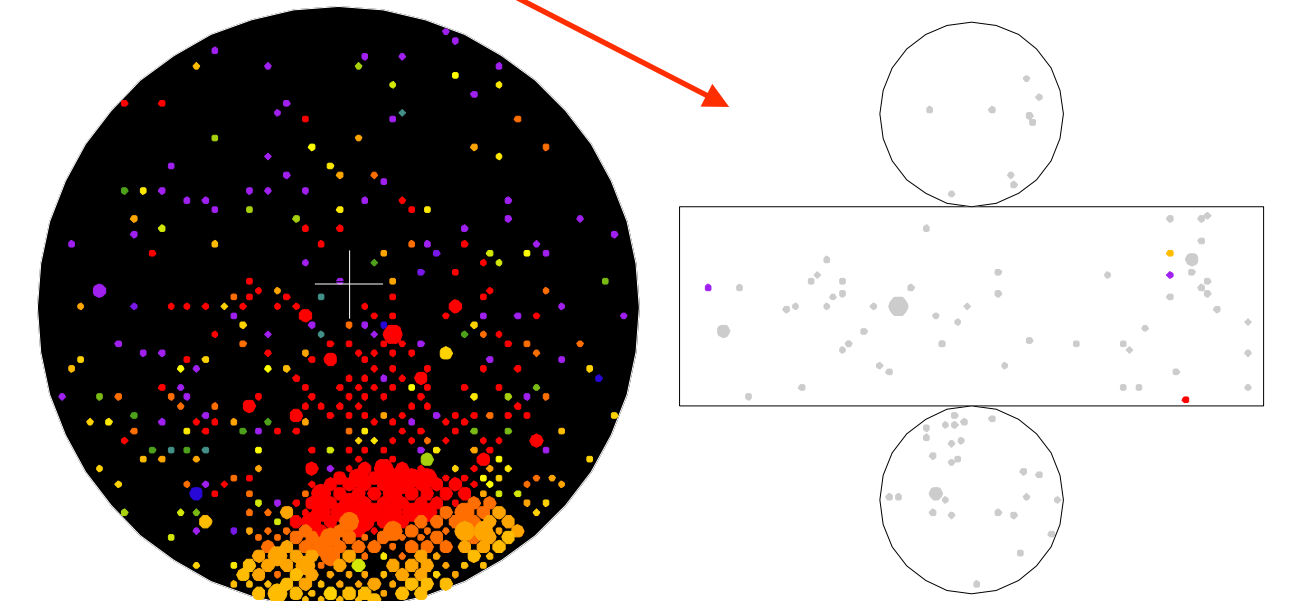
Time (ns)

- < 958
- 958- 963
- 963- 968
- 968- 973
- 973- 978
- 978- 983
- 983- 988
- 988- 993
- 993- 998
- 998-1003
- 1003-1008
- 1008-1013
- 1013-1018
- 1018-1023
- 1023-1028
- >1028



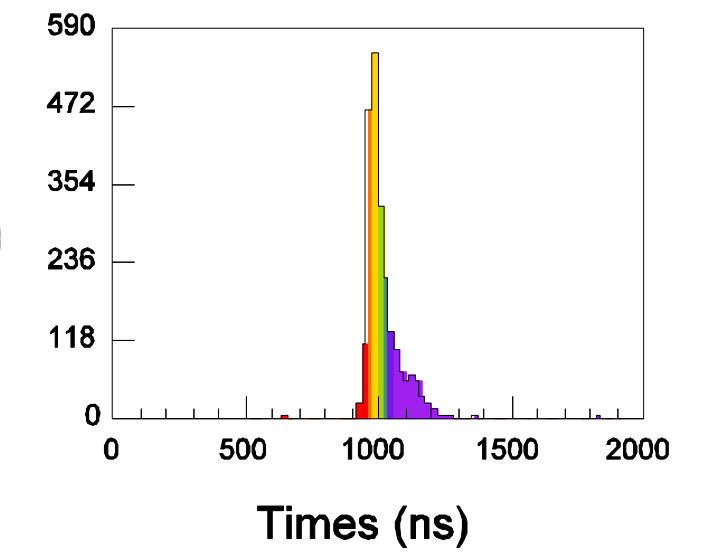
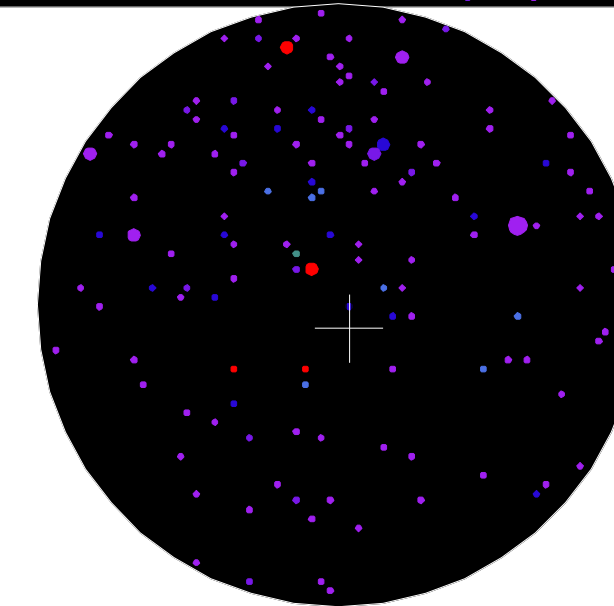
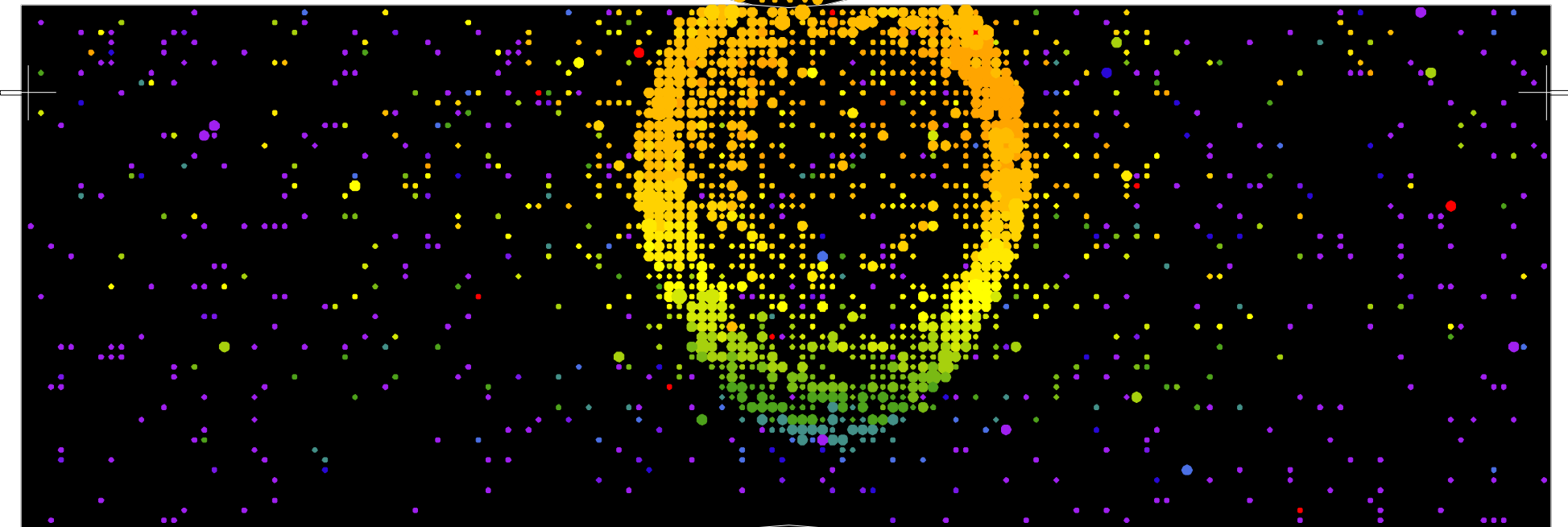
## Super-Kamiokande

Run 3062 Event 475360  
96-11-08:12:07:30  
Inner: 2305 hits, 7763 pE  
Outer: 5 hits, 4 pE (in-time)  
Trigger ID: 0x03  
D wall: 601.2 cm  
FC mu-like,  $p = 1088.0 \text{ MeV}/c$



Time (ns)

- < 971
- 971- 977
- 977- 983
- 983- 989
- 989- 995
- 995-1001
- 1001-1007
- 1007-1013
- 1013-1019
- 1019-1025
- 1025-1031
- 1031-1037
- 1037-1043
- 1043-1049
- 1049-1055
- >1055



electron-like

muon-like

# PARTIALLY CONTAINED

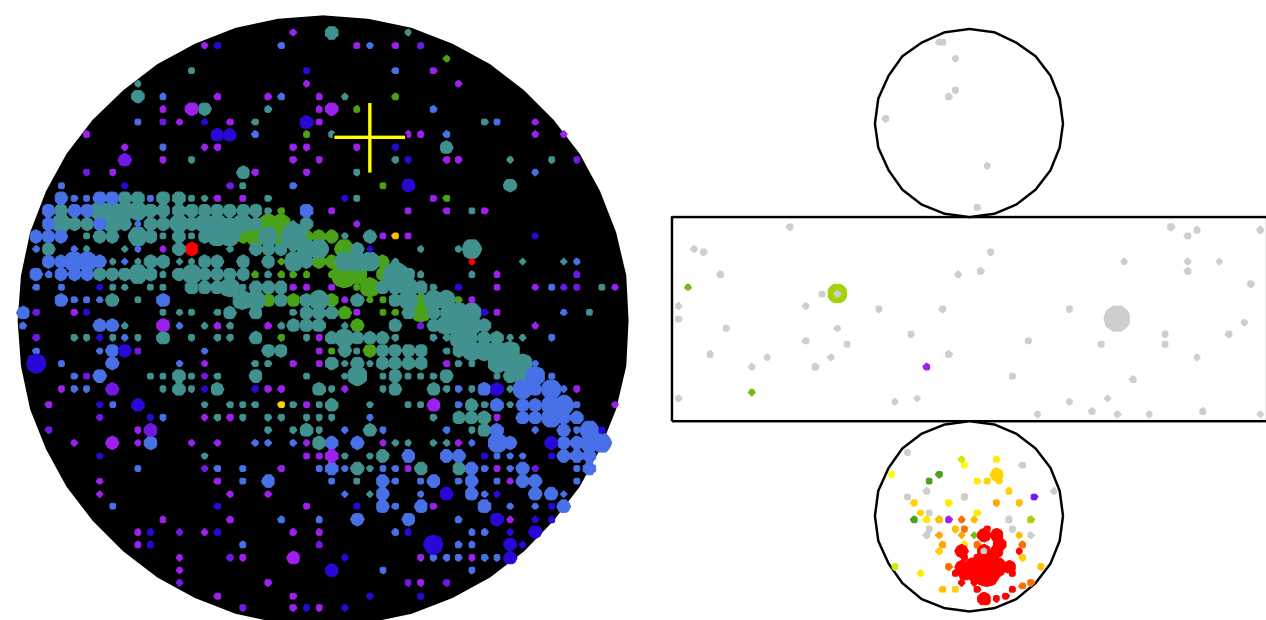


one cluster in outer detector

two clusters in outer detector

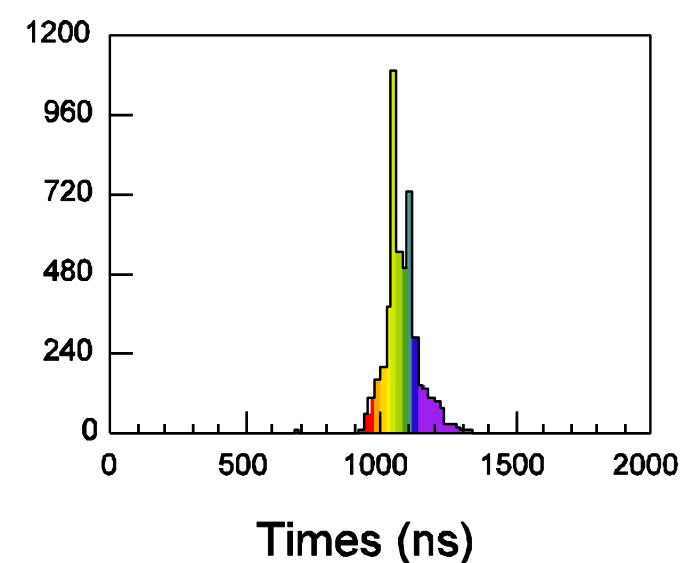
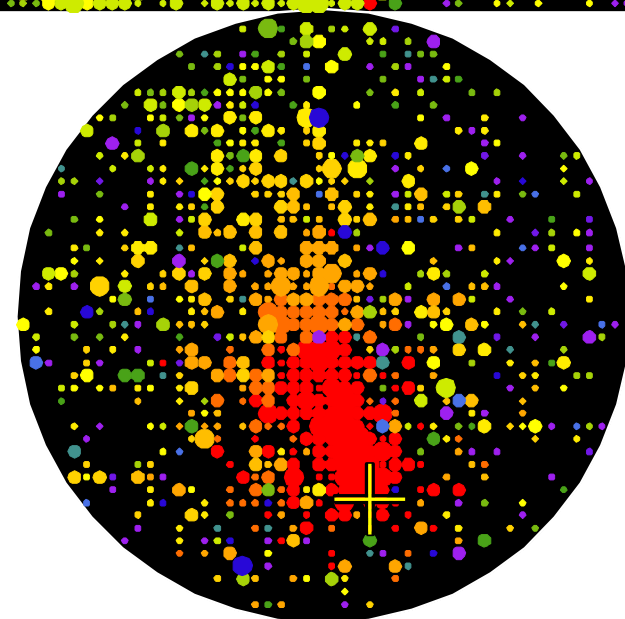
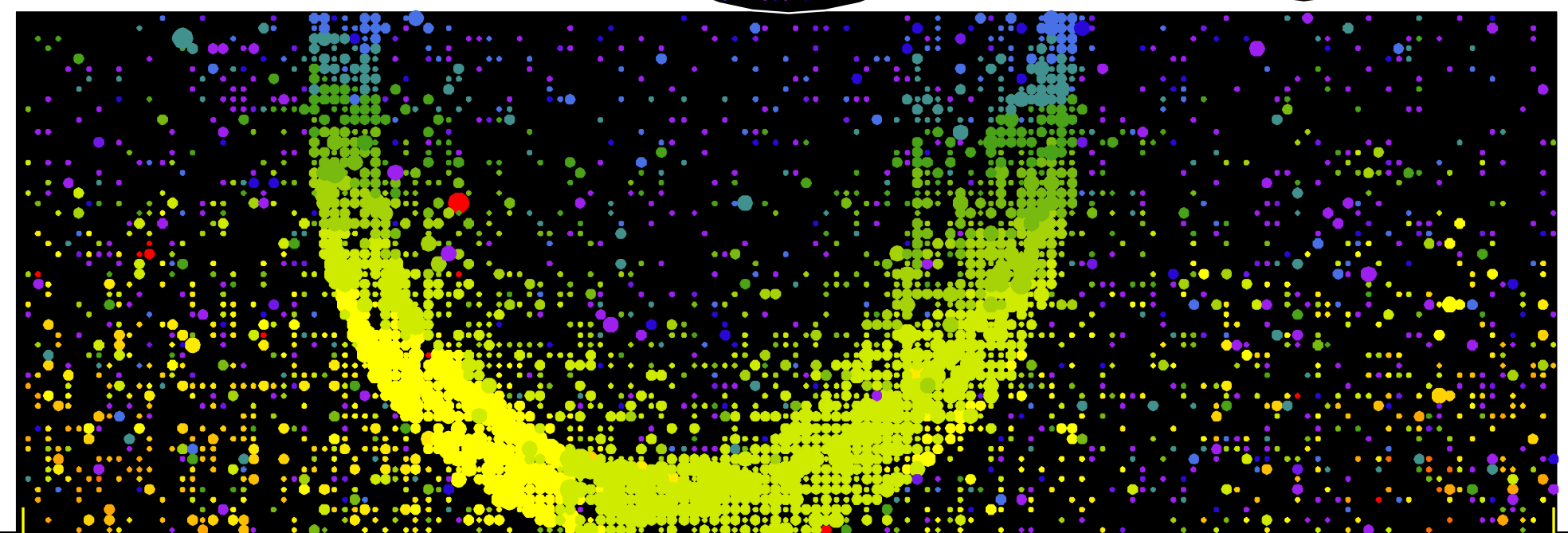
## Super-Kamiokande

Run 8205 Event 3894074  
99-12-16:08:14:45  
Inner: 4771 hits, 15758 pE  
Outer: -1 hits, 0 pE (in-time)  
Trigger ID: 0x0f  
ap ve#:  
Fully-Contained



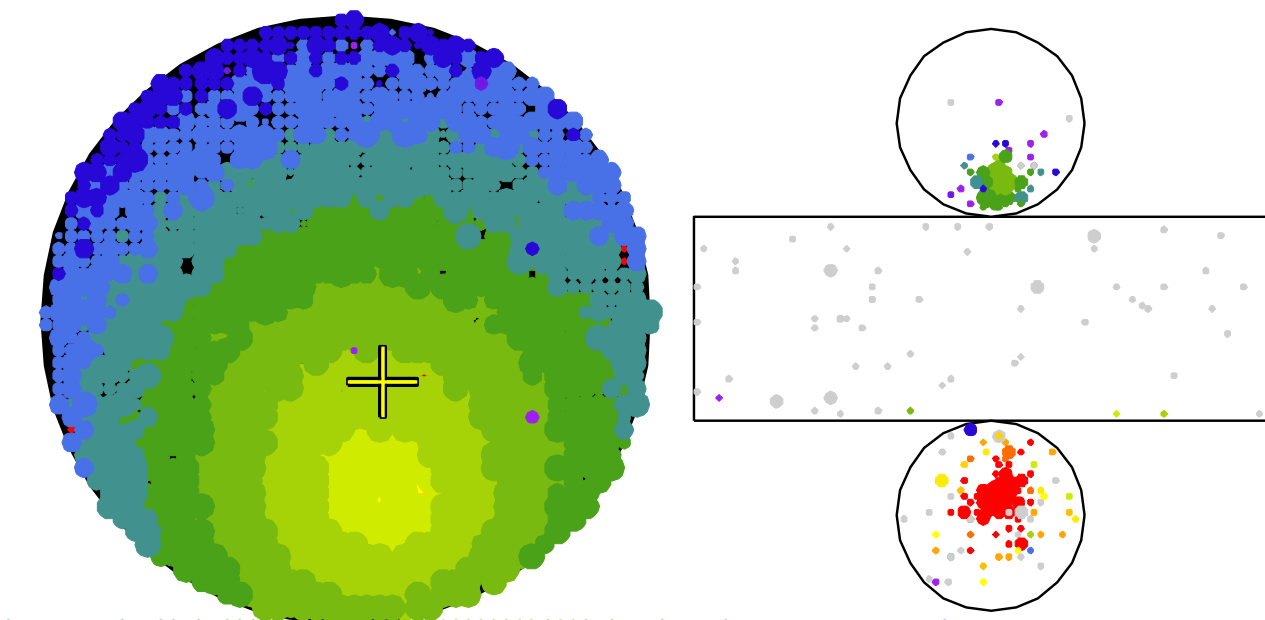
### Time(ns)

- < 982
- 982- 994
- 994-1006
- 1006-1018
- 1018-1030
- 1030-1042
- 1042-1054
- 1054-1066
- 1066-1078
- 1078-1090
- 1090-1102
- 1102-1114
- 1114-1126
- 1126-1138
- 1138-1150
- >1150



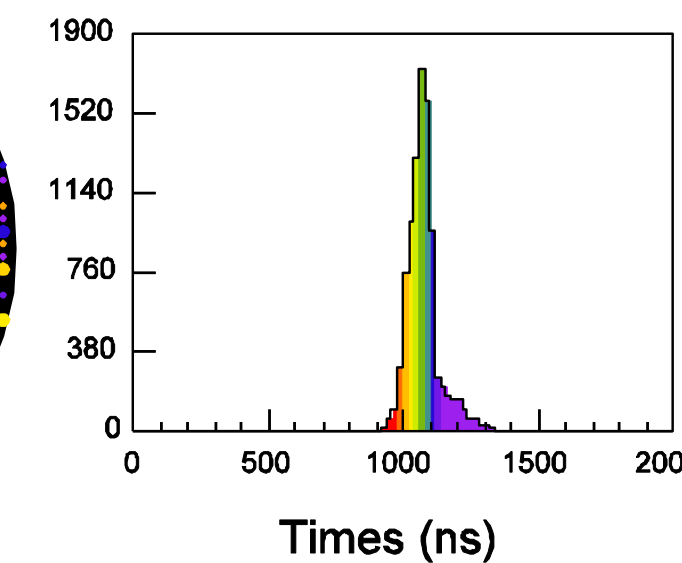
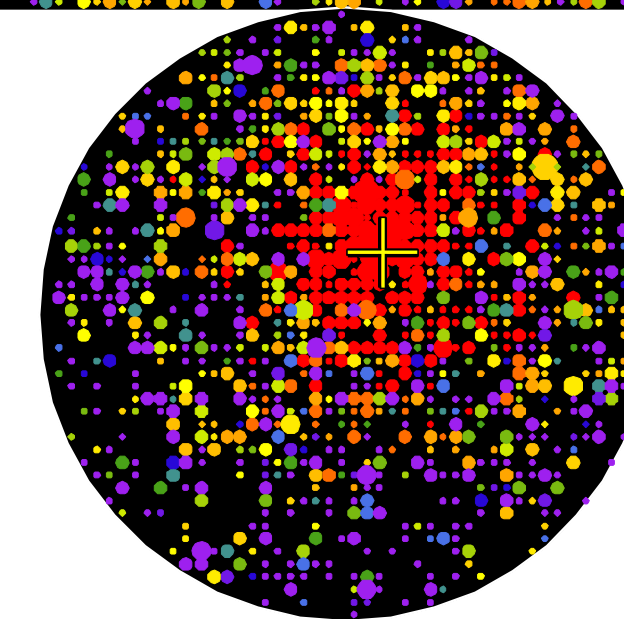
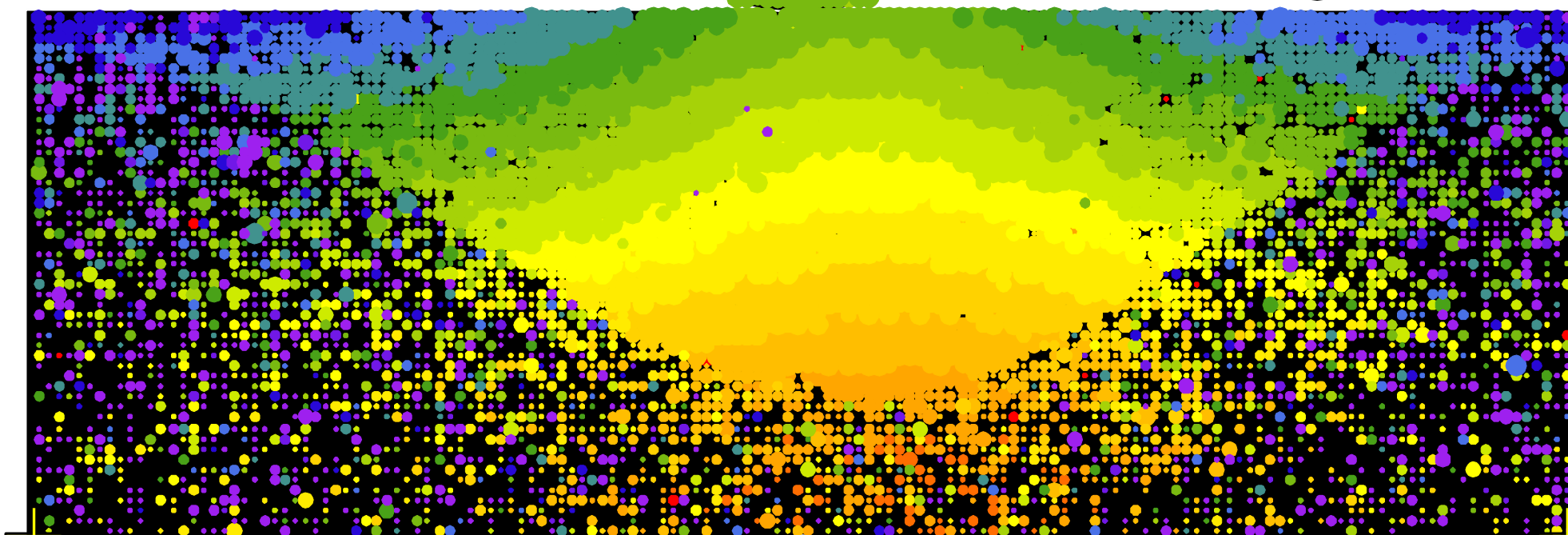
## Super-Kamiokande

Run 8060 Event 7678869  
99-10-29:14:09:48  
Inner: 9144 hits, 85718 pE  
Outer: -1 hits, 0 pE (in-time)  
Trigger ID: 0x0f  
ap ve#:  
Fully-Contained



### Time(ns)

- < 991
- 991-1001
- 1001-1011
- 1011-1021
- 1021-1031
- 1031-1041
- 1041-1051
- 1051-1061
- 1061-1071
- 1071-1081
- 1081-1091
- 1091-1101
- 1101-1111
- 1111-1121
- 1121-1131
- >1131

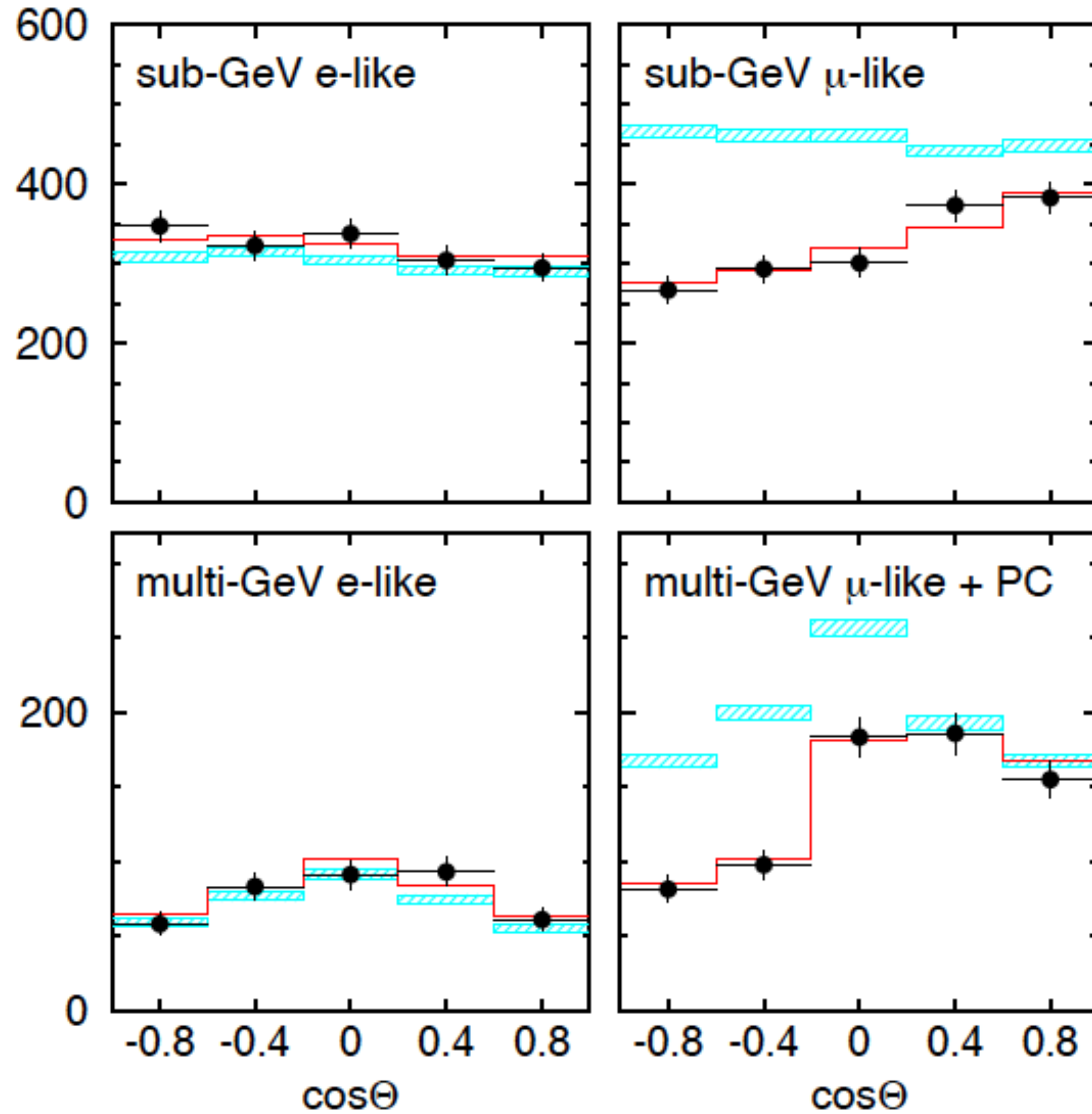


stopping muon

upward throughgoing muon



# THE “SMOKING GUN” PLOTS



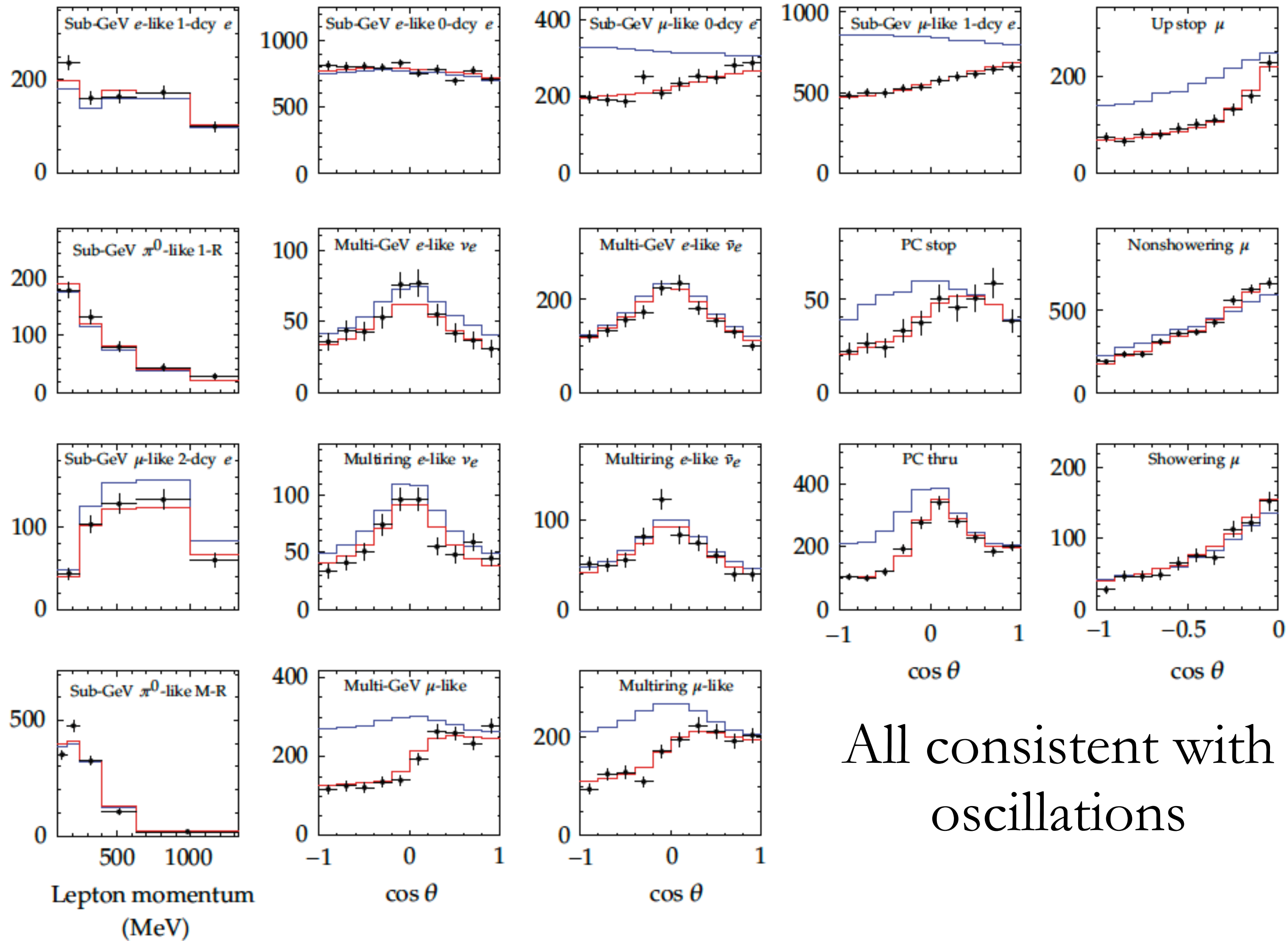
Expected, no oscillations

Fit to data, oscillations

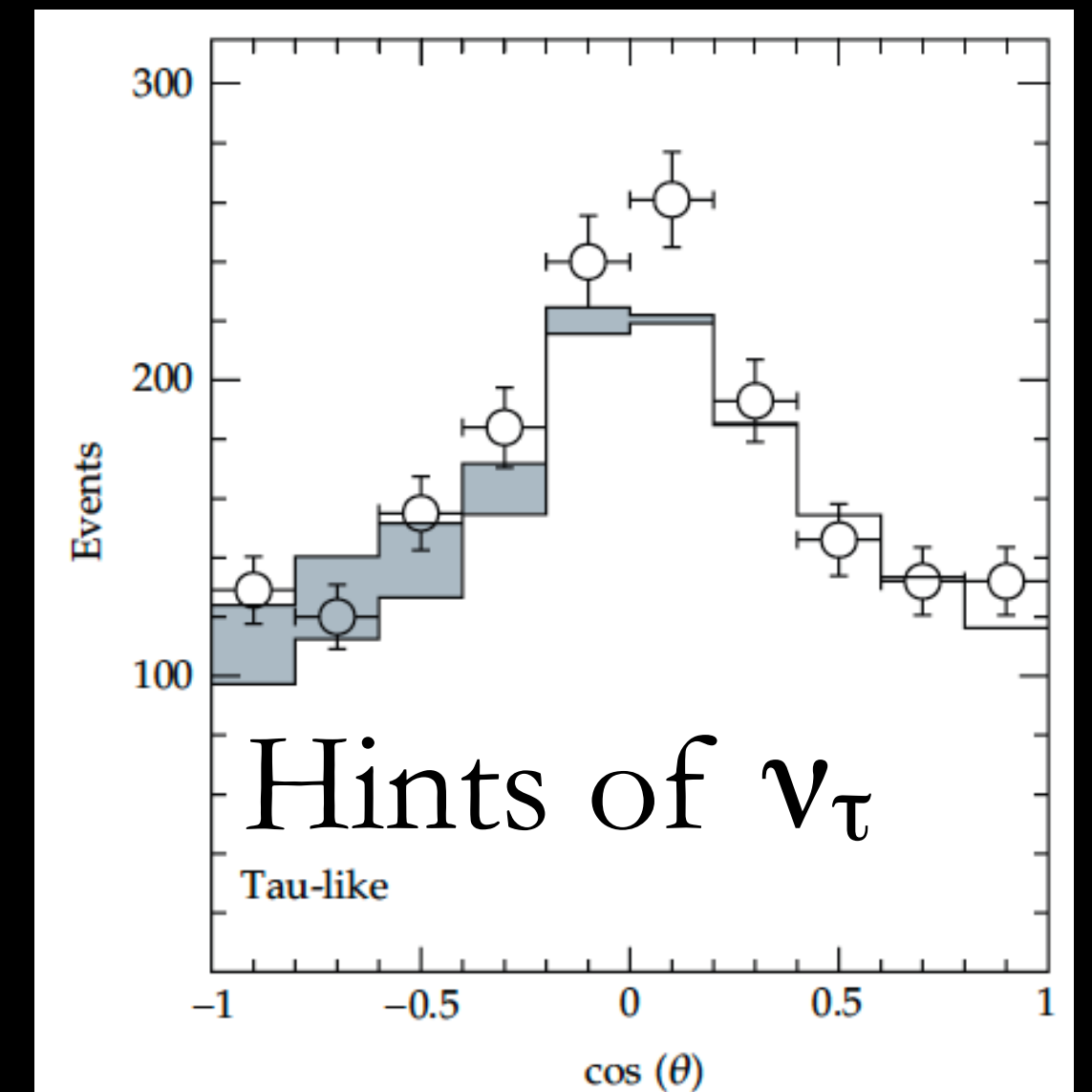
Neutrino “disappearance” depends on energy and direction (path length)

**Discovery of neutrino oscillations!**

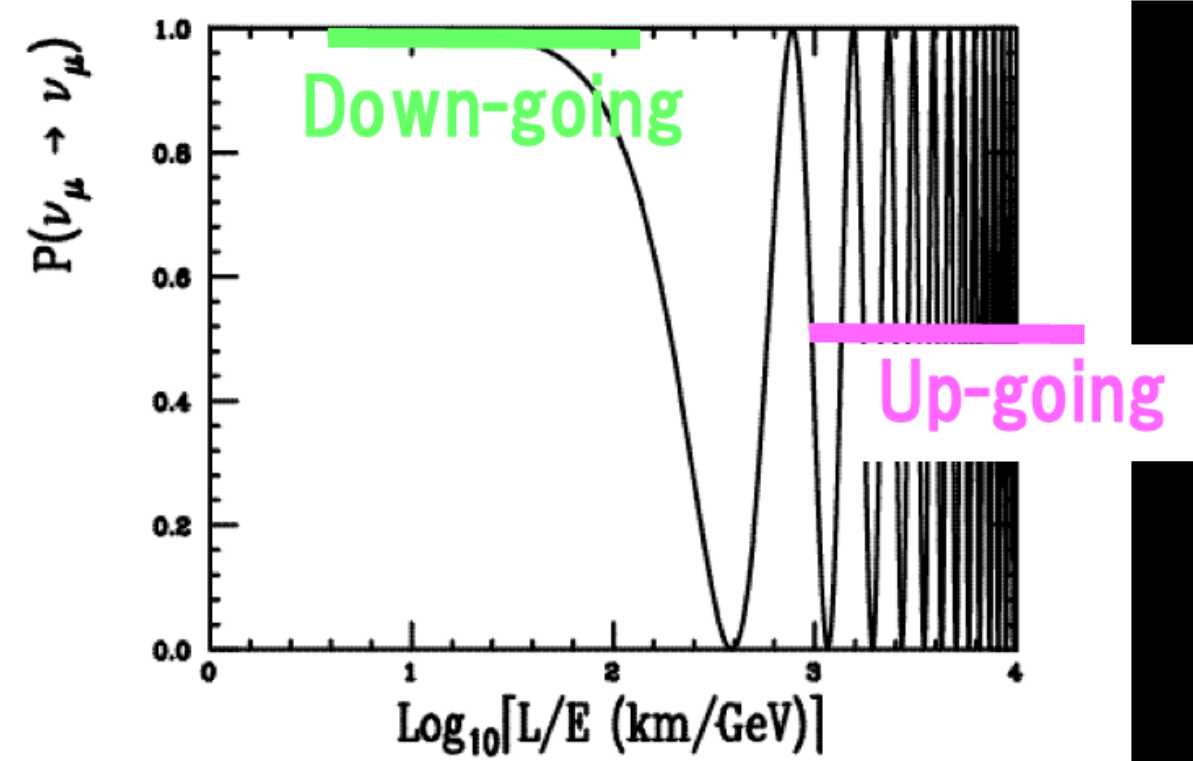
# A WEALTH OF DATA...



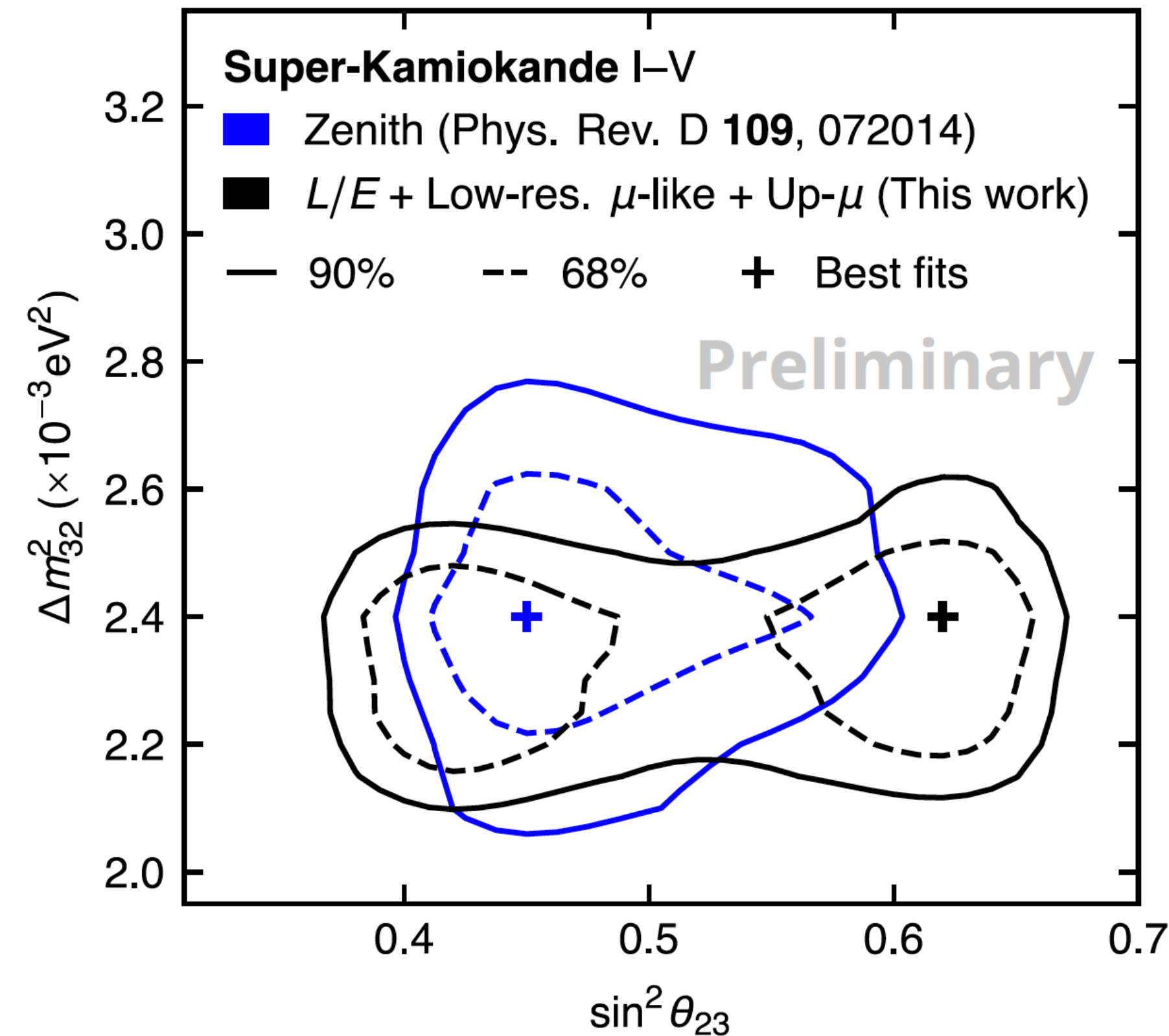
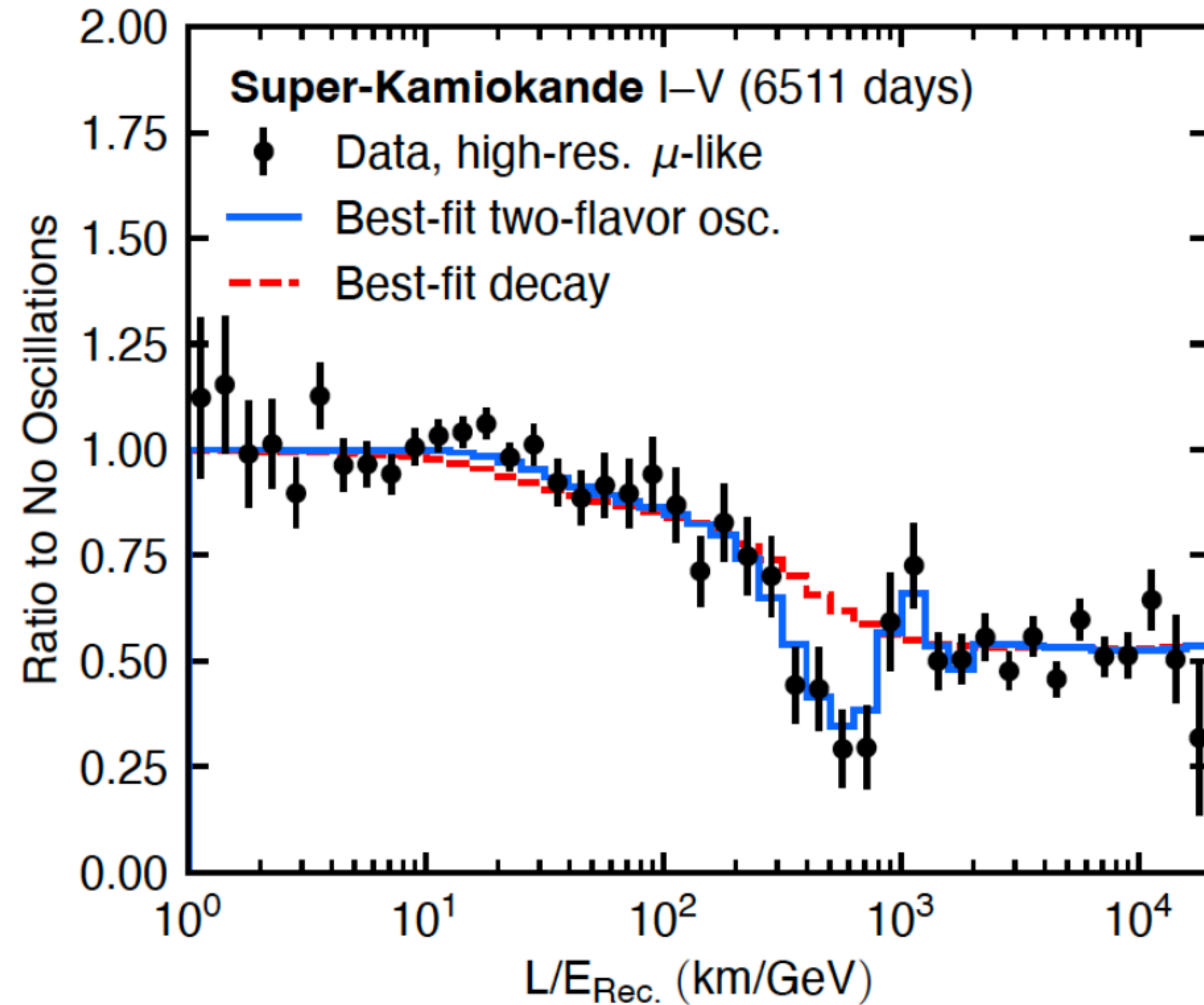
All consistent with oscillations



# LATEST RESULTS, NEUTRINO 2024

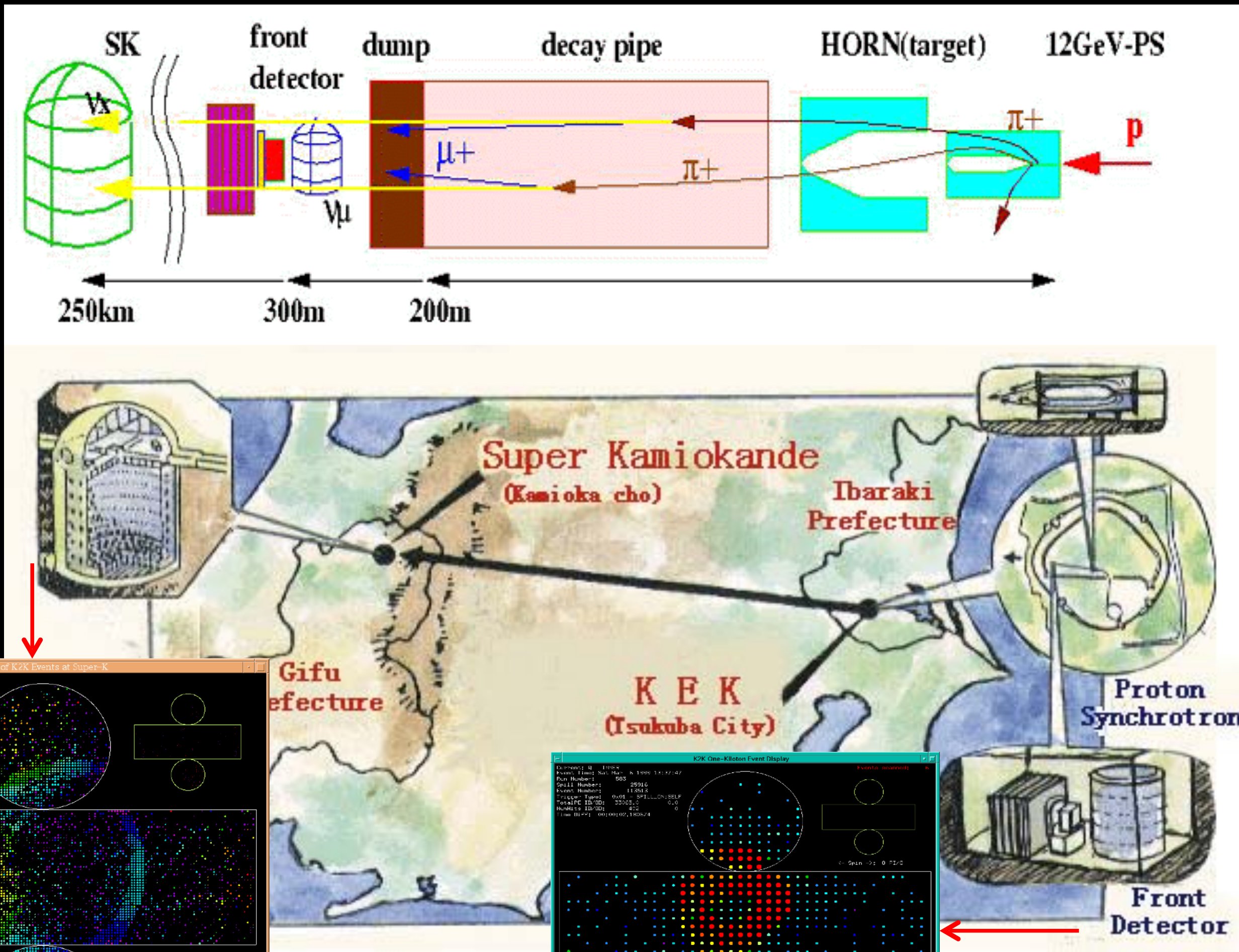


- $\Delta m^2$  much larger than for solar. Partly  $\nu_\mu \rightarrow \nu_\tau$ . Therefore these have to be different oscillations from what explains solar.

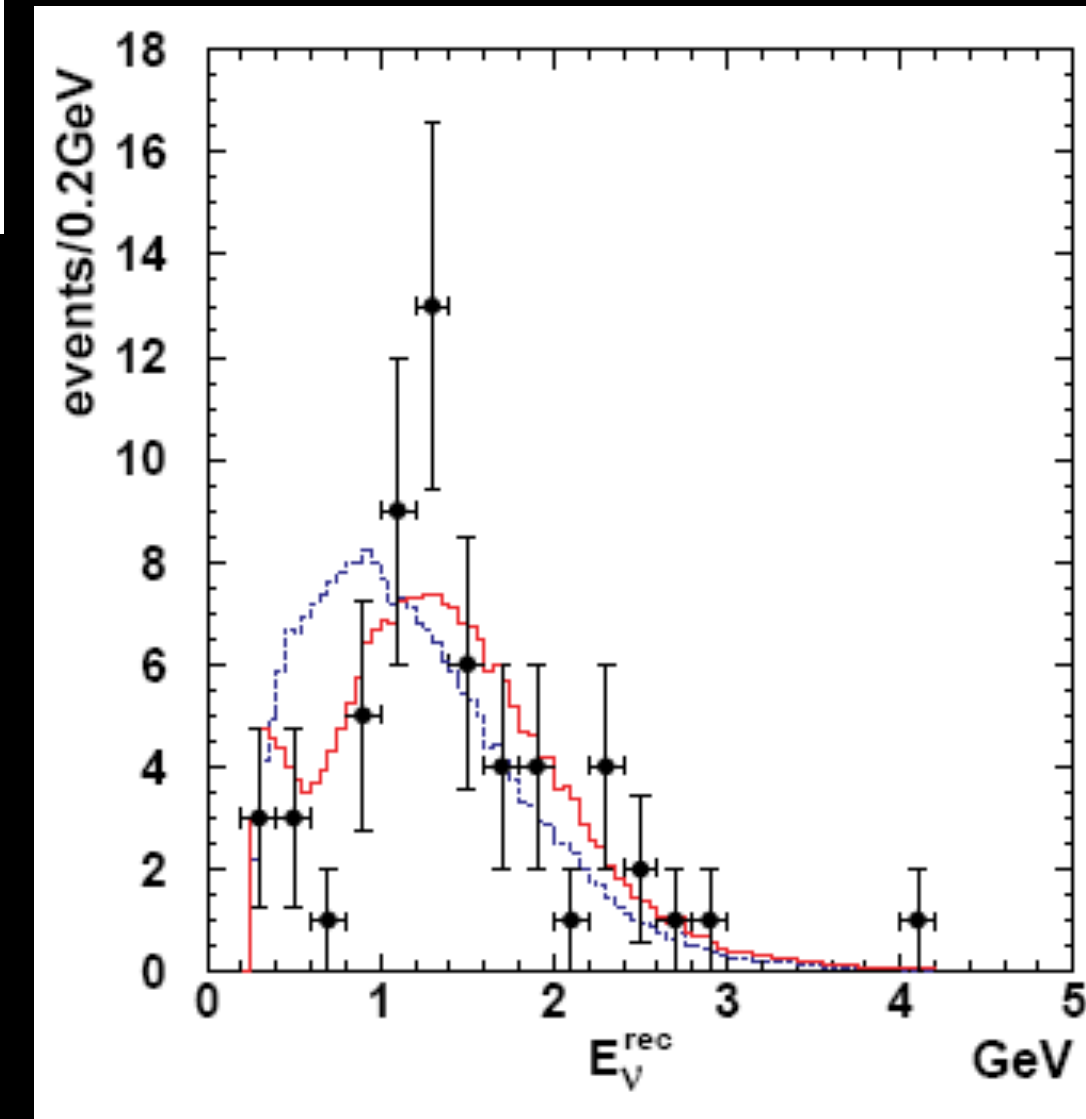


EARLY CONFIRMATION

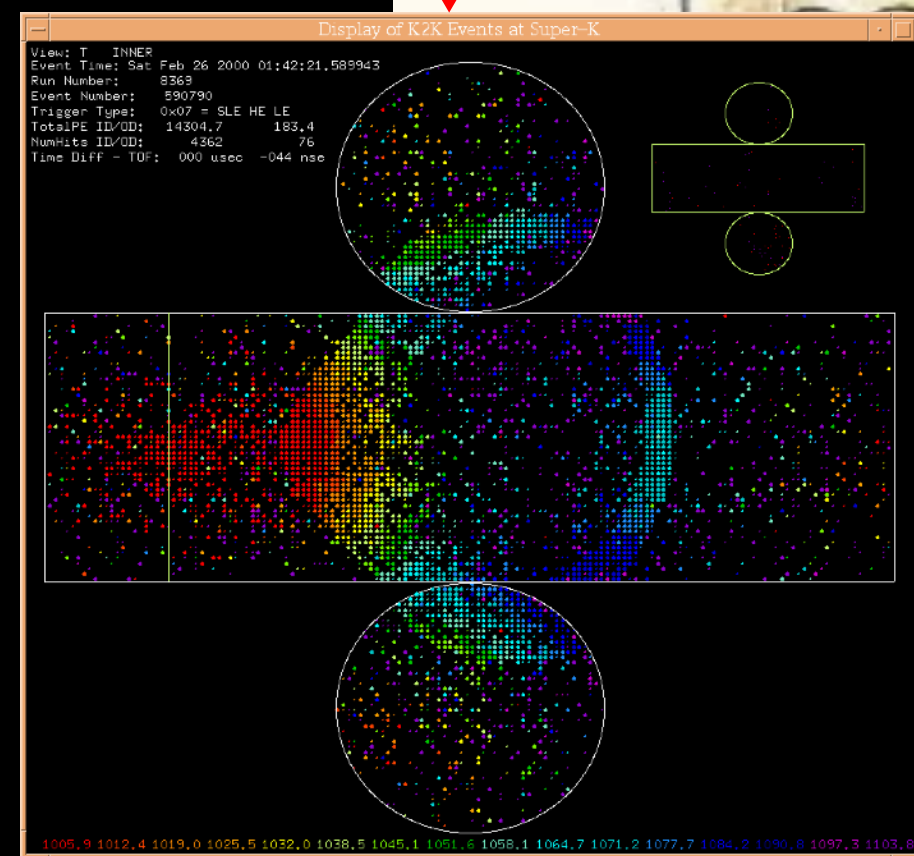
# K2K - FROM KEK TO KAMIOKA



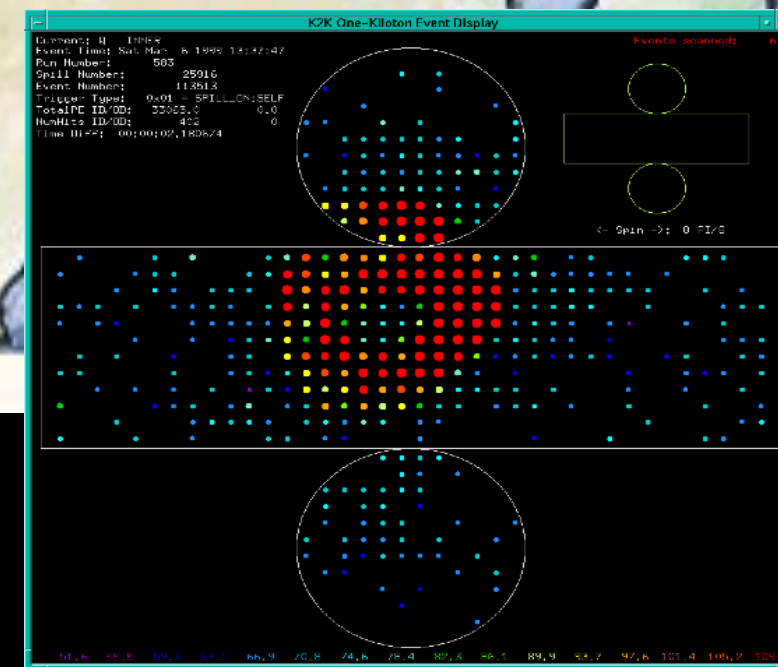
- First long baseline accelerator neutrino experiment!



Use ND data to predict non-oscillated FD spectrum

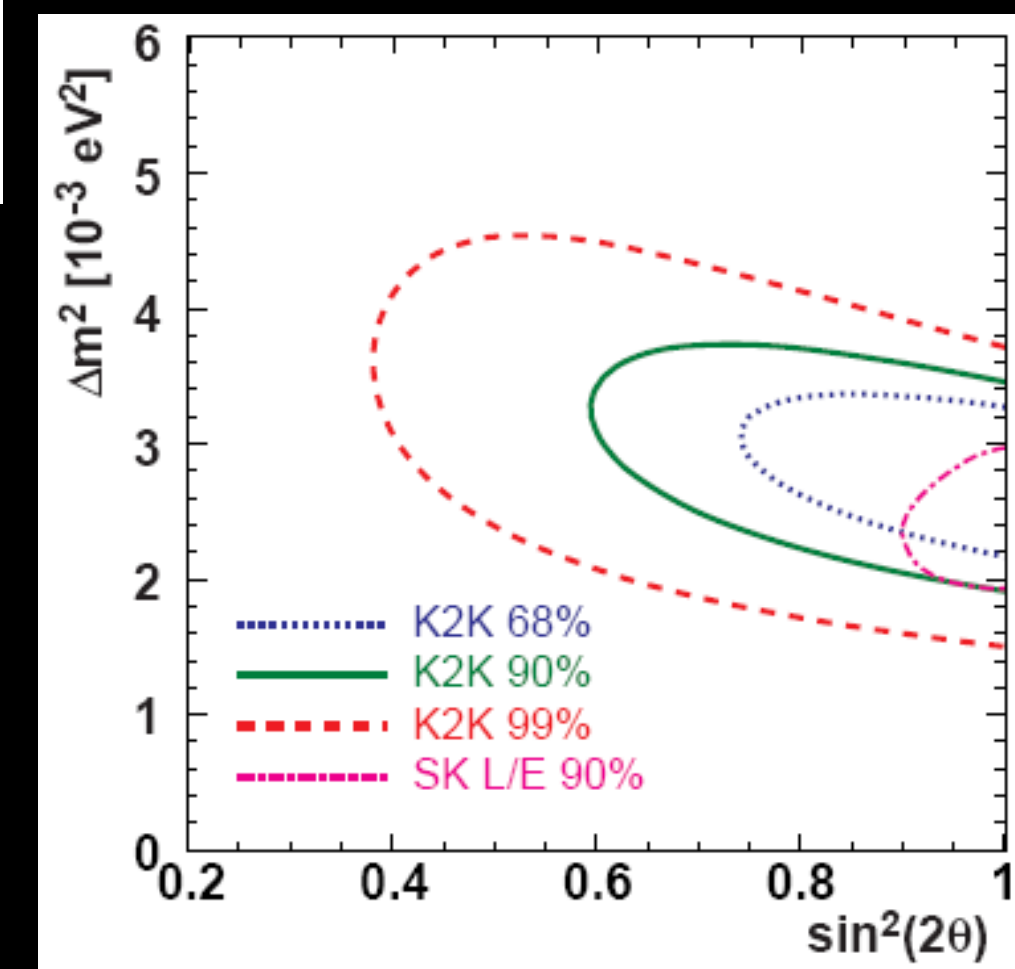


Far detector (FD) event



Near detector (ND) event

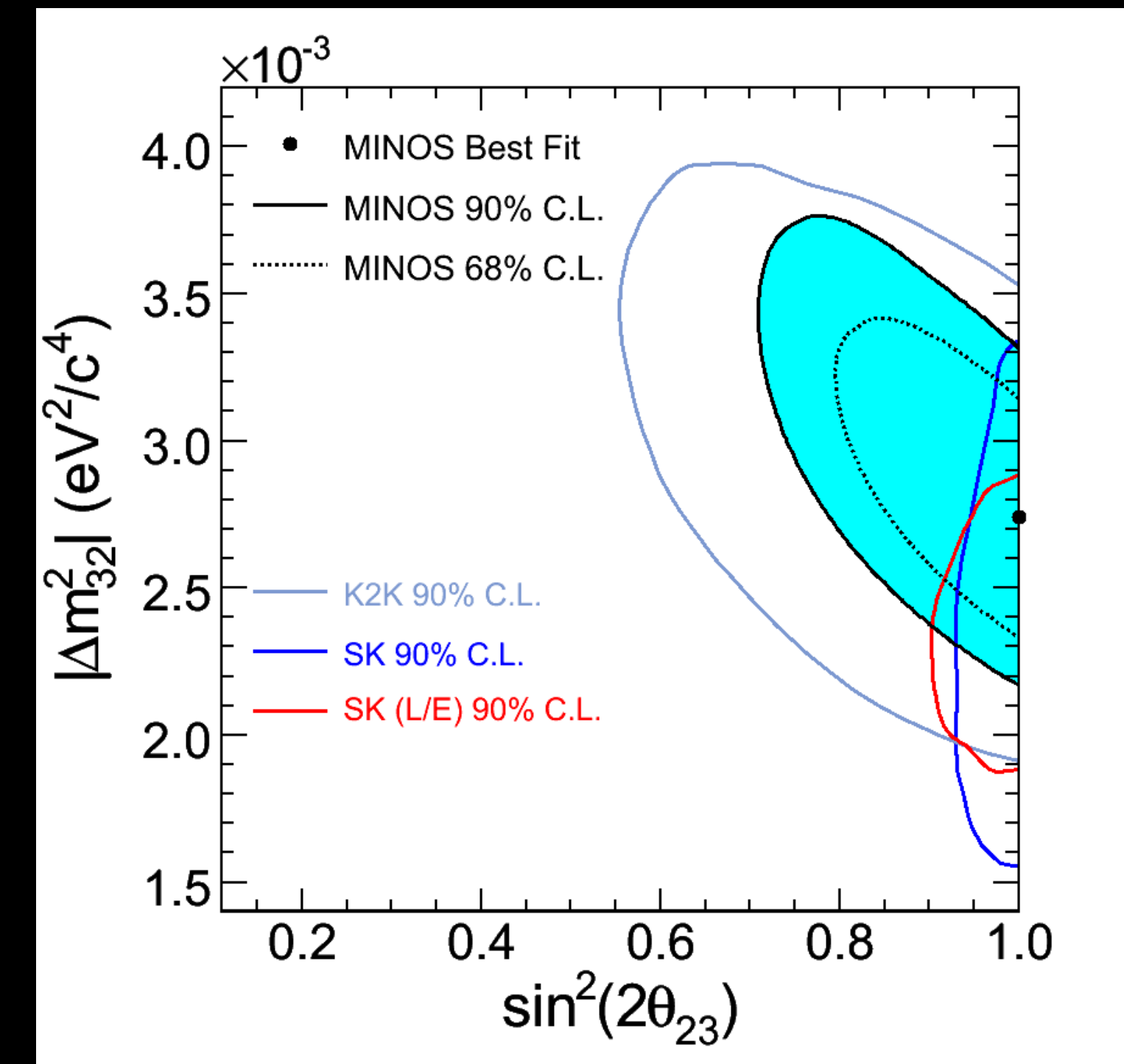
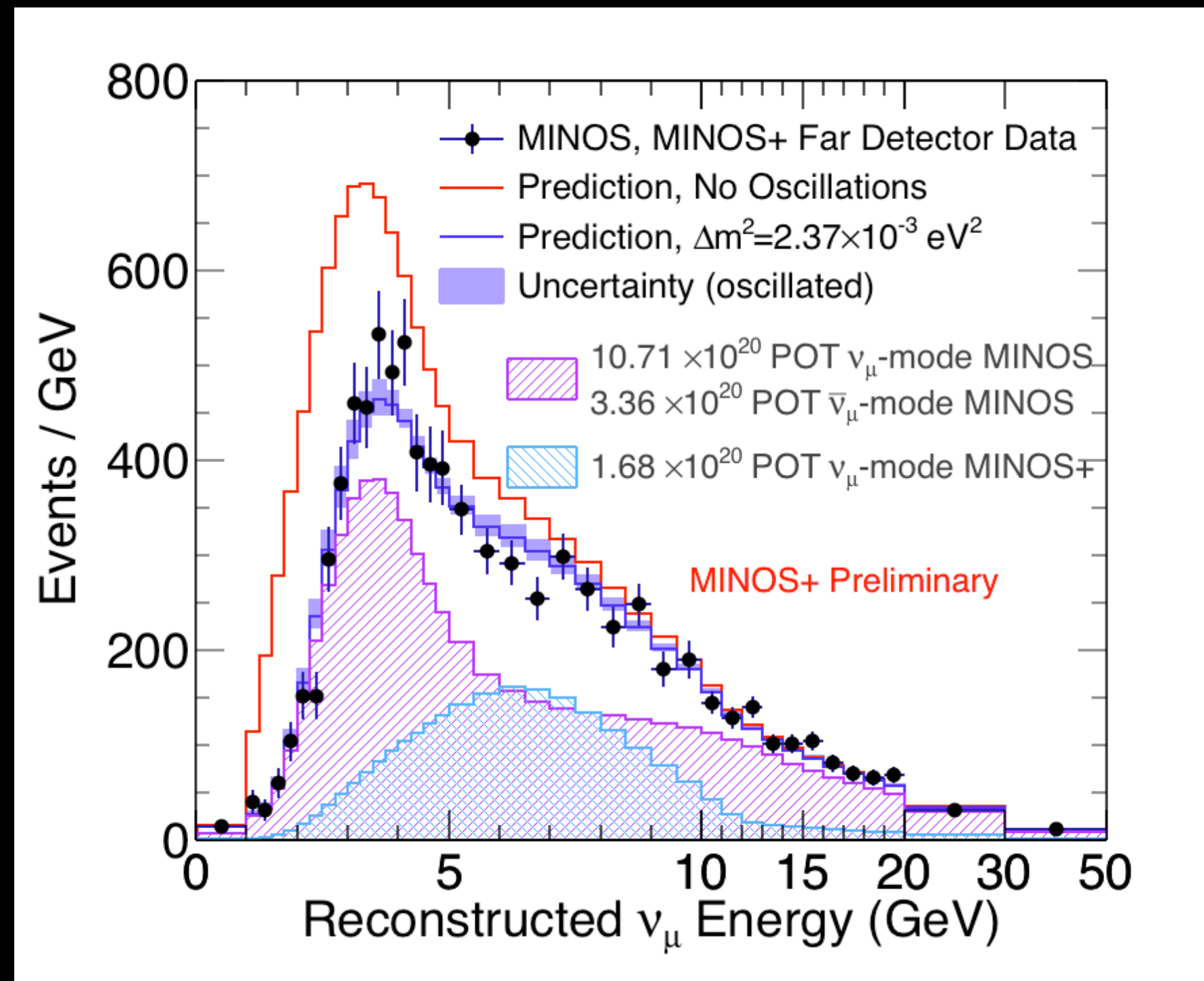
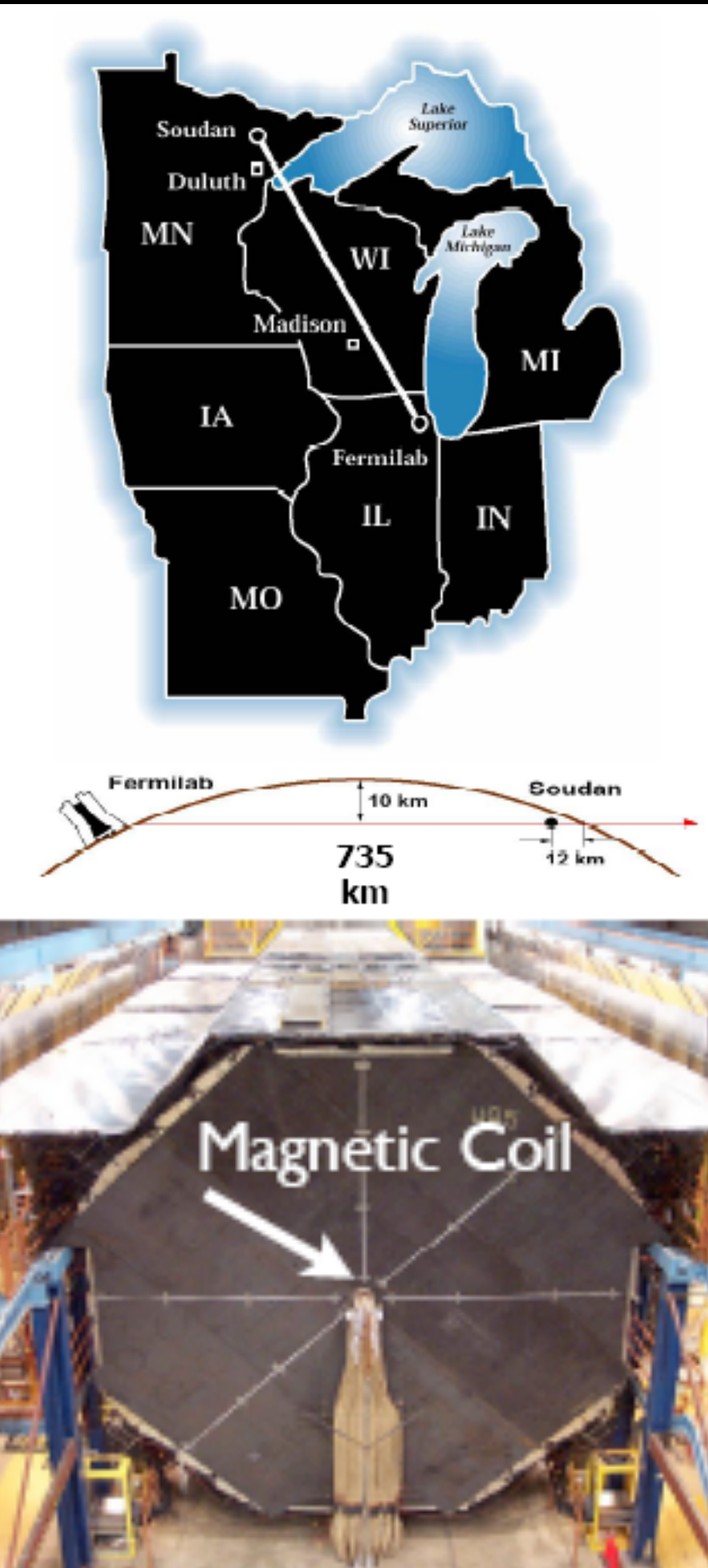
Spectral distortion compatible with atmospheric oscillation parameters



# MINOS



- Long-baseline experiment at Soudan with Fermilab beam (735 km)
- W/r K2K, beam is more intense and higher energy ( $\sim$ same L/E)
- Magnetized iron and plastic scintillator detector: better energy resolution
- Confirms SK and K2K with better precision on  $\Delta m^2$

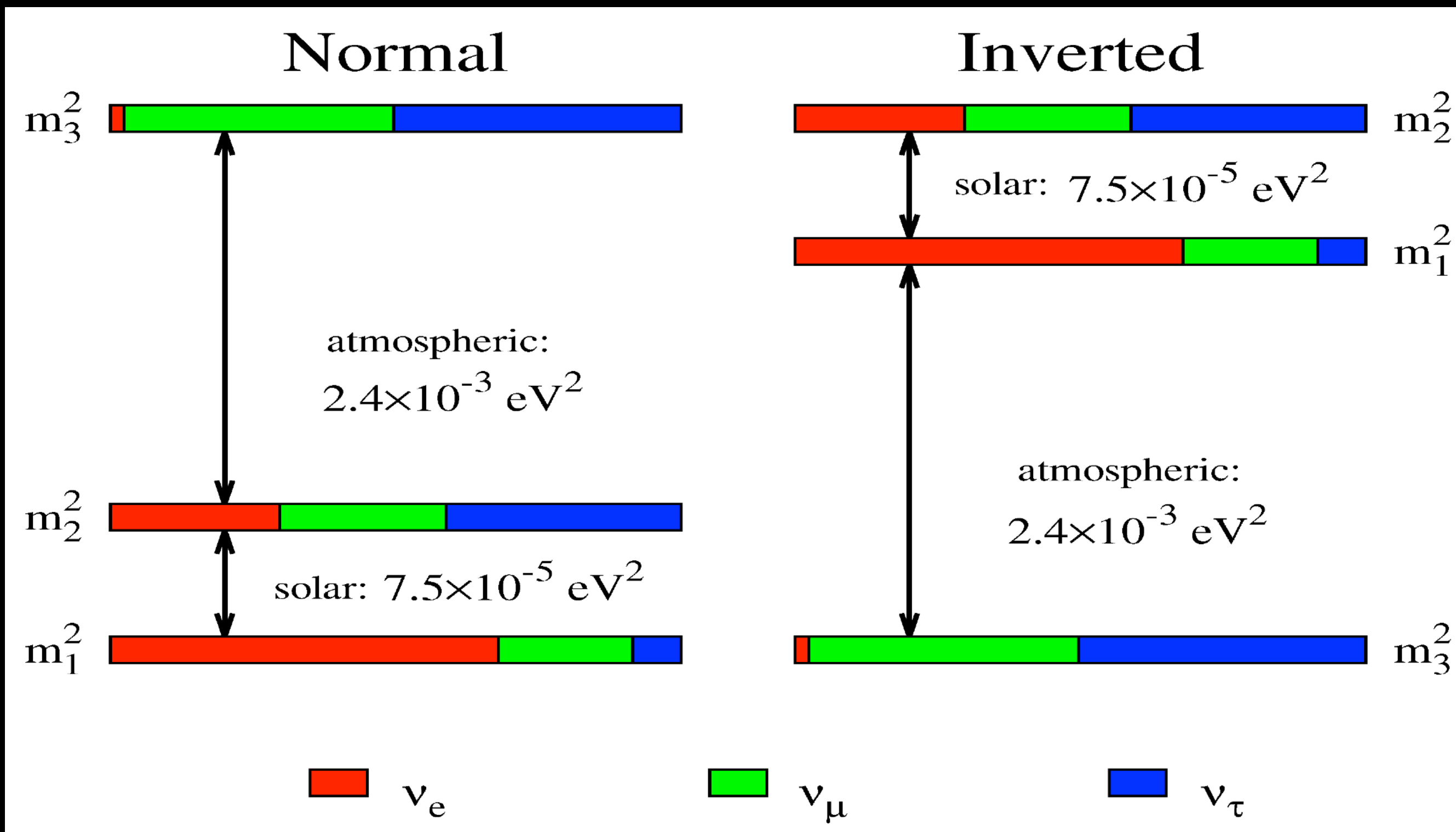


OSCILLATIONS WITH  
3 FLAVORS

# NEUTRINO MASS ORDERING



- With 3 neutrinos, have 2 independent mass splittings  $m_3^2 - m_1^2 = (m_3^2 - m_2^2) + (m_2^2 - m_1^2)$
- But that's OK, since
  - $|\Delta m_{sol}^2| \sim |\Delta m_{reaLBL}^2| \sim |\Delta m_{21}^2| \sim 7.5 \times 10^{-5} eV^2$
  - $|\Delta m_{atm}^2| \sim |\Delta m_{accLBL}^2| \sim |\Delta m_{32}^2| \sim 2.4 \times 10^{-3} eV^2$
- MSW effect in the Sun: we know  $\Delta m_{21}^2 > 0$ . Still, 2 possible orderings:



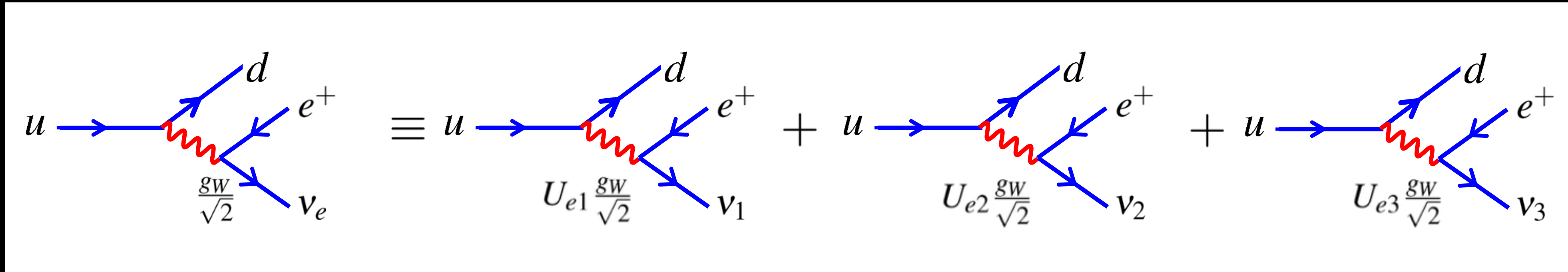
$\Delta m_{31}^2 \approx \Delta m_{32}^2$  is a common approximation but it's of course not true!

How to determine the order?

- make a precision measurement of  $|\Delta m_{31}^2|$
- measure sign of  $\Delta m_{32}^2$  as well, with matter effects



# 3 FLAVOR NEUTRINO MIXING



- Simple extension of the two-neutrino mechanism
- U elements are complex, in the general case

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

- Mixing matrix has to be unitary to preserve probability

$$\begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix} = \begin{pmatrix} U_{e1}^* & U_{\mu1}^* & U_{\tau1}^* \\ U_{e2}^* & U_{\mu2}^* & U_{\tau2}^* \\ U_{e3}^* & U_{\mu3}^* & U_{\tau3}^* \end{pmatrix} \begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix}$$

$$U^\dagger U = I \quad \Rightarrow \quad U^{-1} = U^\dagger = (U^*)^T$$

- Inverse matrix

- Unitarity constraints
- 18  $\rightarrow$  9 d.o.f

$$\begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix} \begin{pmatrix} U_{e1}^* & U_{\mu1}^* & U_{\tau1}^* \\ U_{e2}^* & U_{\mu2}^* & U_{\tau2}^* \\ U_{e3}^* & U_{\mu3}^* & U_{\tau3}^* \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

# SURVIVAL PROBABILITY



$$|\psi(t=0)\rangle = |\nu_e\rangle = U_{e1}|\nu_1\rangle + U_{e2}|\nu_2\rangle + U_{e3}|\nu_3\rangle$$

$$|\psi(L)\rangle = U_{e1}|\nu_1\rangle e^{-i\phi_1} + U_{e2}|\nu_2\rangle e^{-i\phi_2} + U_{e3}|\nu_3\rangle e^{-i\phi_3}$$

$$\begin{aligned} |\psi(L)\rangle &= (U_{e1}U_{e1}^*e^{-i\phi_1} + U_{e2}U_{e2}^*e^{-i\phi_2} + U_{e3}U_{e3}^*e^{-i\phi_3})|\nu_e\rangle \\ &+ (U_{e1}U_{\mu 1}^*e^{-i\phi_1} + U_{e2}U_{\mu 2}^*e^{-i\phi_2} + U_{e3}U_{\mu 3}^*e^{-i\phi_3})|\nu_\mu\rangle \\ &+ (U_{e1}U_{\tau 1}^*e^{-i\phi_1} + U_{e2}U_{\tau 2}^*e^{-i\phi_2} + U_{e3}U_{\tau 3}^*e^{-i\phi_3})|\nu_\tau\rangle \end{aligned}$$

$$\begin{aligned} P(\nu_e \rightarrow \nu_e) &= |\langle \nu_e | \psi(L) \rangle|^2 \\ &= |U_{e1}U_{e1}^*e^{-i\phi_1} + U_{e2}U_{e2}^*e^{-i\phi_2} + U_{e3}U_{e3}^*e^{-i\phi_3}|^2 \end{aligned}$$

$$\begin{aligned} P(\nu_e \rightarrow \nu_e) = 1 &+ 2|U_{e1}|^2|U_{e2}|^2\Re\{[e^{-i(\phi_1-\phi_2)} - 1]\} \\ &+ 2|U_{e1}|^2|U_{e3}|^2\Re\{[e^{-i(\phi_1-\phi_3)} - 1]\} \\ &+ 2|U_{e2}|^2|U_{e3}|^2\Re\{[e^{-i(\phi_2-\phi_3)} - 1]\} \end{aligned}$$

• flavor states  $|\nu_\alpha\rangle = \sum_k U_{\alpha k} |\nu_k\rangle$  • mass states

$\nu_\alpha = \nu_e, \nu_\mu, \nu_\tau$   $\nu_k = \nu_1, \nu_2, \nu_3$

$$\phi_i = p_i \cdot x = E_i t - |\vec{p}|L = (E_i - |\vec{p}|)L$$

expressing  $\nu_1, \nu_2, \nu_3$  as a function of  $\nu_e, \nu_\mu, \nu_\tau$  and re-arranging the terms

making use of unitarity relations

# SURVIVAL PROBABILITY



$$P(\nu_e \rightarrow \nu_e) = 1 + 2|U_{e1}|^2|U_{e2}|^2\Re\{[e^{-i(\phi_1-\phi_2)} - 1]\} + 2|U_{e1}|^2|U_{e3}|^2\Re\{[e^{-i(\phi_1-\phi_3)} - 1]\} + 2|U_{e2}|^2|U_{e3}|^2\Re\{[e^{-i(\phi_2-\phi_3)} - 1]\}$$

$$\begin{aligned} \Re\{e^{-i(\phi_1-\phi_2)} - 1\} &= \cos(\phi_2 - \phi_1) - 1 \\ &= -2\sin^2\left(\frac{\phi_2 - \phi_1}{2}\right) \\ \phi_i \approx \frac{m_i^2}{2E}L &\longrightarrow = -2\sin^2\left(\frac{(m_2^2 - m_1^2)L}{4E}\right) \end{aligned}$$

$$\Delta m_{21}^2 = m_2^2 - m_1^2$$

$$\Delta_{21} = \frac{(m_2^2 - m_1^2)L}{4E} = \frac{\Delta m_{21}^2 L}{4E} = 1.27 \frac{\Delta m_{21}^2 (\text{eV}^2)L(\text{km})}{E(\text{GeV})}$$



$$P(\nu_e \rightarrow \nu_e) = 1 - 4|U_{e1}|^2|U_{e2}|^2 \sin^2 \Delta_{21} - 4|U_{e1}|^2|U_{e3}|^2 \sin^2 \Delta_{31} - 4|U_{e2}|^2|U_{e3}|^2 \sin^2 \Delta_{32}$$

- Let's examine this. Survival (or disappearance) probability:
  - Depends only on module of U elements, not on phases
  - Depends on Δs only via sin², so does not depend on sign of any Δm².

- General expression for both survival and oscillation:
 
$$P(\nu_\alpha \rightarrow \nu_\beta) = \left| \langle \nu_\beta | \nu_\alpha(L) \rangle \right|^2 = \left| \sum_i U_{\alpha i}^* U_{\beta i} e^{-i \left( \frac{m_i^2 L}{2E} \right)} \right|^2$$

$$A_{\alpha\beta}^{ij} = U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*$$

$$\Delta m_{ij}^2 = m_i^2 - m_j^2$$

$$= \delta_{\alpha\beta} - 4 \sum_{i>j} \Re A_{\alpha\beta}^{ij} \sin^2 \left( \frac{\Delta m_{ij}^2 L}{4E} \right) + 2 \sum_{i>j} \Im A_{\alpha\beta}^{ij} \sin \left( \frac{\Delta m_{ij}^2 L}{2E} \right)$$

- Let's examine this as well. If  $\alpha \neq \beta$ , oscillation (or appearance) probability:
  - Depends also on phases
  - Depends on  $\Delta$ s also via a sin term, so it does depend on sign of  $\Delta m^2$ 
    - But not if U is real, since in that case  $\Im A_{\alpha\beta}^{ij} = 0$

$$\begin{aligned}
 P\left(\nu_\beta \rightarrow \nu_\alpha\right) &= \left| \langle \nu_\alpha | \nu_\beta(L) \rangle \right|^2 = \left| \sum_i U_{\alpha i} U_{\beta i}^* e^{-i\left(\frac{m_i^2 L}{2E}\right)} \right|^2 \\
 &= \delta_{\alpha\beta} - 4 \sum_{i>j} \Re(A_{\alpha\beta}^{ij})^* \sin^2\left(\frac{\Delta m_{ij}^2 L}{4E}\right) + 2 \sum_{i>j} \Im(A_{\alpha\beta}^{ij})^* \sin\left(\frac{\Delta m_{ij}^2 L}{2E}\right)
 \end{aligned}$$

- If the U matrix is not real, then

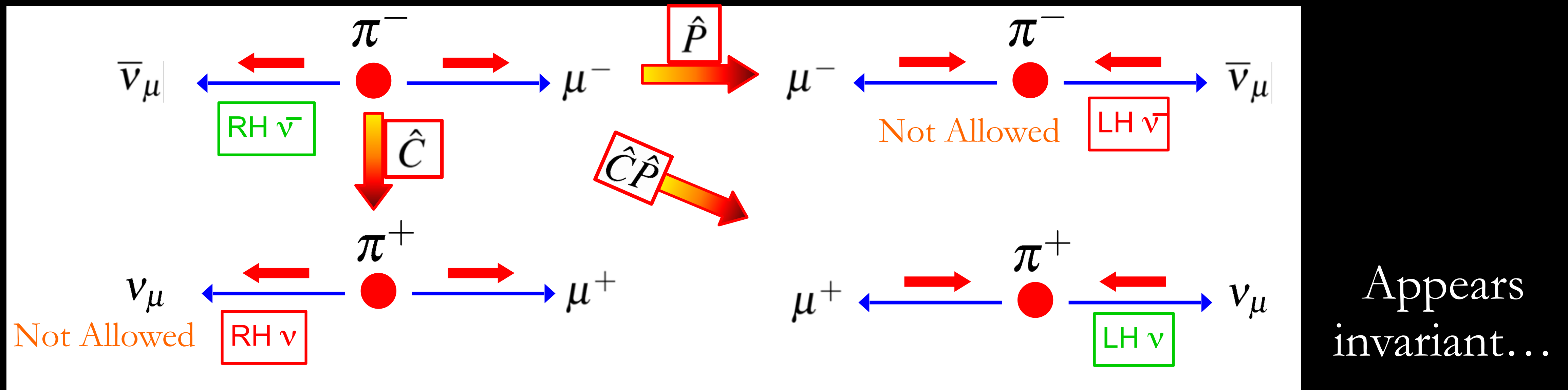
$$P\left(\nu_\alpha \rightarrow \nu_\beta\right) \neq P\left(\nu_\beta \rightarrow \nu_\alpha\right)$$

- Not time-symmetric!

- In addition to parity, two other discrete symmetries

Parity	$\hat{P} :$	$\vec{r} \rightarrow -\vec{r}$
Time Reversal	$\hat{T} :$	$t \rightarrow -t$
Charge Conjugation	$\hat{C} :$	Particle $\leftrightarrow$ Anti-particle

- Weak interactions violate P. CPT must be conserved. But what about C and CP ?



- Effect of discrete symmetries in neutrino oscillations:

T	$\nu_e \rightarrow \nu_\mu$	$\xrightarrow{\hat{T}}$	$\nu_\mu \rightarrow \nu_e$
CP	$\nu_e \rightarrow \nu_\mu$	$\xrightarrow{\hat{C}\hat{P}}$	$\bar{\nu}_e \rightarrow \bar{\nu}_\mu$
CPT	$\nu_e \rightarrow \nu_\mu$	$\xrightarrow{\hat{C}\hat{P}\hat{T}}$	$\bar{\nu}_\mu \rightarrow \bar{\nu}_e$

- CPT conservation implies:  $P(\nu_e \rightarrow \nu_\mu) = P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)$        $P(\nu_\mu \rightarrow \nu_e) = P(\bar{\nu}_e \rightarrow \bar{\nu}_\mu)$
- But we saw that, if the PMNS matrix is not real, then  $P(\nu_e \rightarrow \nu_\mu) \neq P(\nu_\mu \rightarrow \nu_e)$
- Therefore  $P(\nu_e \rightarrow \nu_\mu) \neq P(\bar{\nu}_e \rightarrow \bar{\nu}_\mu)$
- So, if the PMNS matrix is not real, CP is violated in neutrino oscillations!

IMPORTANT IMPLICATIONS ON THE MATTER/ANTIMATTER ASYMMETRY IN THE UNIVERSE!

- PMNS matrix degrees of freedom?
  - 3x3 complex numbers, so 18 real numbers. Minus 9 unitarity constraints = 9 d.o.f
  - 3 real angles and 6 complex phases, but the charged leptons are Dirac particles, their fields can be phase rotated.
  - So 3 angles -  $\theta_{12}, \theta_{13}, \theta_{23}$  - and 3 phases ( $\delta_{CP}, \alpha, \beta$ )

$$s_{ij} = \sin \theta_{ij}$$

$$c_{ij} = \cos \theta_{ij}$$

$$\begin{bmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{bmatrix} \begin{bmatrix} c_{13} & 0 & s_{13}e^{-i\delta_{CP}} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta_{CP}} & 0 & c_{13} \end{bmatrix} \begin{bmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & e^{i\alpha} & 0 \\ 0 & 0 & e^{i\beta} \end{bmatrix} \begin{bmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{bmatrix}$$

- The Majorana phases ( $\alpha, \beta$ ) appear in the diagonal, so no effect on oscillations

$$\begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \times \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{-i\delta} & 0 & c_{13} \end{pmatrix} \times \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$\theta_{23} \approx 49^\circ$  Atmospheric

Solar  $\theta_{12} \approx 33.4^\circ$



# OSCILLATION PROBABILITY



- We can now write the oscillation probability as a function of the angles and phase

$$P(\nu_e \rightarrow \nu_\mu) = |\langle \nu_\mu | \psi(L) \rangle|^2$$

$$= |U_{e1}U_{\mu 1}^* e^{-i\phi_1} + U_{e2}U_{\mu 2}^* e^{-i\phi_2} + U_{e3}U_{\mu 3}^* e^{-i\phi_3}|^2$$

$$P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e) \simeq \sin^2 \theta_{23} \sin^2 2\theta_{13}$$

$$\frac{\sin^2(\Delta_{31} - aL)}{(\Delta_{31} - aL)^2} \Delta_{31}^2$$

$$+ \sin 2\theta_{23} \sin 2\theta_{13} \sin 2\theta_{12}$$

$$\times \frac{\sin(\Delta_{31} - aL)}{(\Delta_{31} - aL)} \Delta_{31}$$

$$\times \frac{\sin(aL)}{aL} \Delta_{21} \cos(\Delta_{31} \pm \delta_{CP})$$

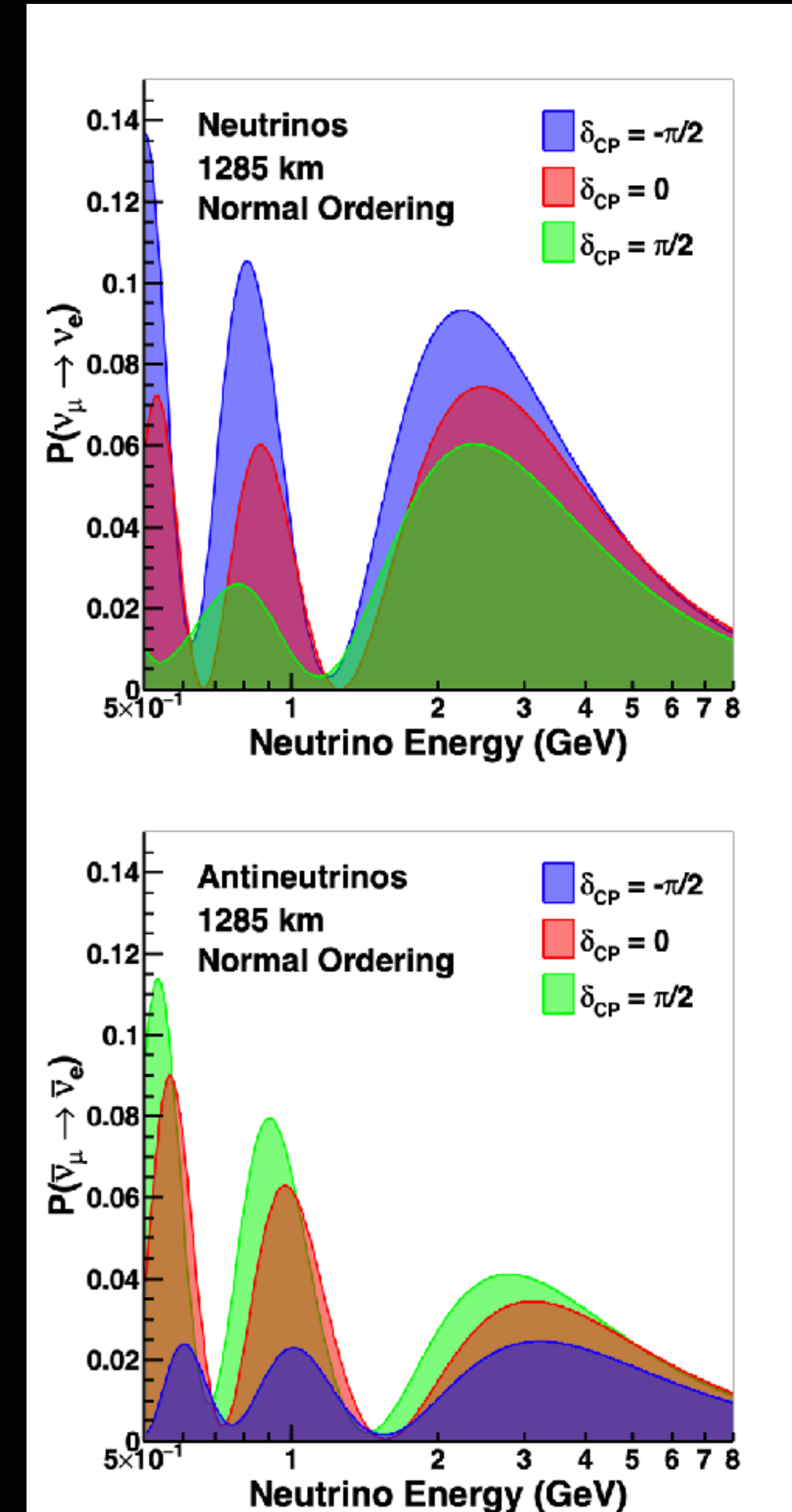
$$+ \cos^2 \theta_{23} \sin^2 2\theta_{12} \frac{\sin^2(aL)}{(aL)^2} \Delta_{21}^2$$

Matter Effects  $a = \pm \frac{G_F N_e}{\sqrt{2}}$

+ Neutrinos  
- Antineutrinos

CP violation

$$\Delta_{ij} = 1.267 \Delta m_{ij}^2 L / E_\nu$$



# BEST STRATEGY FOR EACH ANGLE?



- Since the mass splittings are quite different, the best experiment to measure each mixing angle is different

VACUUM OSCILLATION LENGTH	E ~ 3 MEV (REACTORS)	E ~ 1 GEV (ATM, ACC)
$ \Delta m_{21}^2  \sim 7.5 \times 10^{-5} eV^2$	50 KM (LBL)	16,000 KM (TOO BIG!)
$ \Delta m_{13}^2  \sim  \Delta m_{23}^2  \sim 2.4 \times 10^{-3} eV^2$	1.5 KM (SBL)	515 KM (LBL)

S(L)BL=  
Short (Long)  
Baseline

ACC LBL

REACTOR SBL,  
ACC LBL

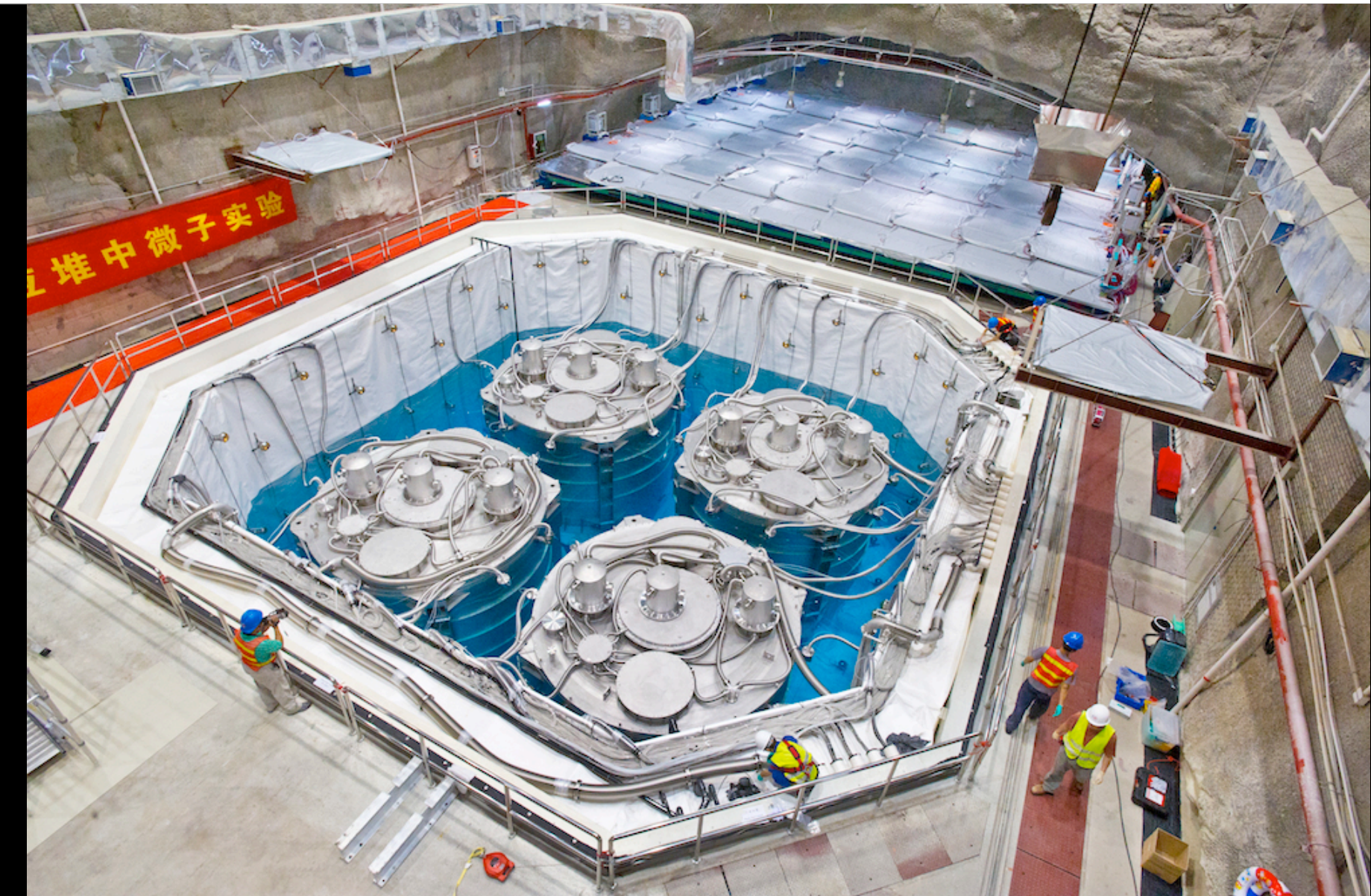
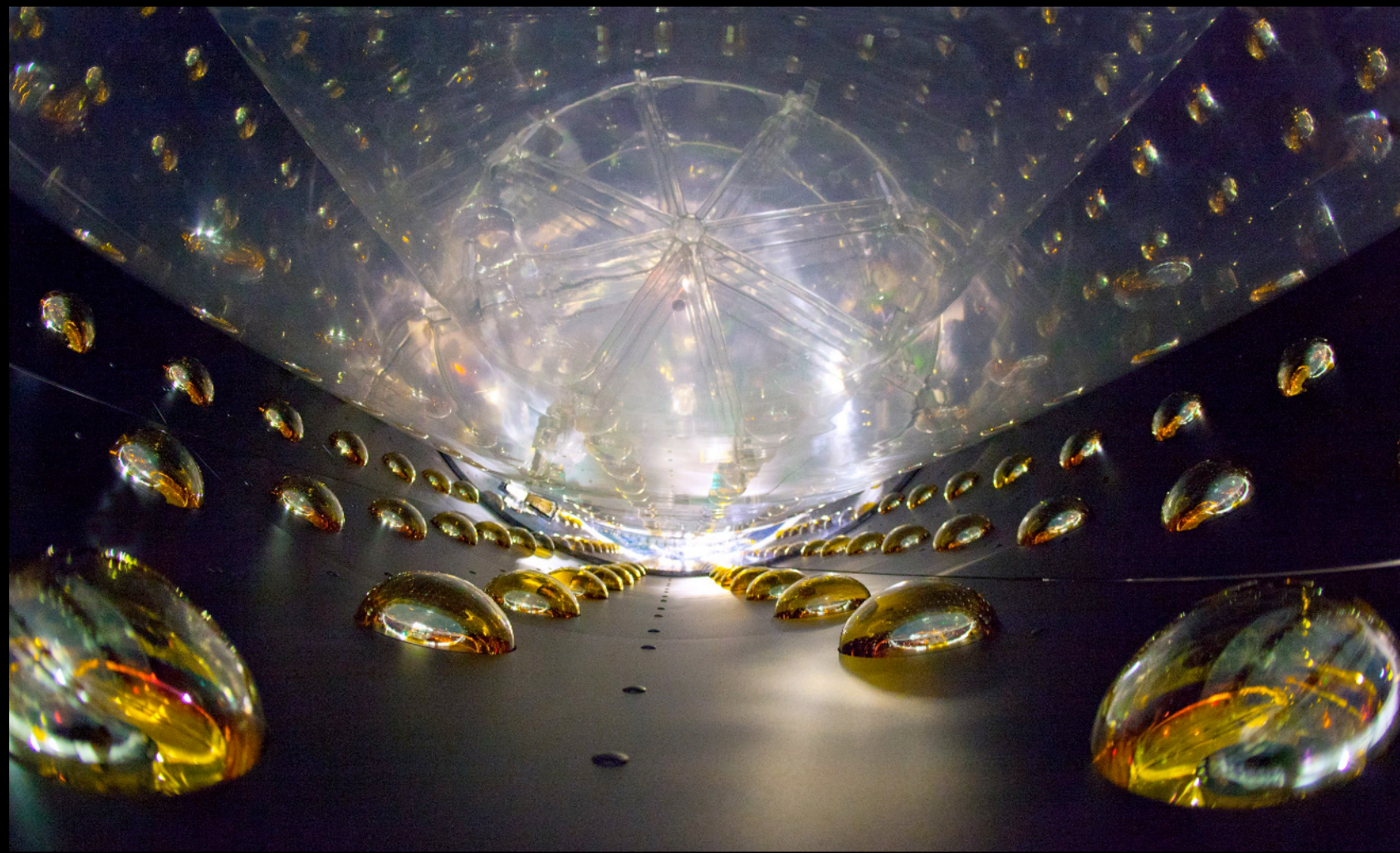
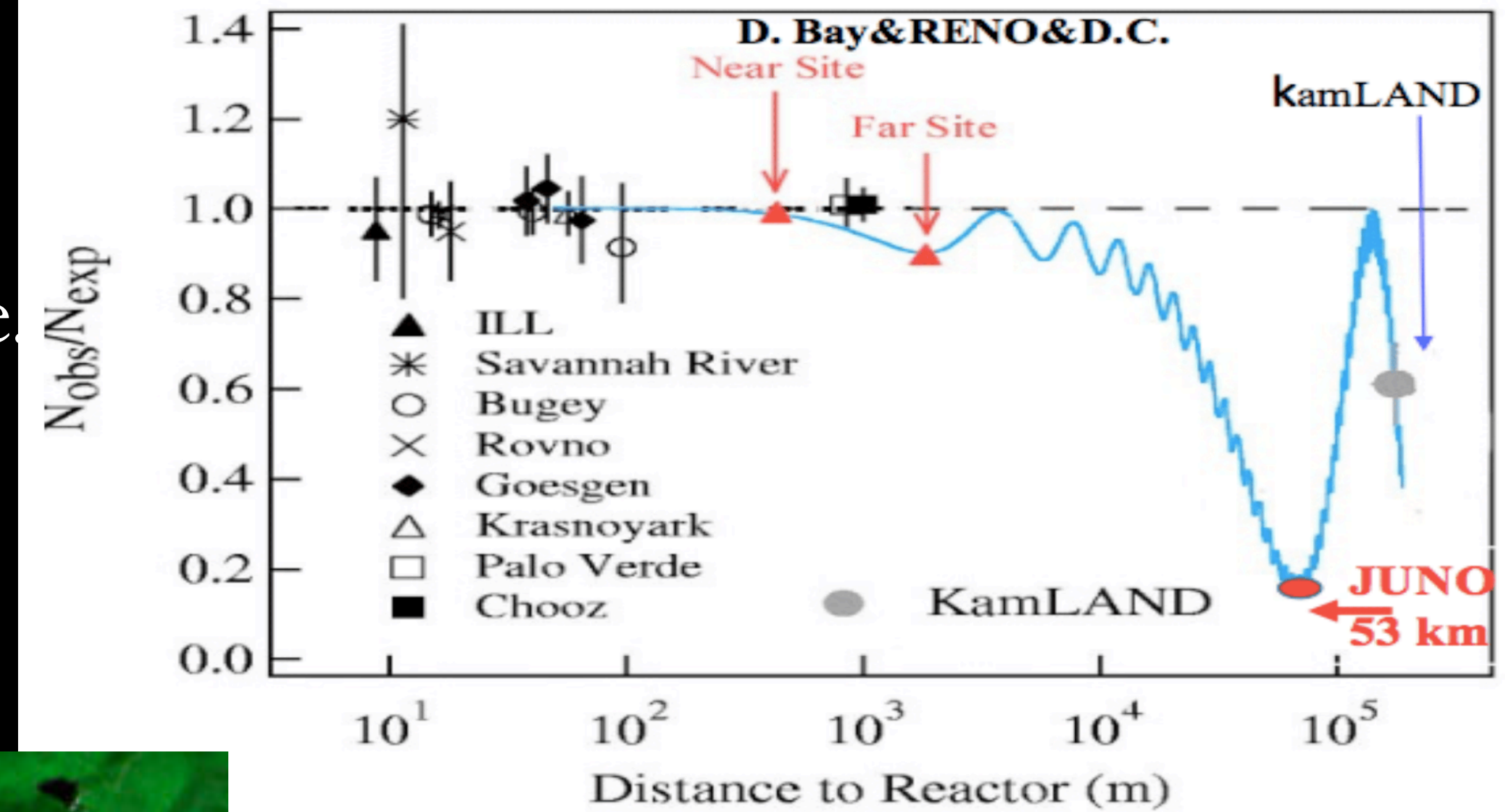
SOLAR (MSW),  
REACTOR LBL

$$\begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \times \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{-i\delta} & 0 & c_{13} \end{pmatrix} \times \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

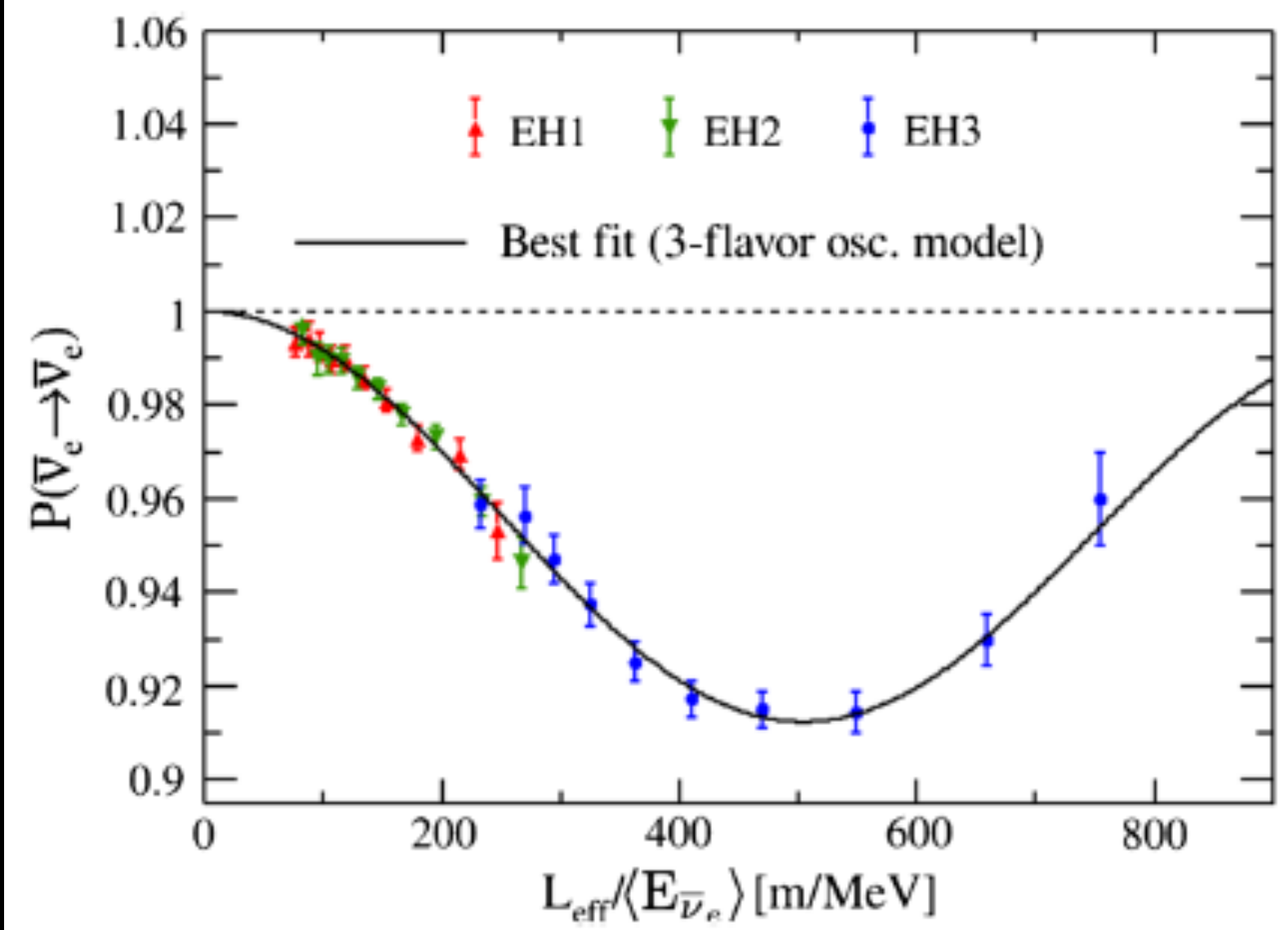
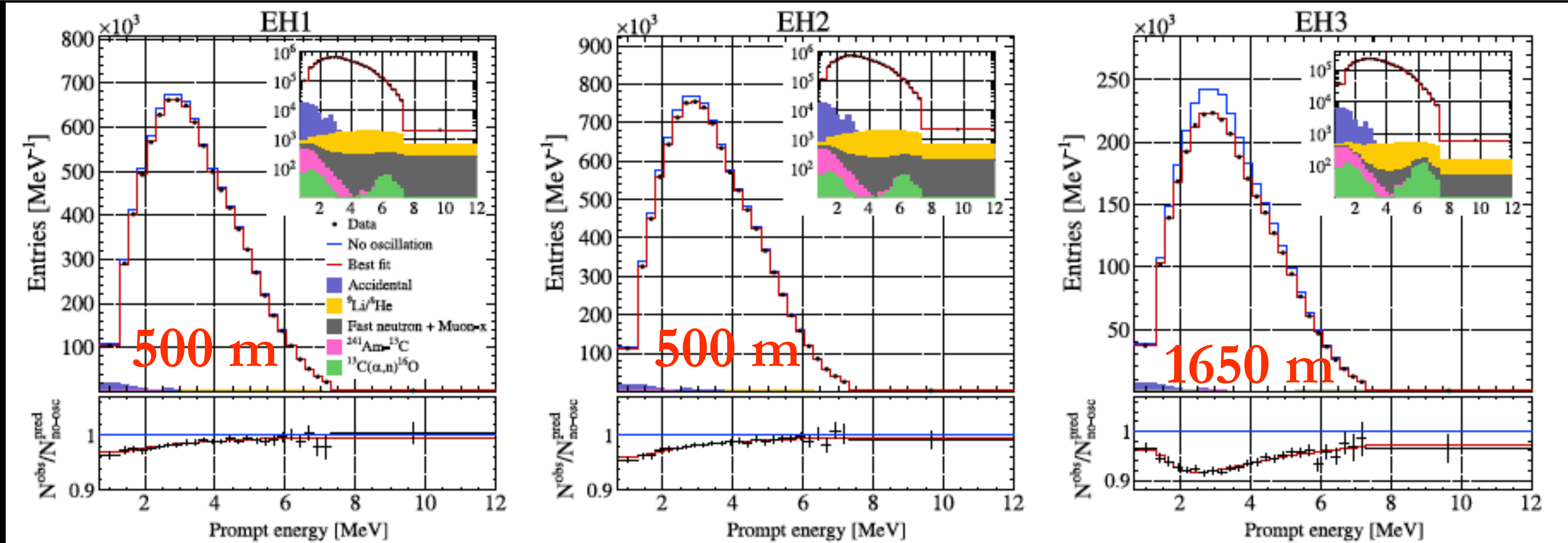
**CURRENT STATUS,  
REACTOR AND ACCELERATOR  
EXPERIMENTS**

# DAYA BAY AND THETA 13

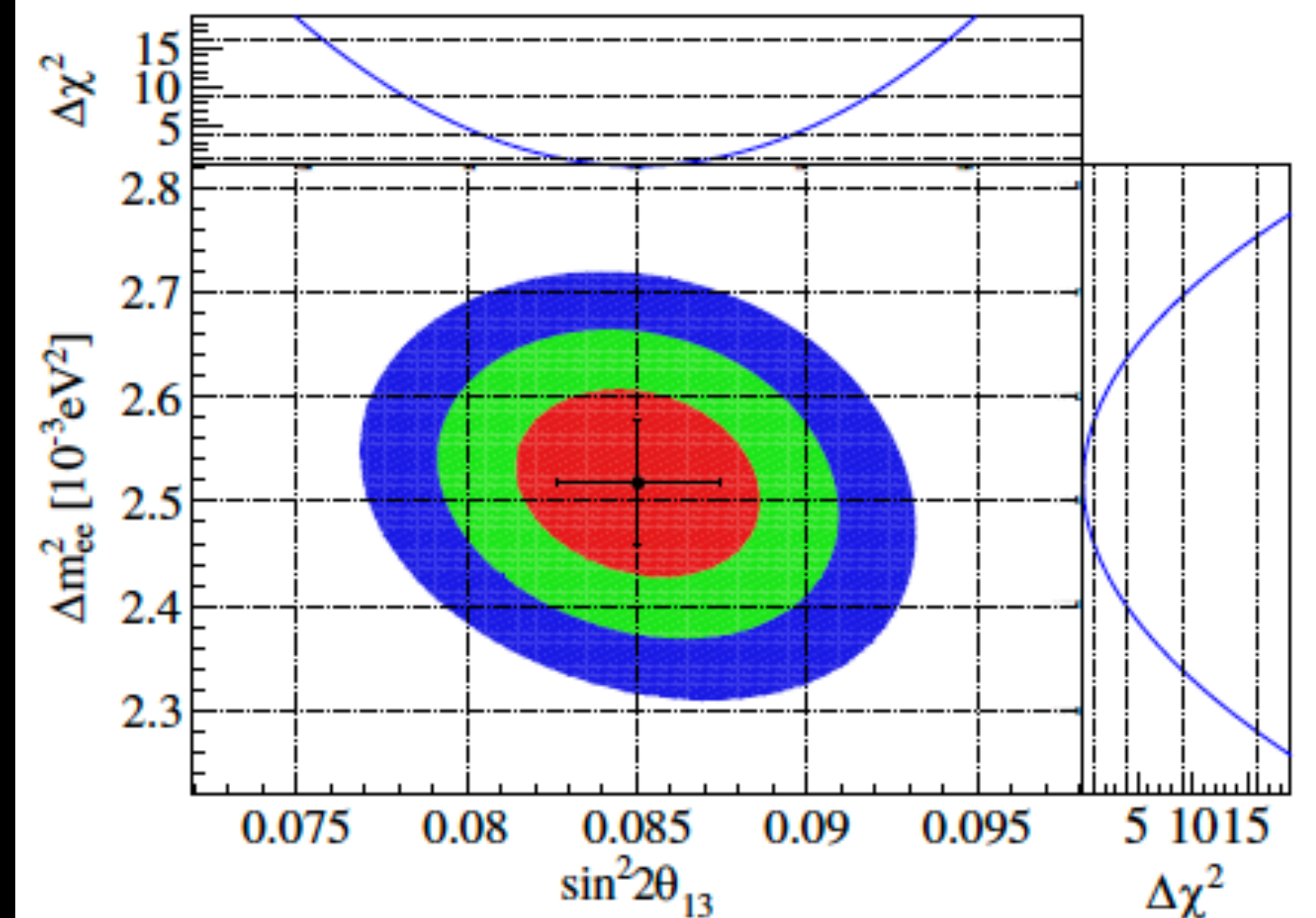
- Next: how to measure  $\theta_{13}$ ?
- Coupled to  $\Delta m_{31}^2$ . At reactor neutrino energies, oscillation length  $\sim 1$  km. Previous exp. too close
- Also, if  $\theta_{13}$  is small, amplitude also small.
- The key experiment was Daya Bay in China
- Two sets of near detectors, one of far detectors
- All identical, so systematic uncertainties cancel



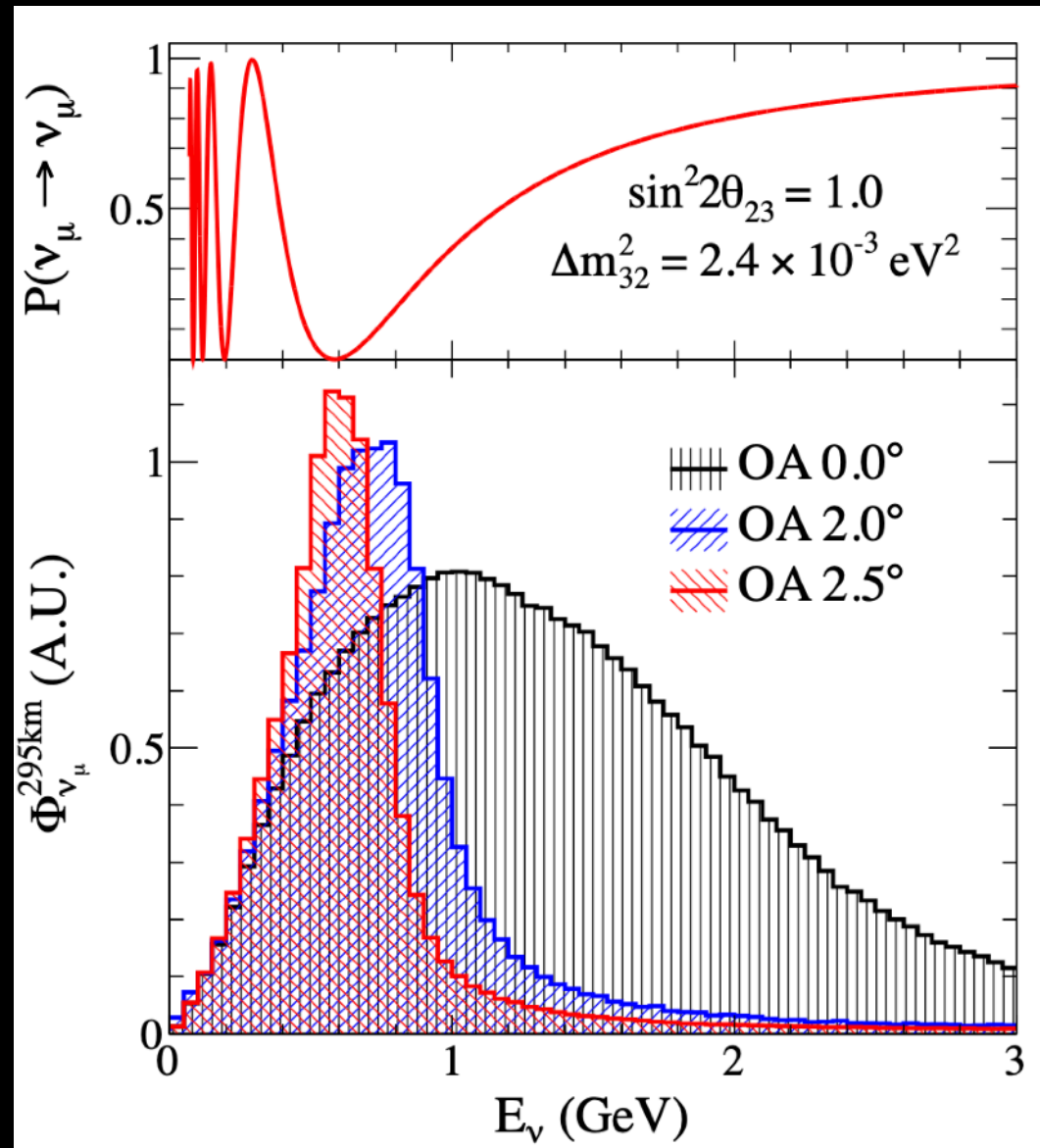
# DAYA BAY RESULTS



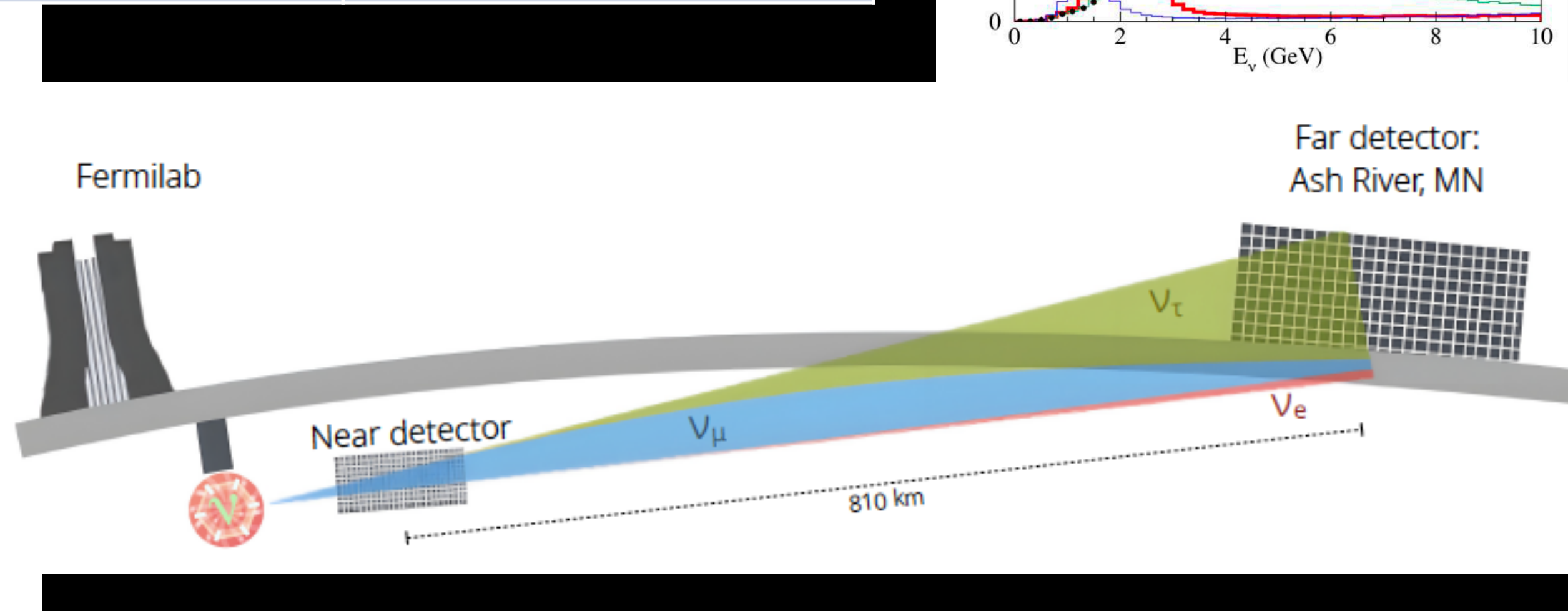
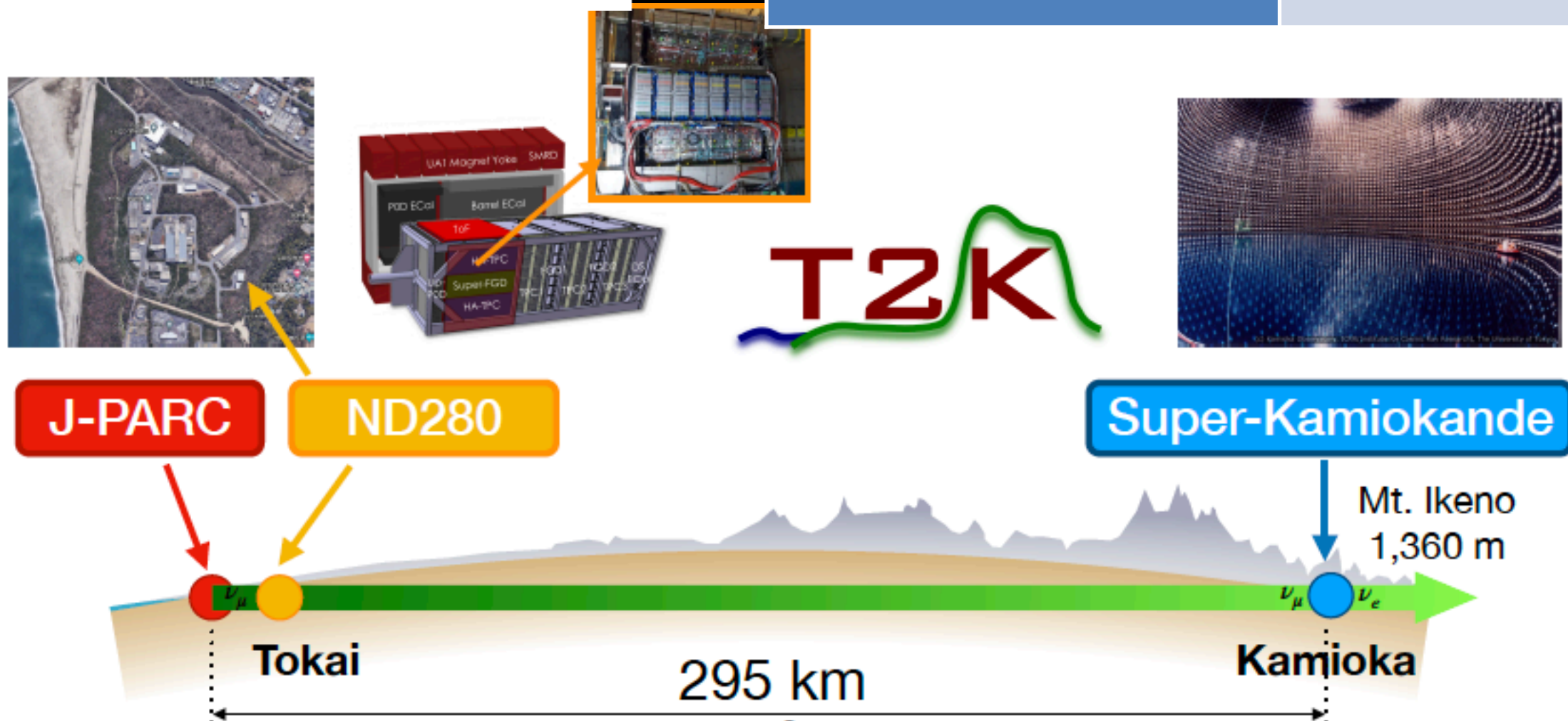
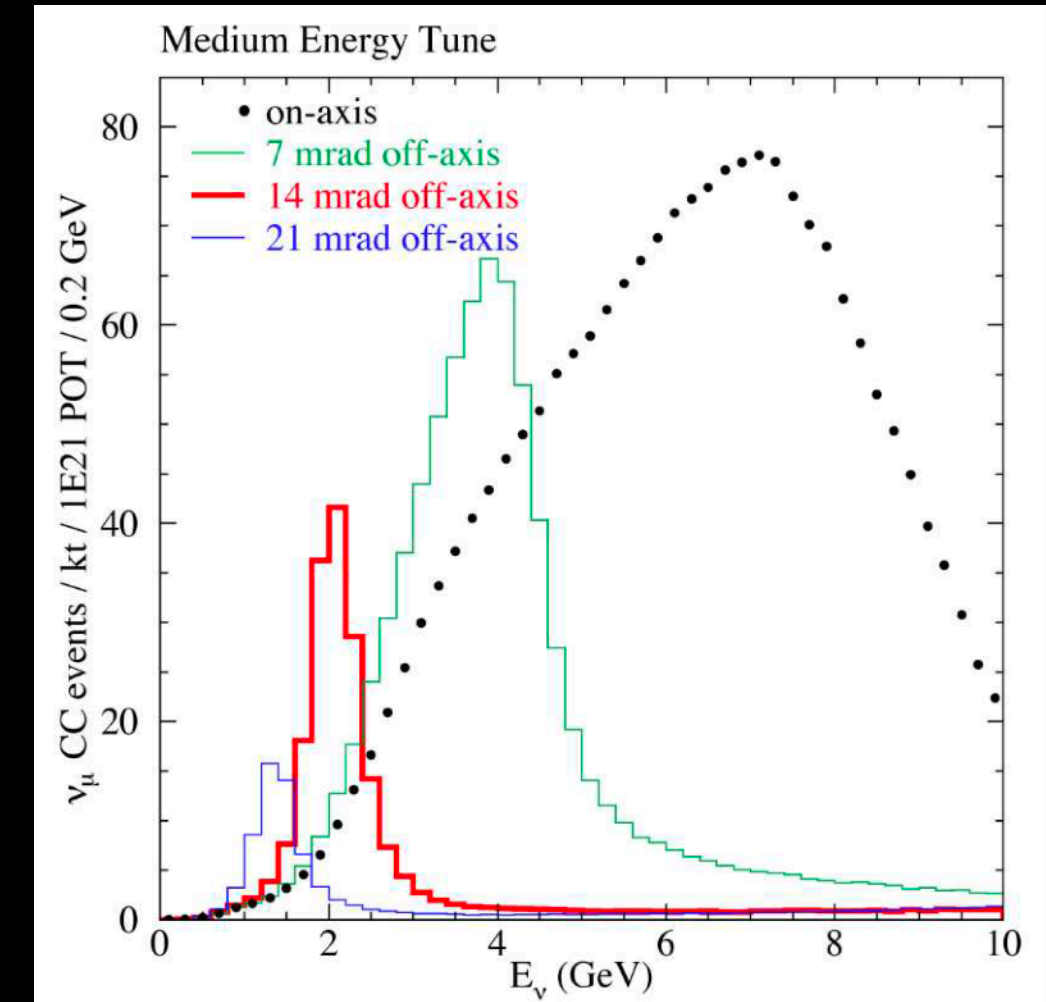
- Outstanding precision
- Even with a small amplitude, very good measurement



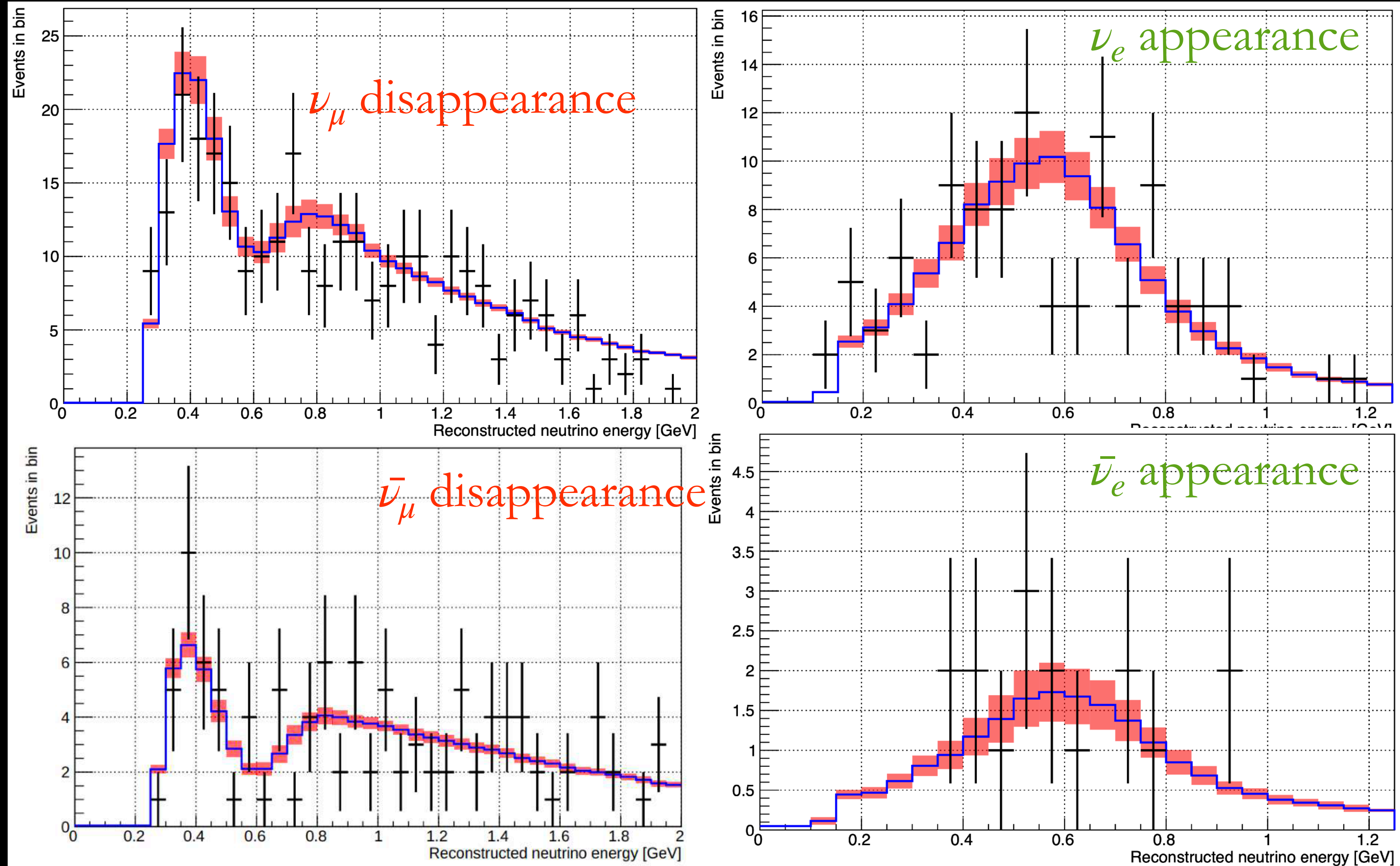
# LBL ACCELERATOR: T2K & NOVA



Beam	JPARC (515 kW)	NuMI, FNAL (700 kW)
Baseline	295 km, off-axis	810 km, off-axis
Peak Energy@FD	0.6 GeV	2 GeV
Far detector	SK, WCD (50 kt)	segmented LS (14 kt)
Near detector	on-axis (INGRID), off-axis (ND280)	functionally identical (300 t)

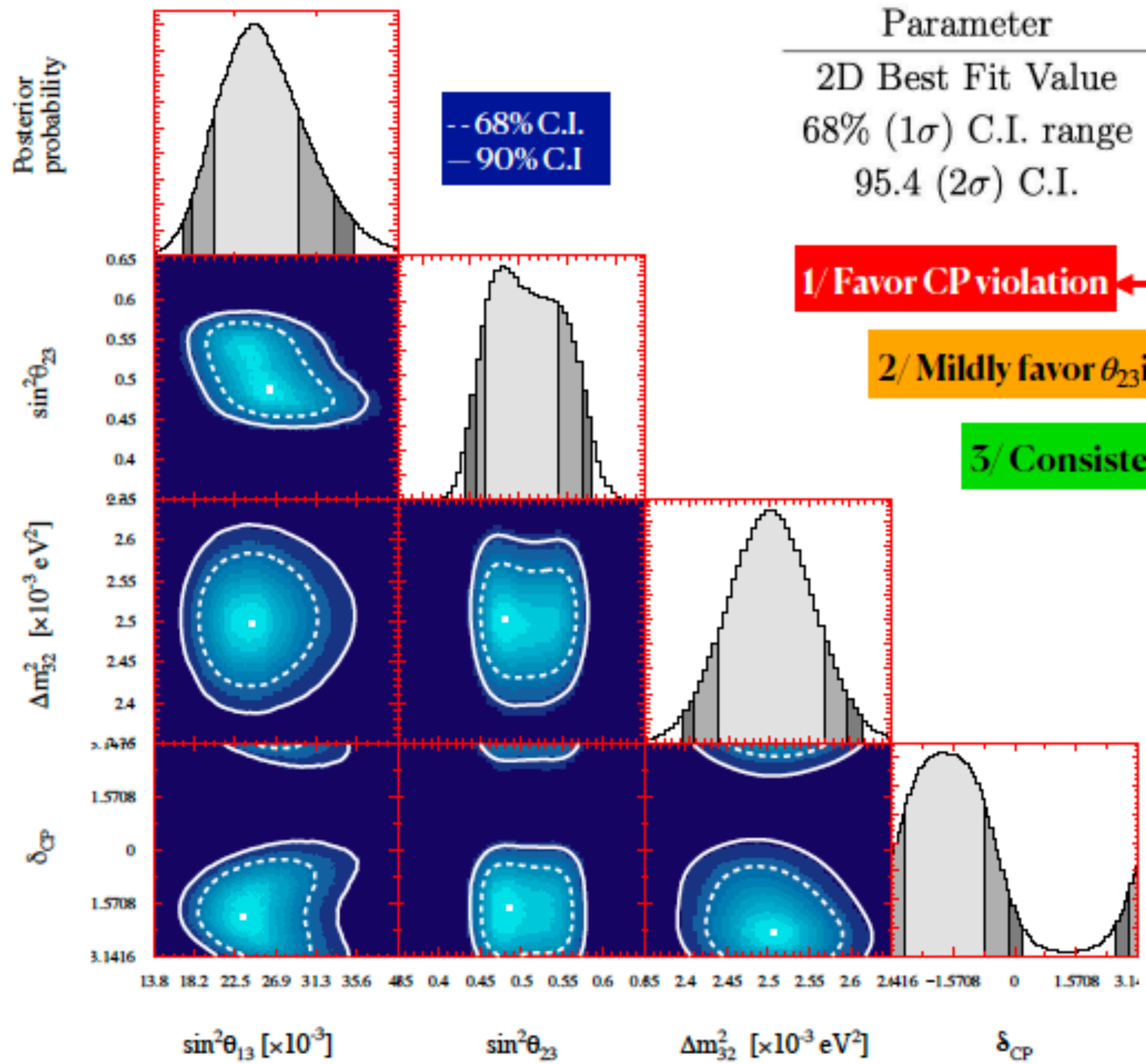


# LATEST T2K RESULTS



With these 4 observation channels, sensitive to many oscillation parameters

# Latest results from T2K



Parameter	$\delta_{CP}$ [rad.]	$\sin^2 \theta_{23}$	$\sin^2 \theta_{13}$	$\Delta m_{32}^2$ [ $\times 10^{-3}$ eV $^2$ ]
2D Best Fit Value	-2.01	0.48	0.024	2.51
68% ( $1\sigma$ ) C.I. range	[-2.83, -0.75]	[0.47, 0.55]	[0.021, 0.030]	[-2.59, -2.51] $\cup$ [2.44, 2.57]
95.4 ( $2\sigma$ ) C.I.	$[-\pi, 0.25] \cup [2.51, \pi]$	[0.45, 0.58]	[0.018, 0.036]	[-2.65, -2.45] $\cup$ [2.39, 2.62]

1/ Favor CP violation

2/ Mildly favor  $\theta_{23}$  in lower octant

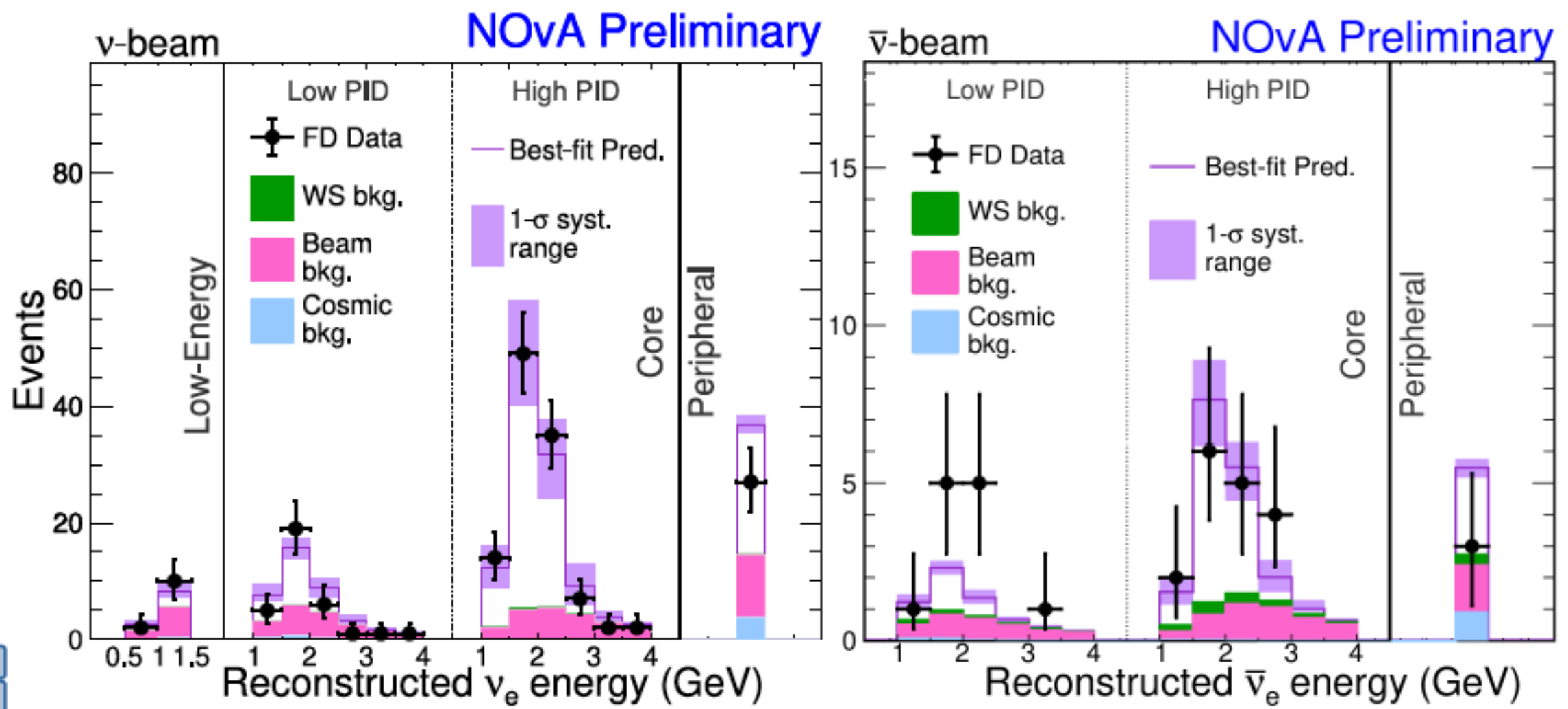
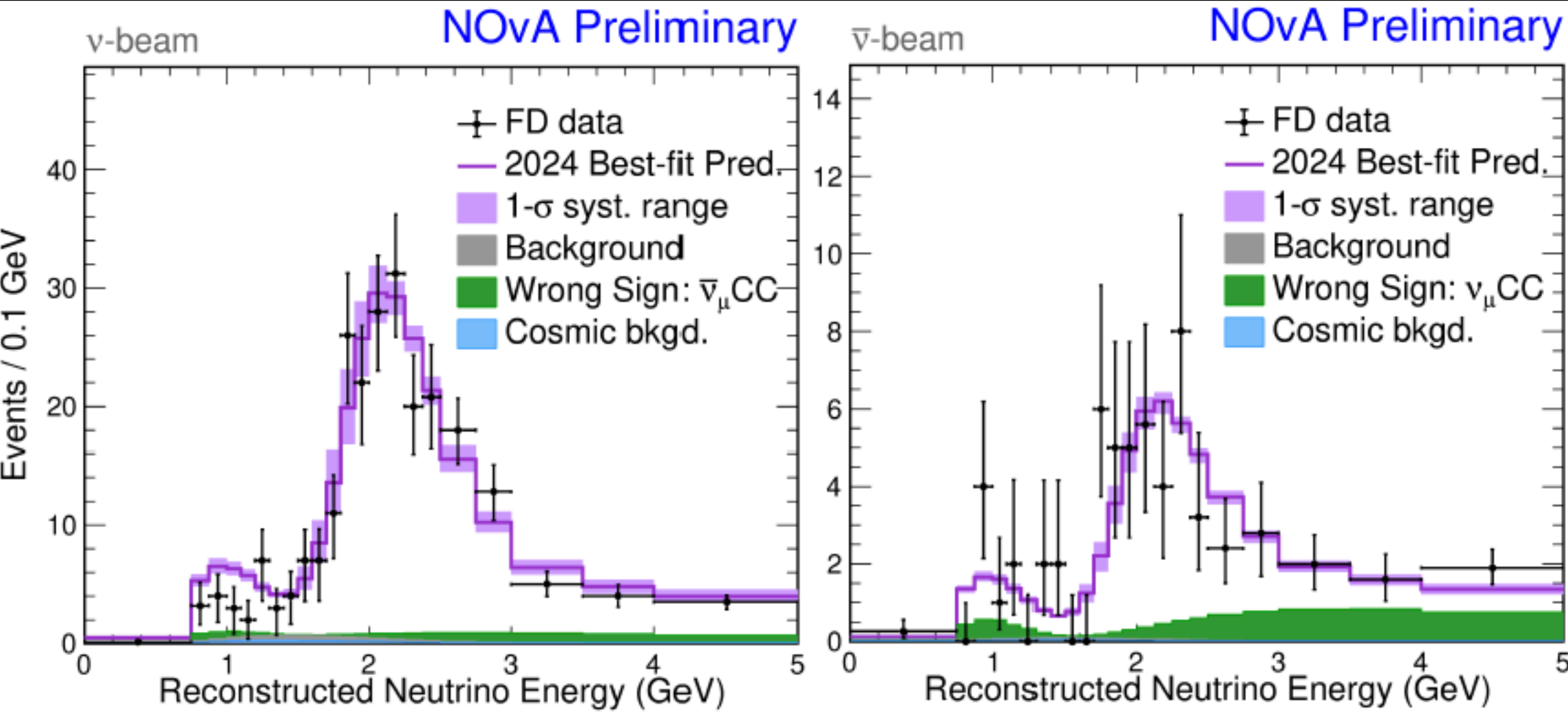
3/ Consistent w/ reactor-based measurements

4/ Slightly favor normal  $\nu$  mass ordering

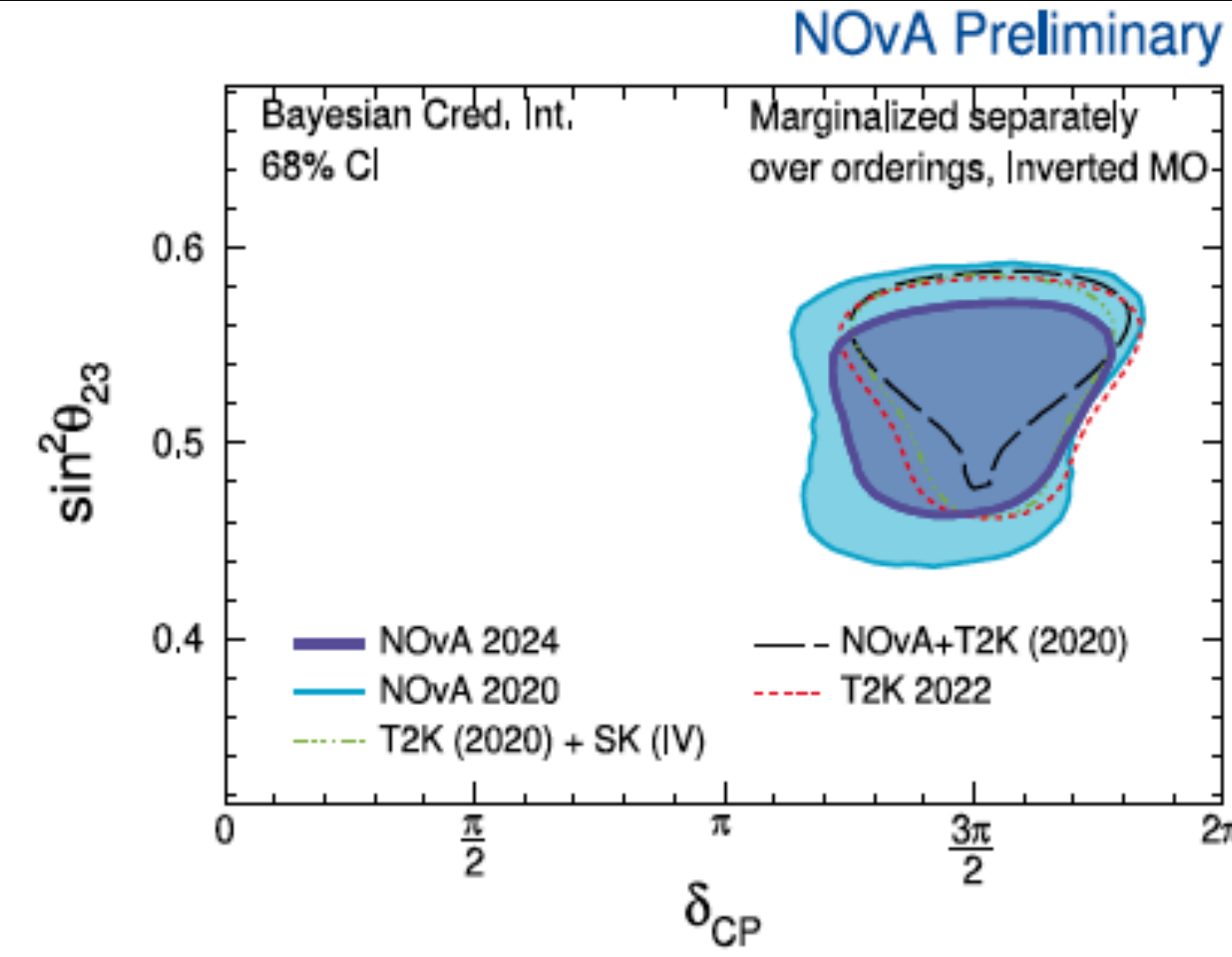
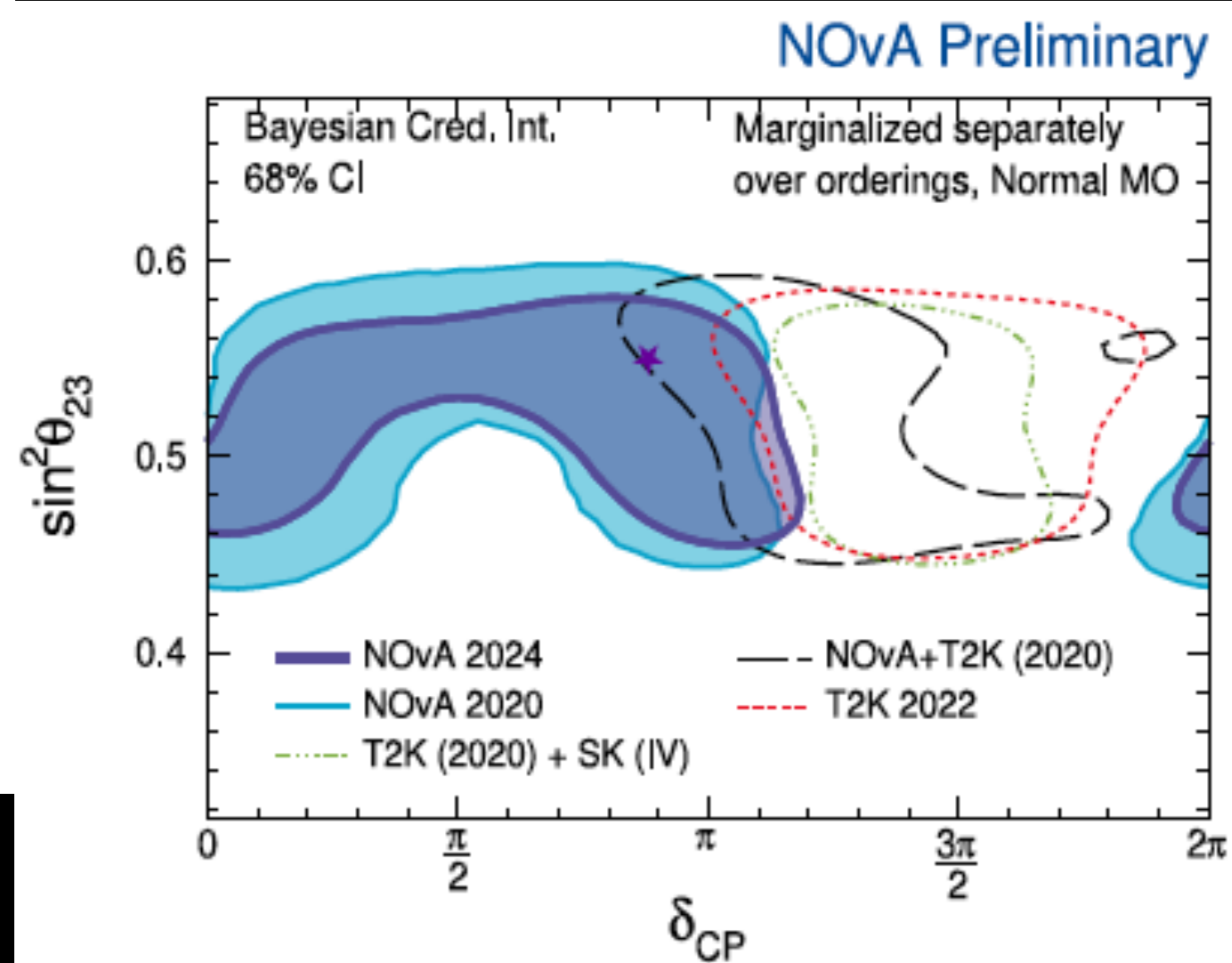
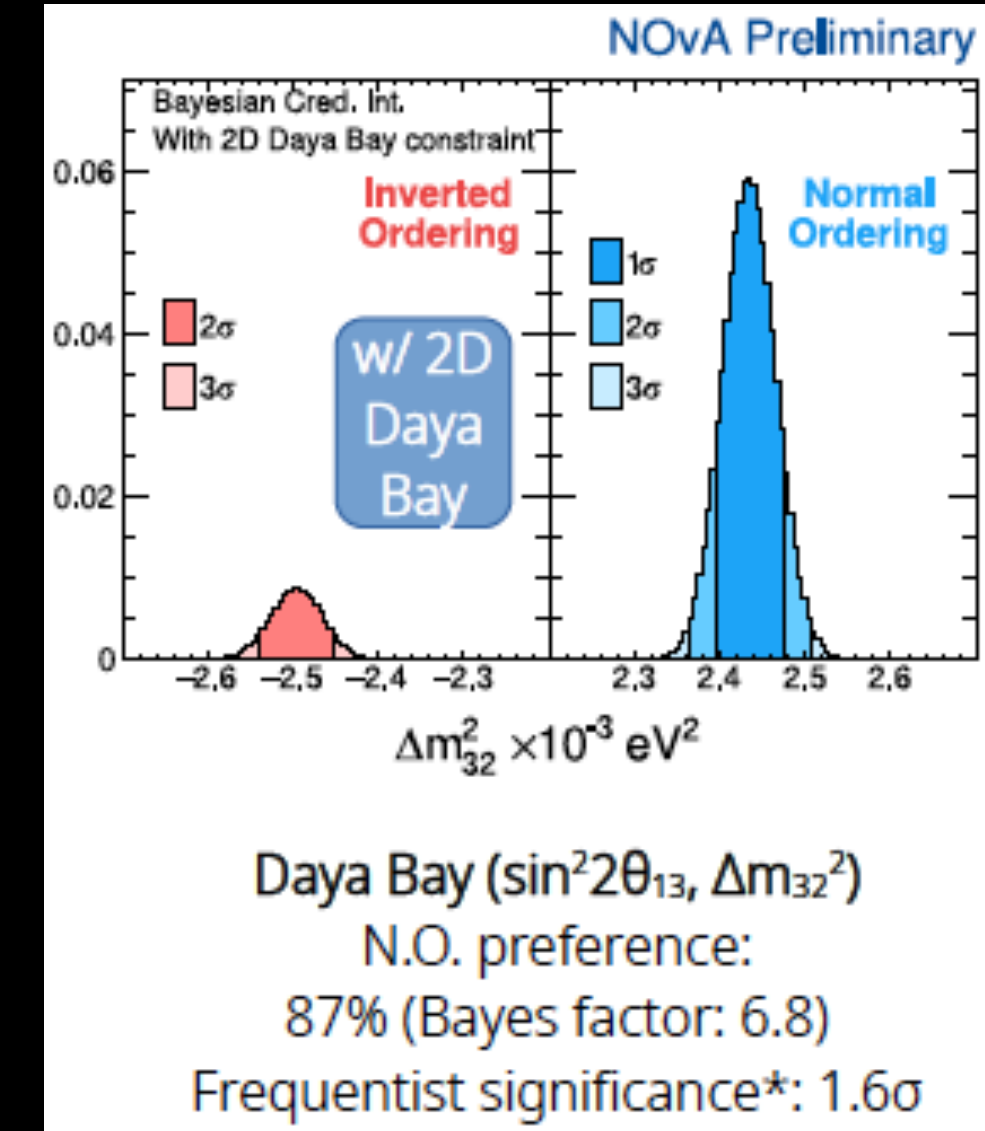
- 4 out of total 6 parameters constrained by T2K data only
- T2K measurement of  $\theta_{13}$  is consistent but less stringent than constraint from reactor-based  $\nu$  experiments,  $\sin^2 \theta_{13}^{\text{reactor}} = 0.0220 \pm 0.0007$
- This reactor constraint is used as external constraint or prior to enhance sensitivity to other parameters.



# NOVA RESULTS



- Mild preference for:
- Normal ordering
- $\sin^2\theta_{23} > 0.5$
- CP violation
- cons. for NO, viol. for IO
- tension with T2K



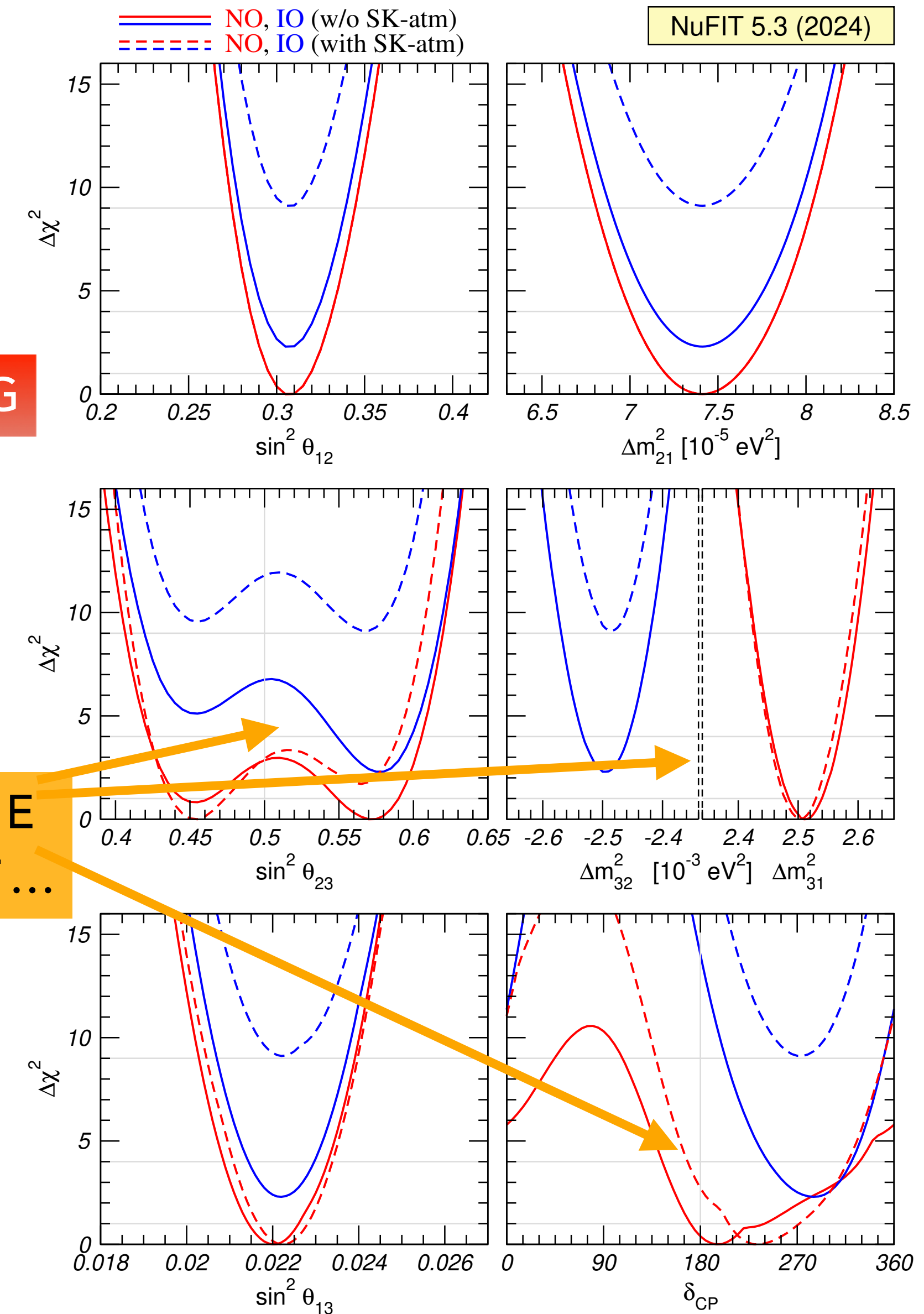
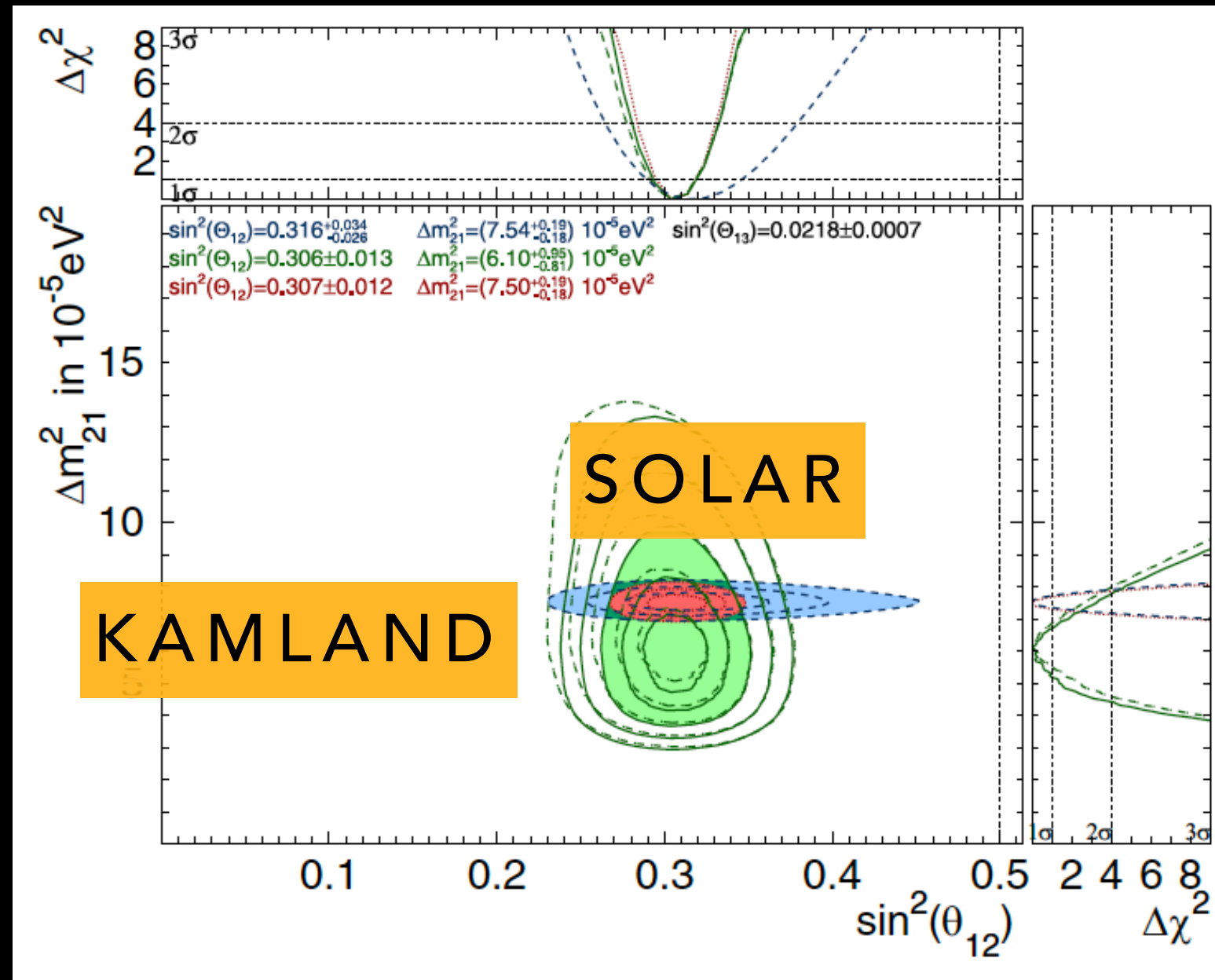
# GLOBAL FITS

# GLOBAL OSCILLATION FITS



- Consistent results favoring the 3-flavor neutrino oscillation framework
- Best precision for the parameters comes from combination of all available solar, reactor, atmospheric and accelerator data
- Tension may point to new physics... or the need for more data...

[HTTP://WWW.NU-FIT.ORG](http://www.nu-fit.org)



NOT QUITE THERE YET...

# GLOBAL FITS RESULTS



parameter	best fit $\pm 1\sigma$	$3\sigma$ range
$\Delta m_{21}^2$ [ $10^{-5}\text{eV}^2$ ]	$7.55^{+0.22}_{-0.20}$	6.98–8.19
$ \Delta m_{31}^2 $ [ $10^{-3}\text{eV}^2$ ] (NO)	$2.51^{+0.02}_{-0.03}$	2.43–2.58
$ \Delta m_{31}^2 $ [ $10^{-3}\text{eV}^2$ ] (IO)	$2.41^{+0.03}_{-0.02}$	2.34–2.49
$\sin^2 \theta_{12}/10^{-1}$	$3.04^{\pm 0.16}$	2.57–3.55
$\sin^2 \theta_{23}/10^{-1}$ (NO)	$5.64^{+0.15}_{-0.21}$	4.23–6.04
$\sin^2 \theta_{23}/10^{-1}$ (IO)	$5.64^{+0.15}_{-0.18}$	4.27–6.03
$\sin^2 \theta_{13}/10^{-2}$ (NO)	$2.20^{+0.05}_{-0.06}$	2.03–2.38
$\sin^2 \theta_{13}/10^{-2}$ (IO)	$2.20^{+0.07}_{-0.04}$	2.04–2.38
$\delta/\pi$ (NO)	$1.12^{+0.16}_{-0.12}$	0.76–2.00
$\delta/\pi$ (IO)	$1.50^{+0.13}_{-0.14}$	1.11–1.87

[HTTPS://GLOBALFIT.ASTROPARTICLES.ES/](https://globalfit.astroparticles.es/)

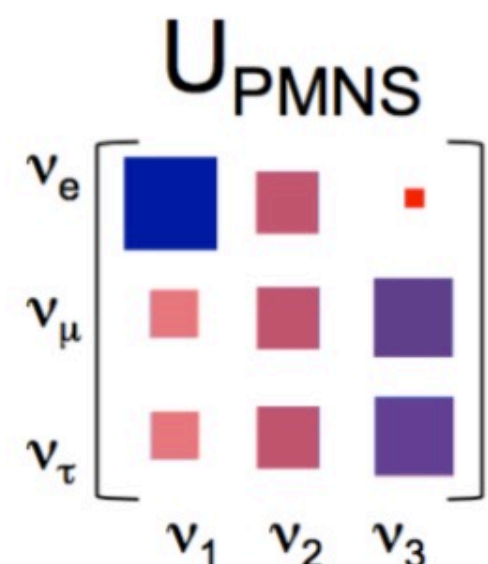
# PMNS VS. CKM



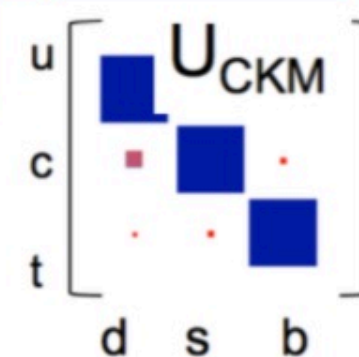
$$|U_{\text{PMNS}}| \sim \begin{pmatrix} 0.8 & 0.5 & 0.1 \\ 0.5 & 0.6 & 0.7 \\ 0.3 & 0.6 & 0.7 \end{pmatrix}$$

far from diagonal -  
two large angles  $\delta_{\text{CP}} = ?$

$$J_{\text{CP}}^{\text{quarks}} = (2.96^{+0.20}_{-0.16}) \times 10^{-5}$$



Mixing	Neutrinos	Quarks
$\theta_{12}$	$(33.6 \pm 0.8)^\circ$	$(13.04 \pm 0.05)^\circ$
$\theta_{23}$	$(45 \pm 3)^\circ$	$(2.38 \pm 0.06)^\circ$
$\theta_{13}$	$(8.5 \pm 0.15)^\circ$	$(0.201 \pm 0.011)^\circ$
$\delta_{\text{CP}}$	$(-90 ?)^\circ$	$(67 \pm 5)^\circ$



almost diagonal -  
all angles small

$$|V_{\text{CKM}}| \sim \begin{pmatrix} 1 & 0.2 & 0.004 \\ 0.2 & 1 & 0.04 \\ 0.008 & 0.04 & 1 \end{pmatrix}$$

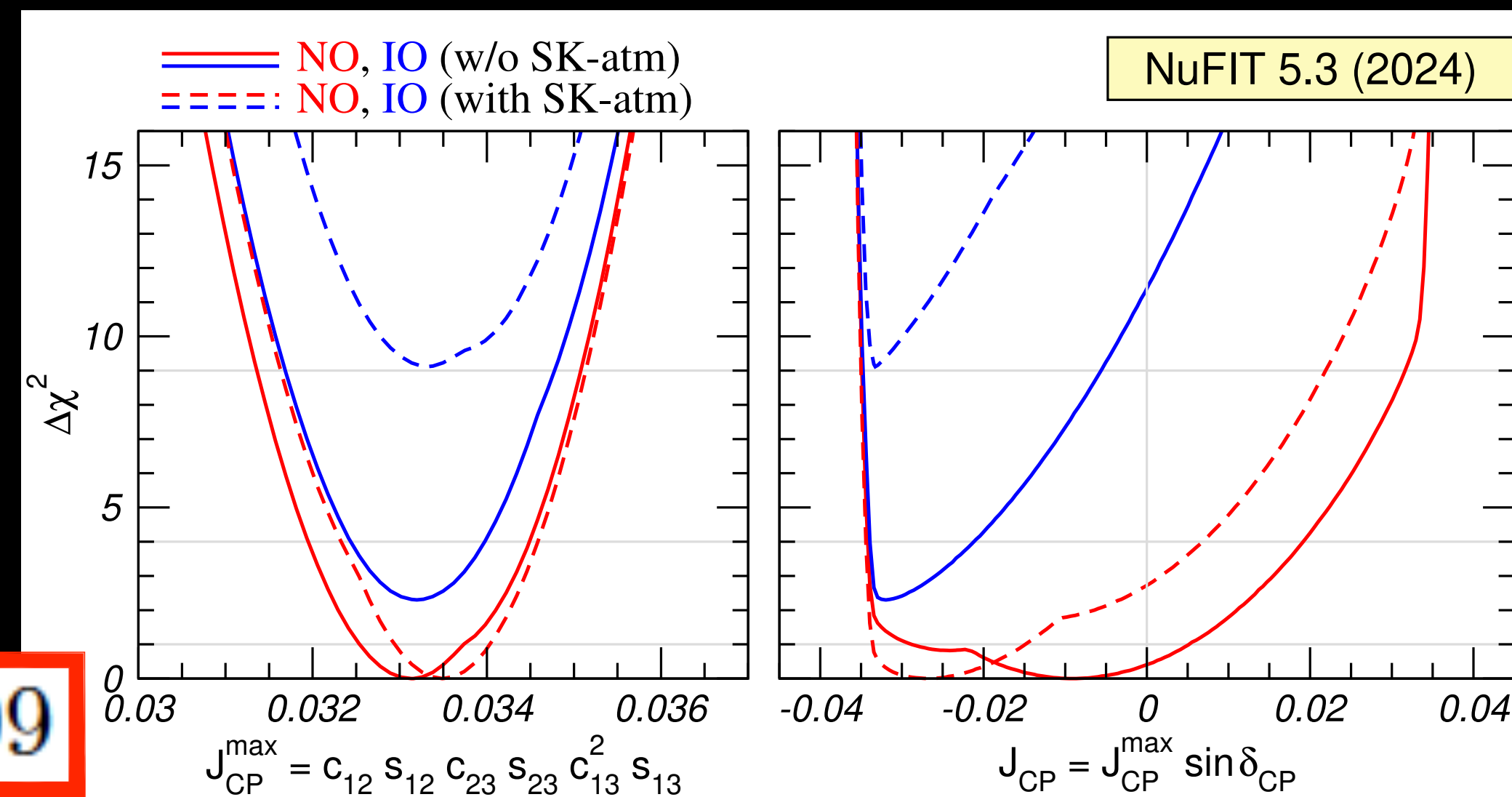
$$\delta_{\text{CP}} = 68^\circ$$

$$\equiv J_{\text{CP}}^{\text{max}} \sin \delta_{\text{CP}}$$

$$J_{\text{CP}}^{\text{max}} = \cos \theta_{12} \sin \theta_{12} \cos \theta_{23} \sin \theta_{23} \cos^2 \theta_{13} \sin \theta_{13}$$

- CP violation effects proportional to Jarlskog invariant, depends on angles too
- With neutrinos can be 3 orders of magnitude larger than with quarks!

$$J_{\text{CP}}^{\text{max}} = 0.0329 \pm 0.0009$$

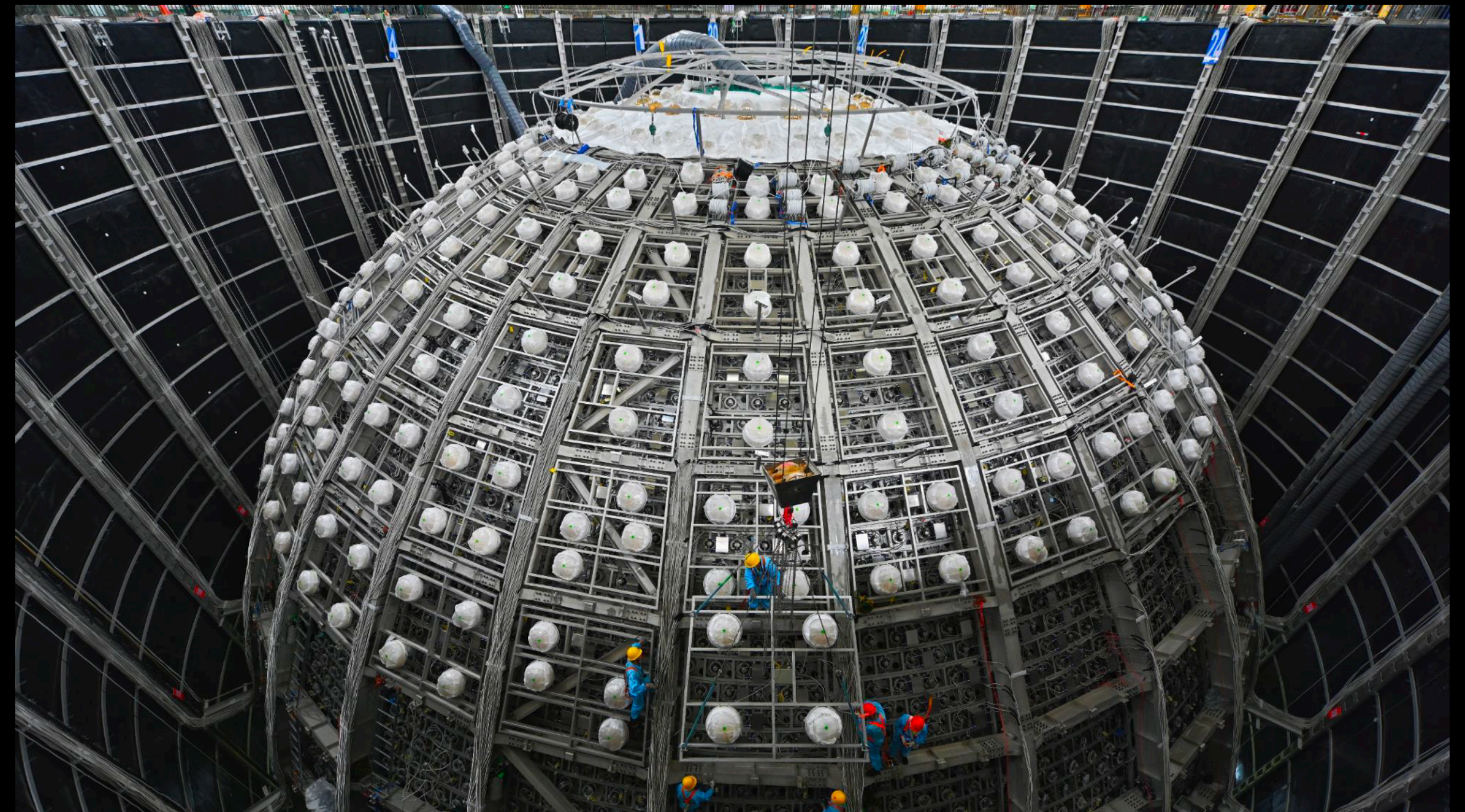
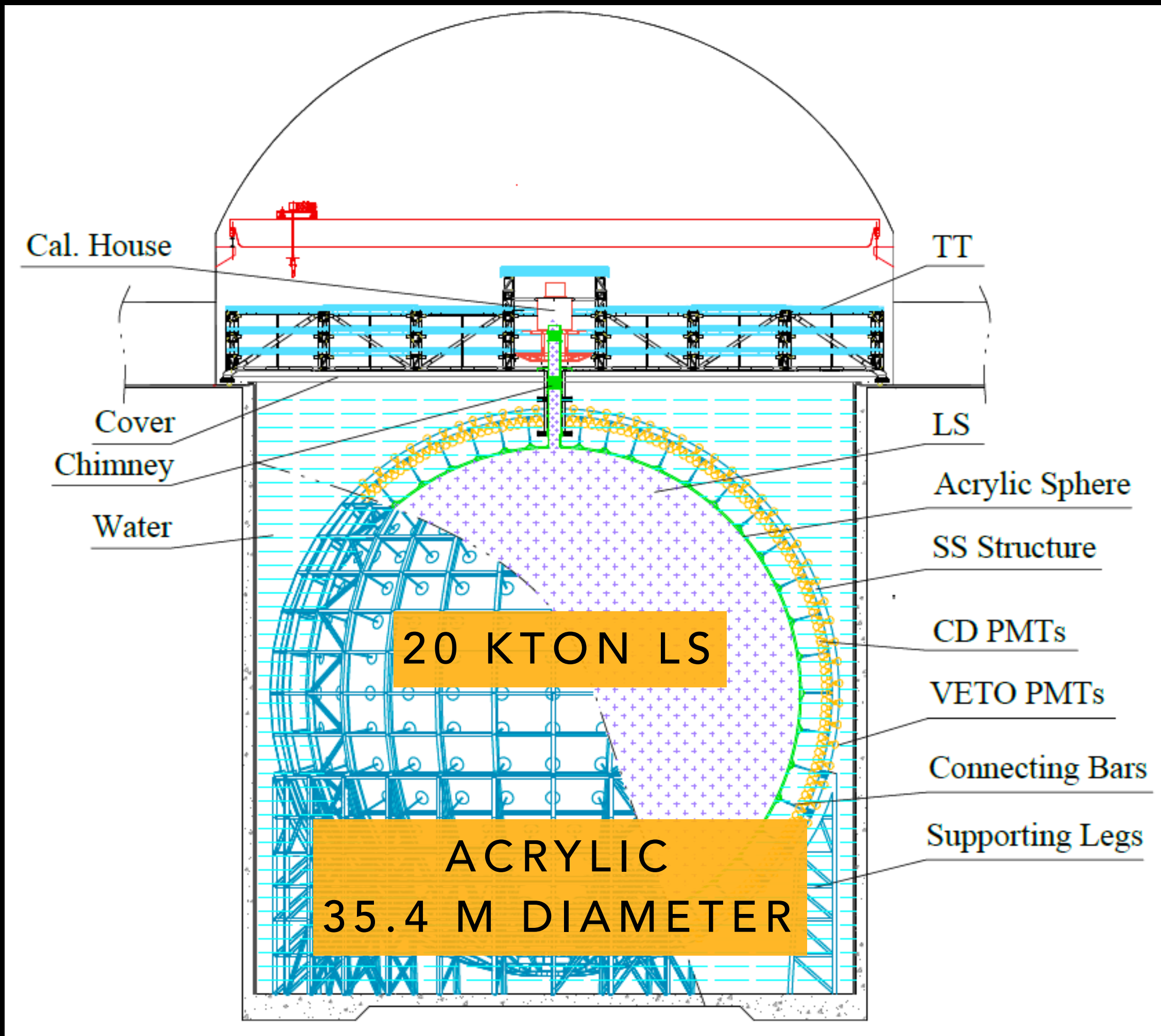


# FUTURE EXPERIMENTS

# JUNO REACTOR EXPERIMENT



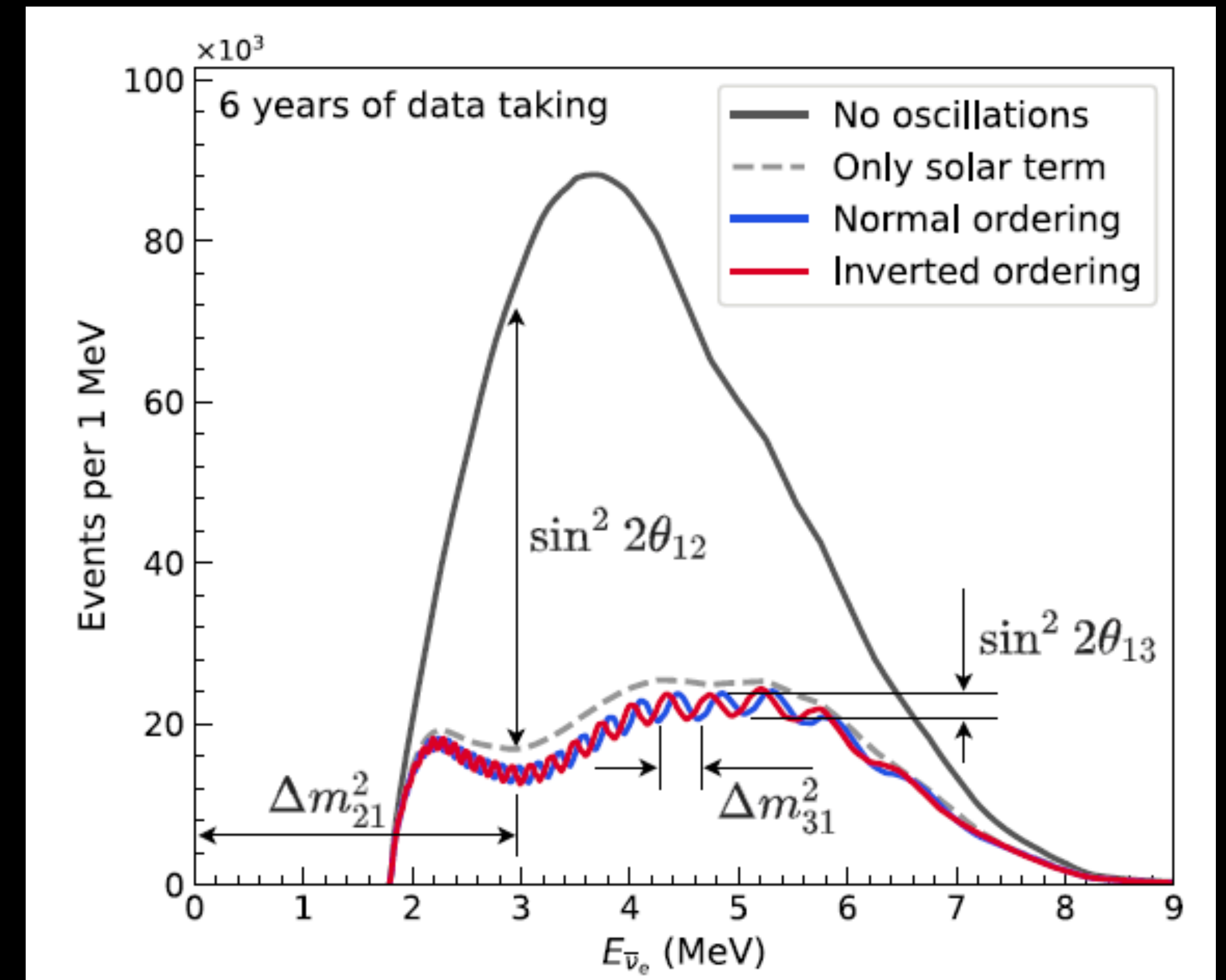
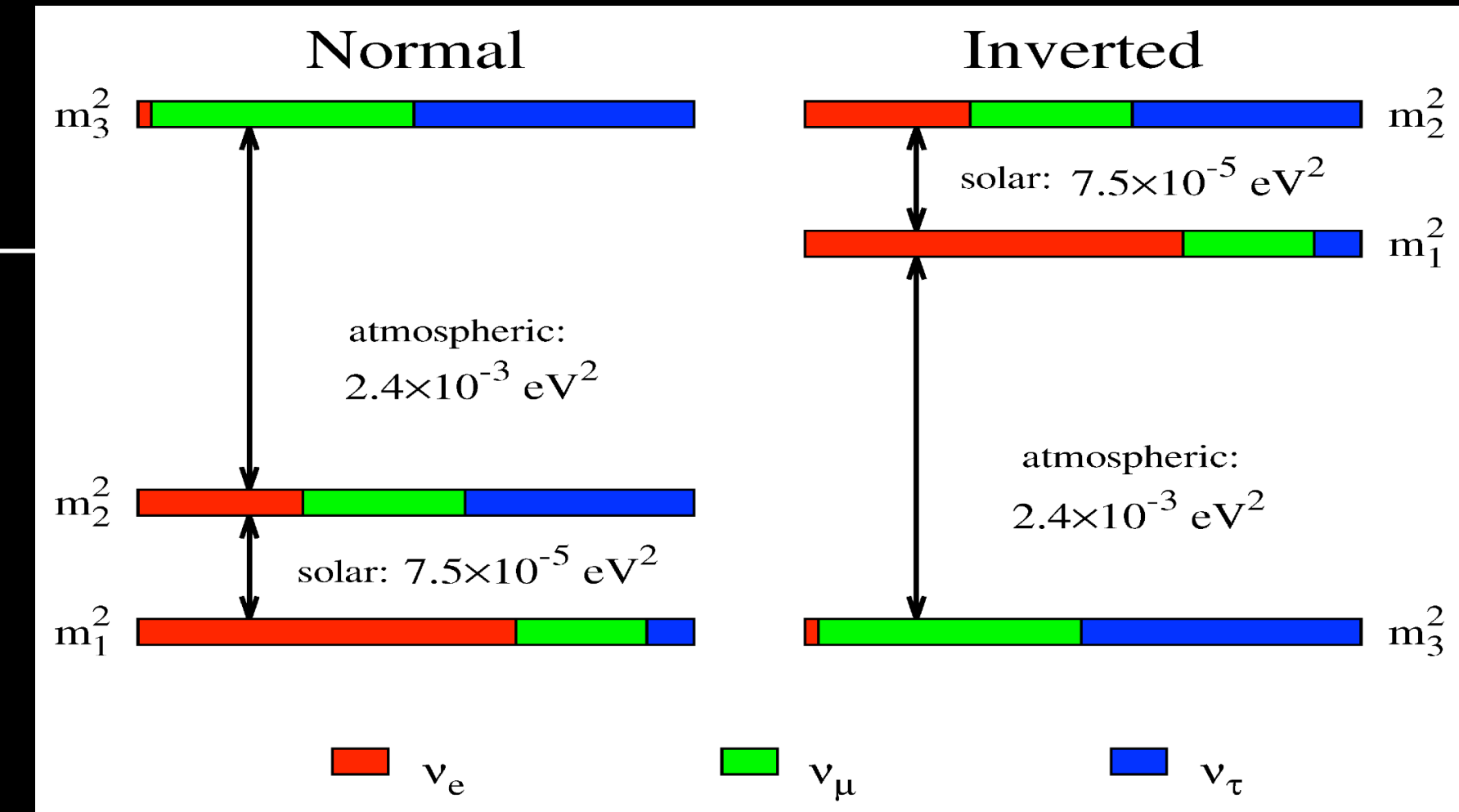
- Follow-up of Daya Bay
- Biggest liquid scintillator (LS) detector ever
- 17612 20-inch PMTs, 25600 3-inch PMTs
- 50 km baseline to powerful reactors
- Starting 2025



# JUNO PHYSICS



- By definition  $\Delta m_{31}^2 = \Delta m_{32}^2 + \Delta m_{21}^2$
- We know that  $\Delta m_{21}^2 > 0$  (MSW solar)
- How to determine the mass ordering?
  - Normal:  $|\Delta m_{31}^2| = |\Delta m_{32}^2| + \Delta m_{21}^2$
  - Inverted:  $|\Delta m_{31}^2| = |\Delta m_{32}^2| - \Delta m_{21}^2$
  - But the difference is small, since  $\Delta m_{21}^2 \approx 3\% \times |\Delta m_{32}^2|$
- Requires distinguishing small details in oscillation pattern
- Expected energy resolution: 2.95% @1MeV
- Expected  $3\sigma$  sensitivity @  $\sim 6 \text{ yrs} * 26.6 \text{ GWth}$





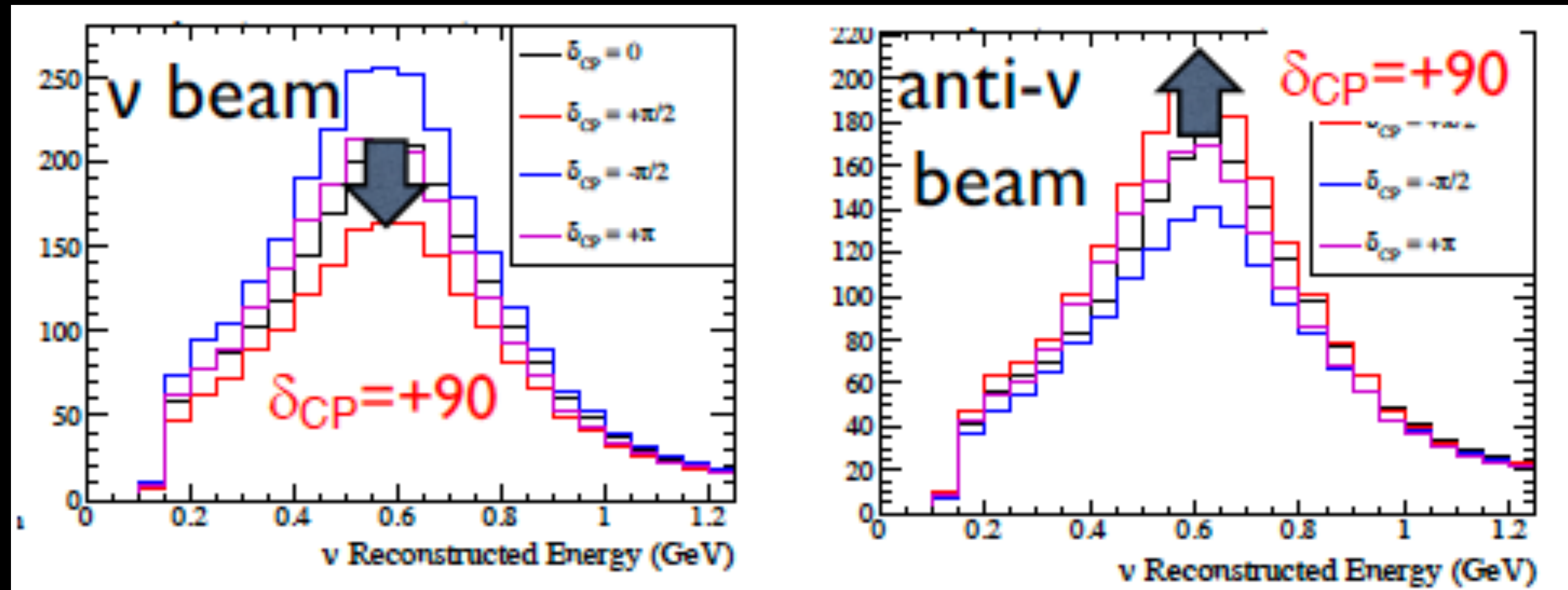
# HYPER-KAMIOKANDE



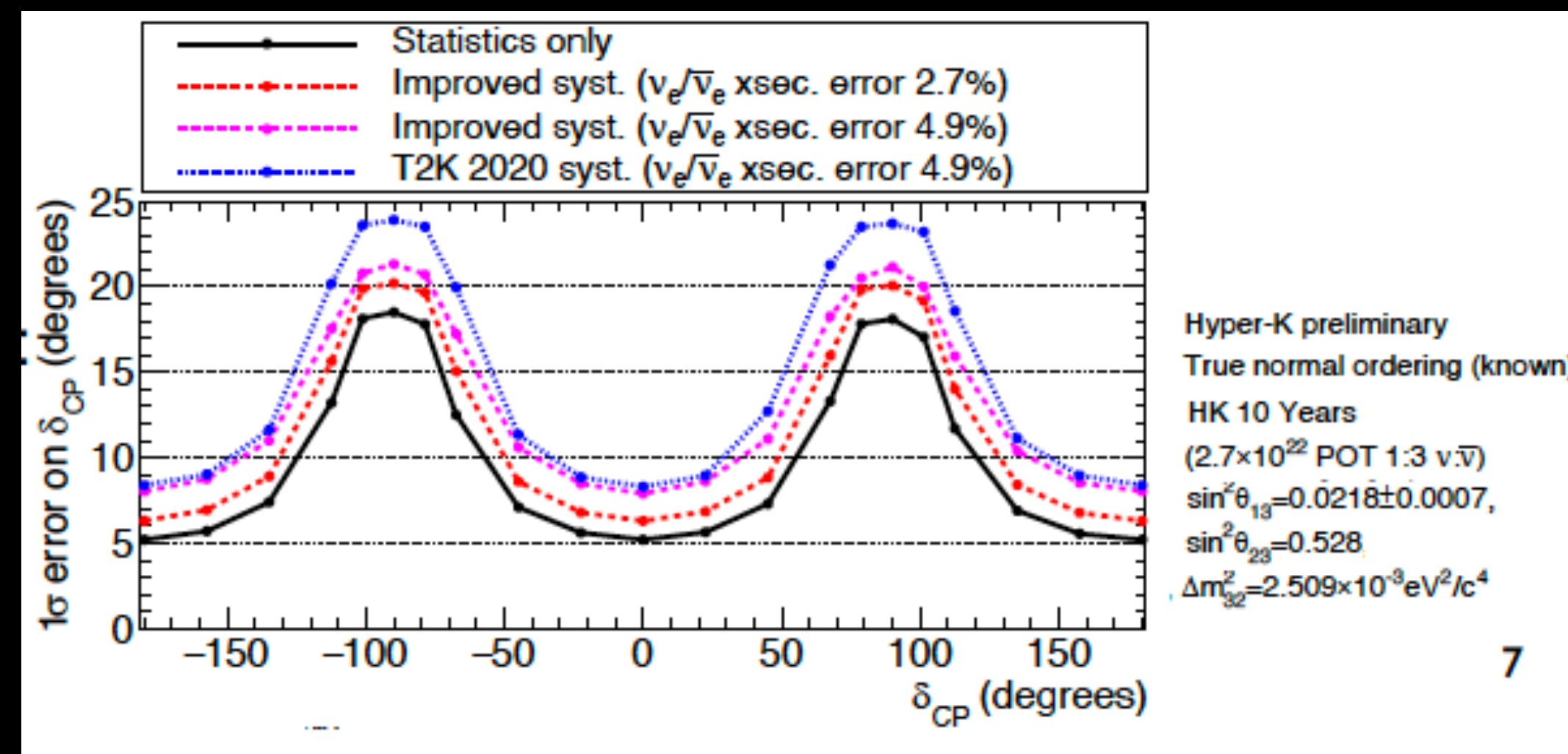
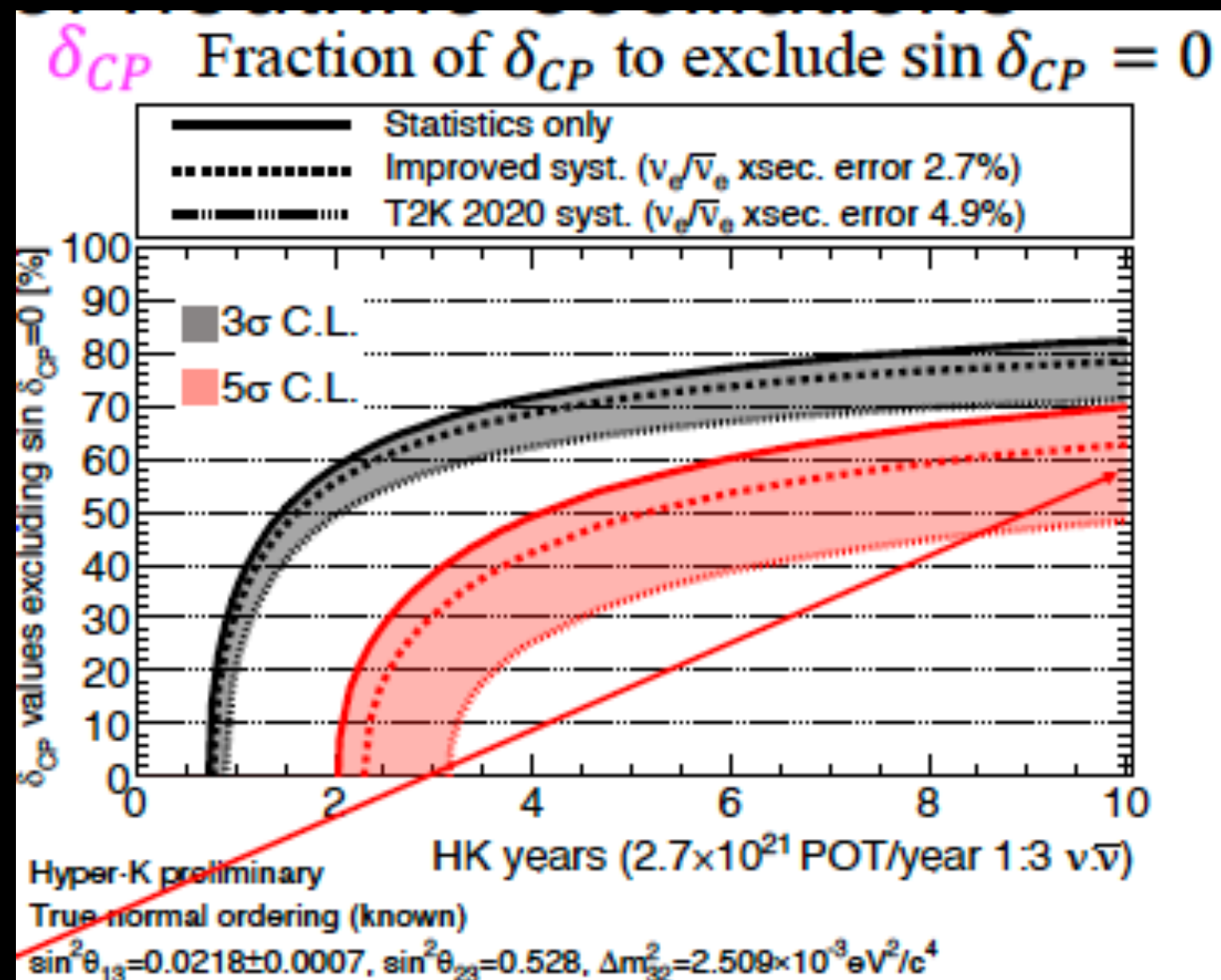
- 260 kton (188 kt fiducial)
- upgrade of the T2K beam and near detectors
- 2.5 deg off-axis
- upgraded PMTs with better QE and timing
- cavity in construction
- expect start of data in 2027



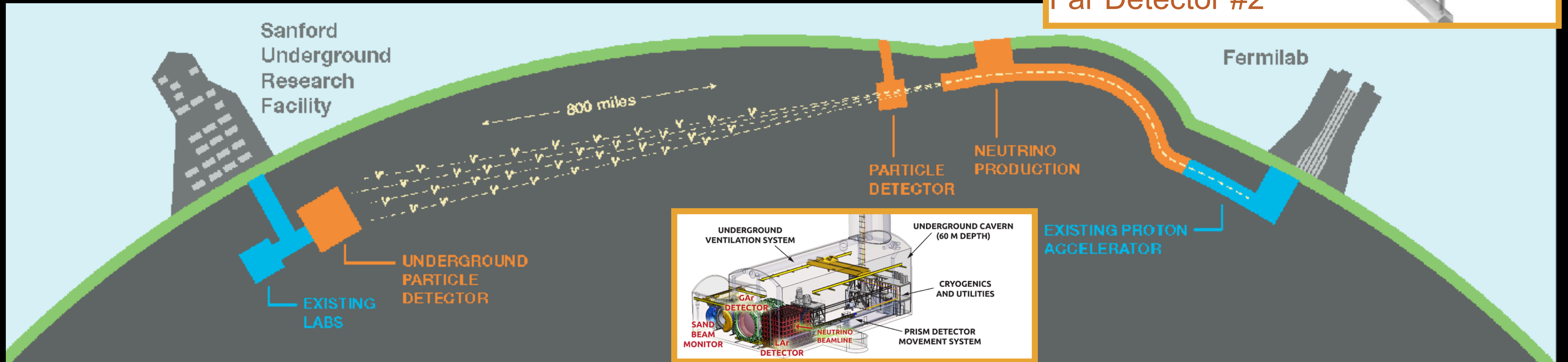
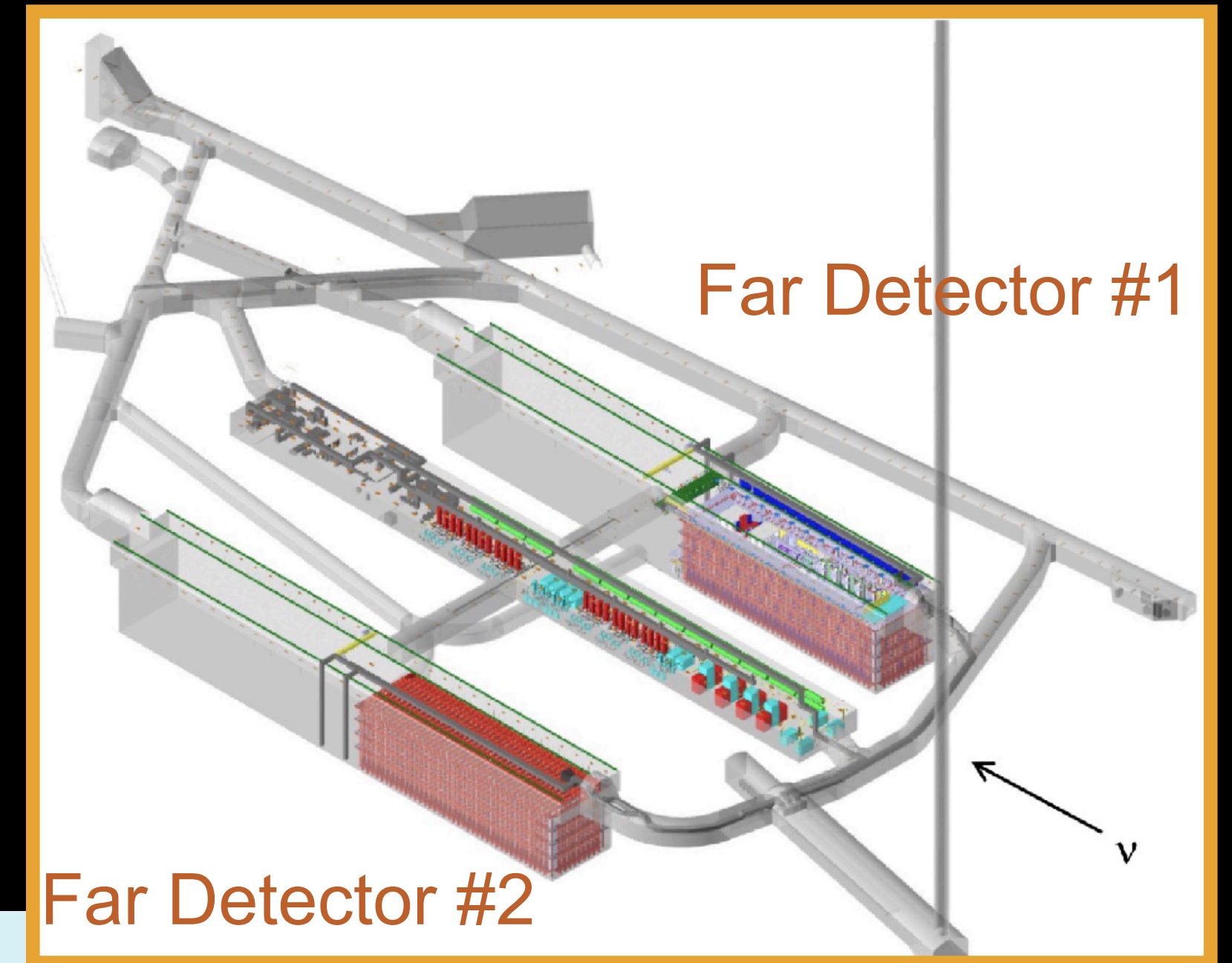
# HK PROJECTED SENSITIVITY



- $\nu_e(\bar{\nu}_e)$  appearance in  $\nu_\mu(\bar{\nu}_\mu)$  beam
- Energy < 1 GeV: mostly QE
- Short distance: small matter effects
- Very high statistics  $\rightarrow$  CP violation discovery ( $5\sigma$ ) in 60% of the values in 10yrs

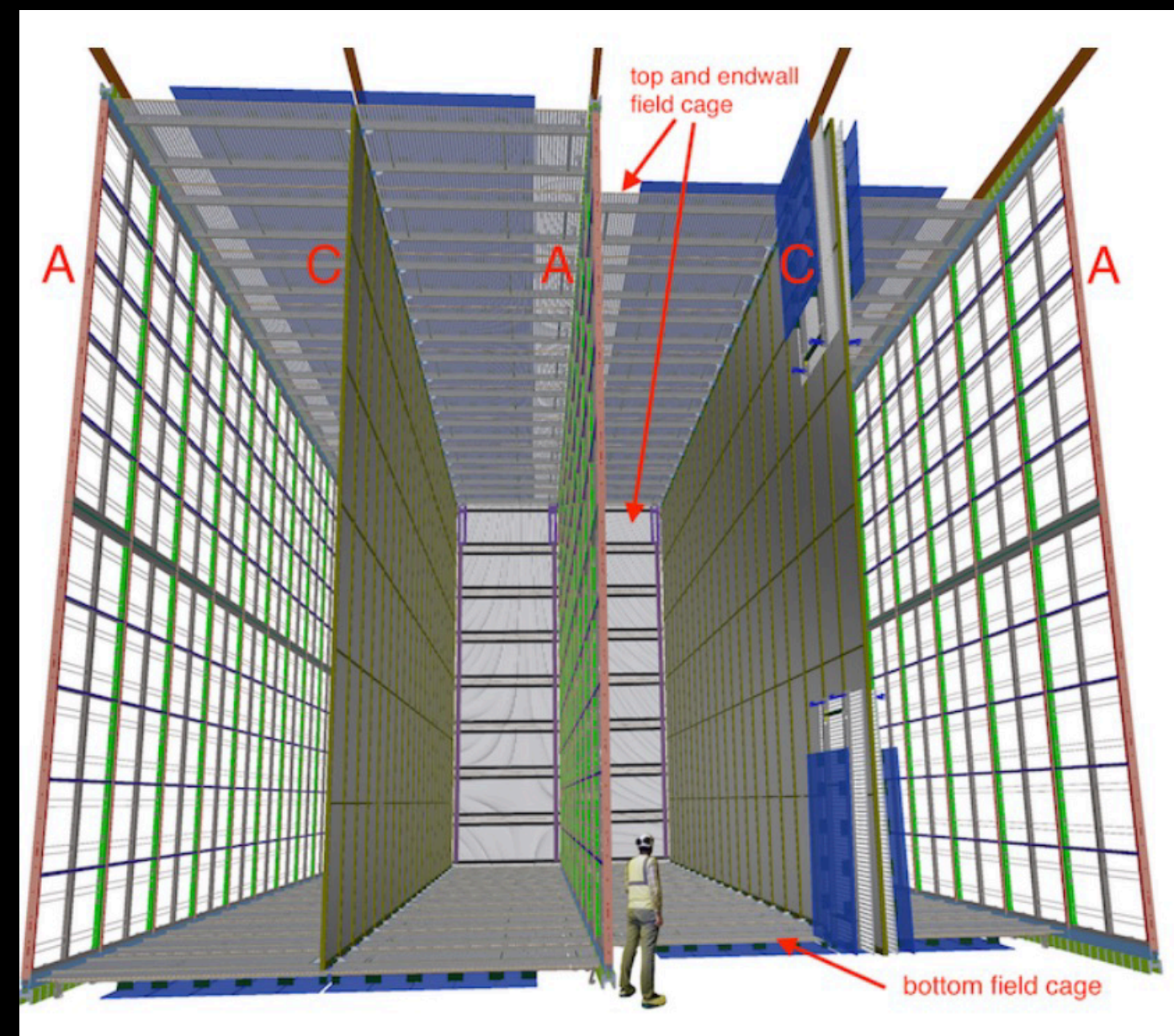
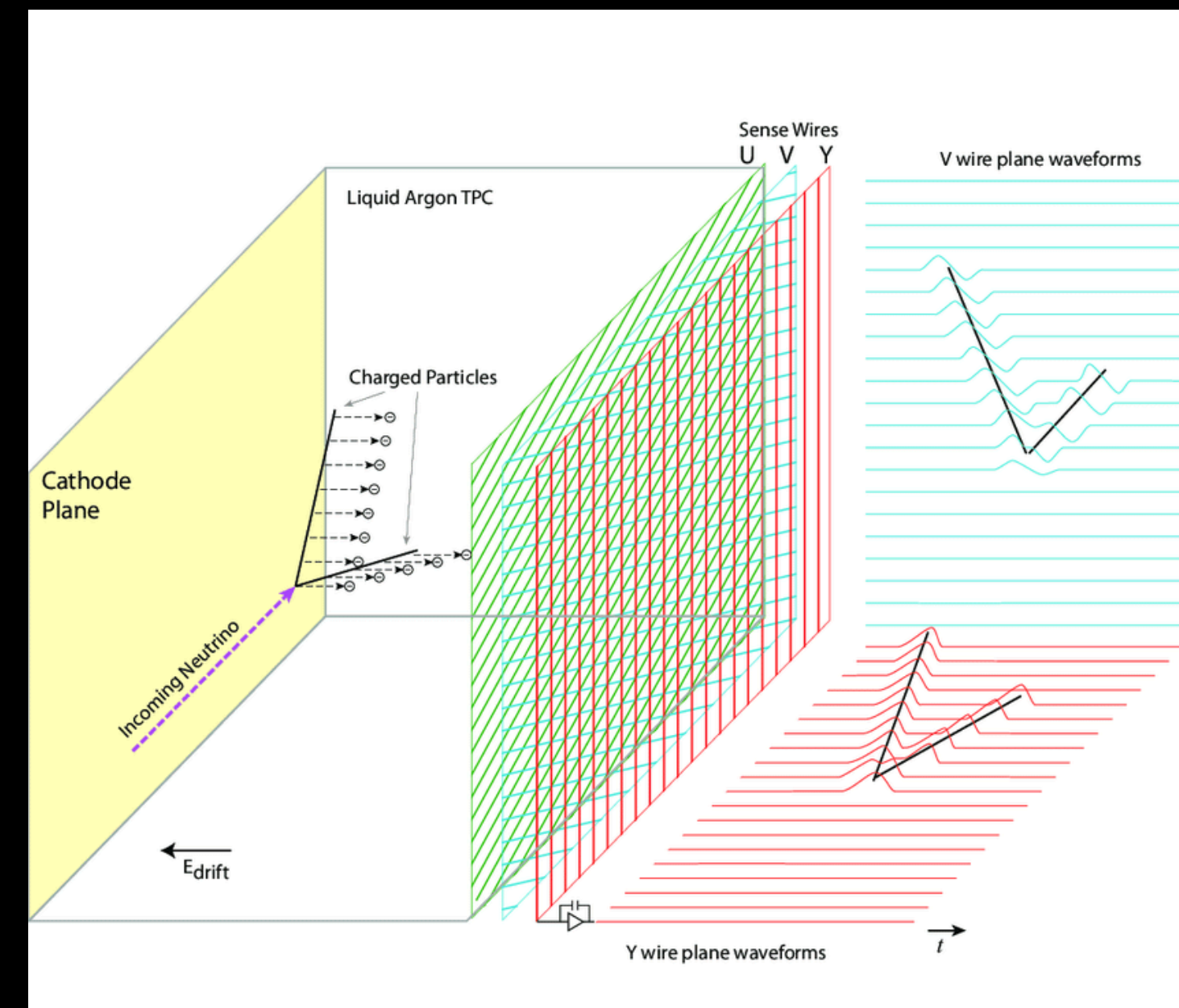
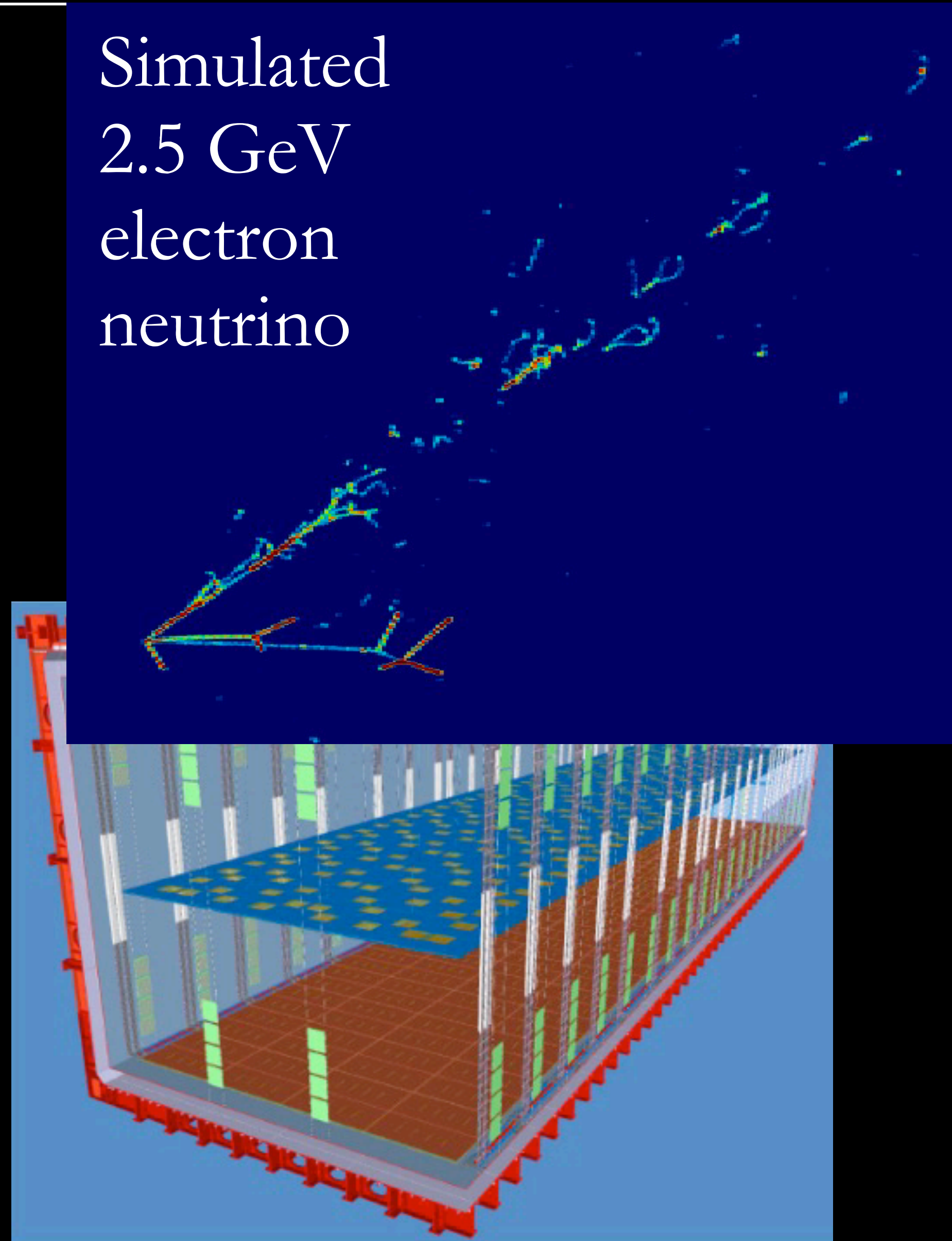


- DUNE overview
  - Fermilab makes intense  $\nu_\mu$  and  $\bar{\nu}_\mu$  beams
  - Near Detector characterizes beam and cross-sections
  - Beams reach Sanford lab, 1285 km away, 1.5 km underground
  - 70 kt Far Detector, divided in 4 modules, at least 3 of which use LArTPC technology (see lecture 2)



- Liquid Argon Time Projection Chambers
  - Horizontal Drift (Far Detector 1)
  - Vertical Drift (Far Detector 2, possibly 3)
- Precision tracking (5 mm wire pitch)
- Detects all charges -> full calorimetry
- Full event ( $\nu$  ID and energy) reconstruction

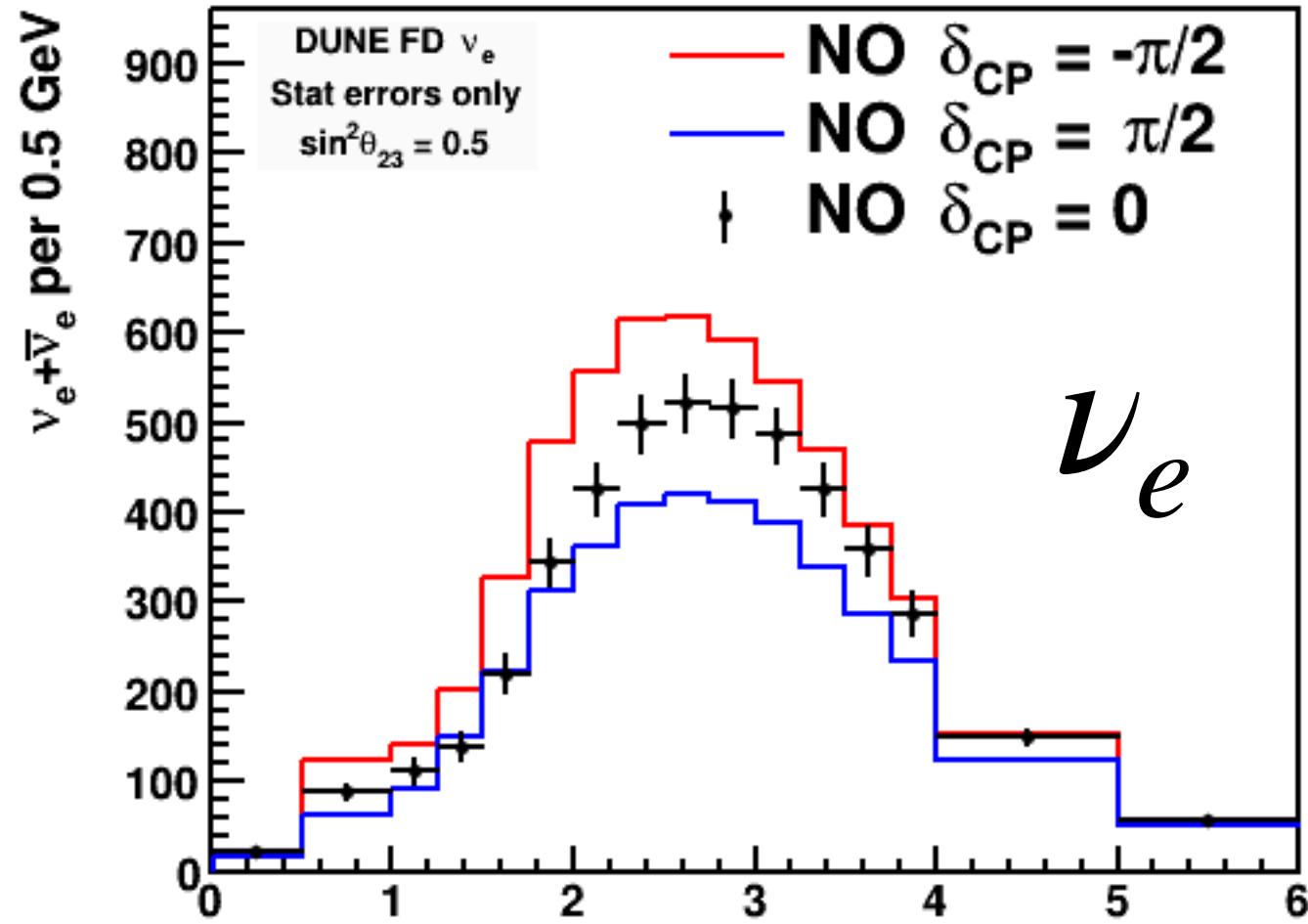
Simulated  
2.5 GeV  
electron  
neutrino



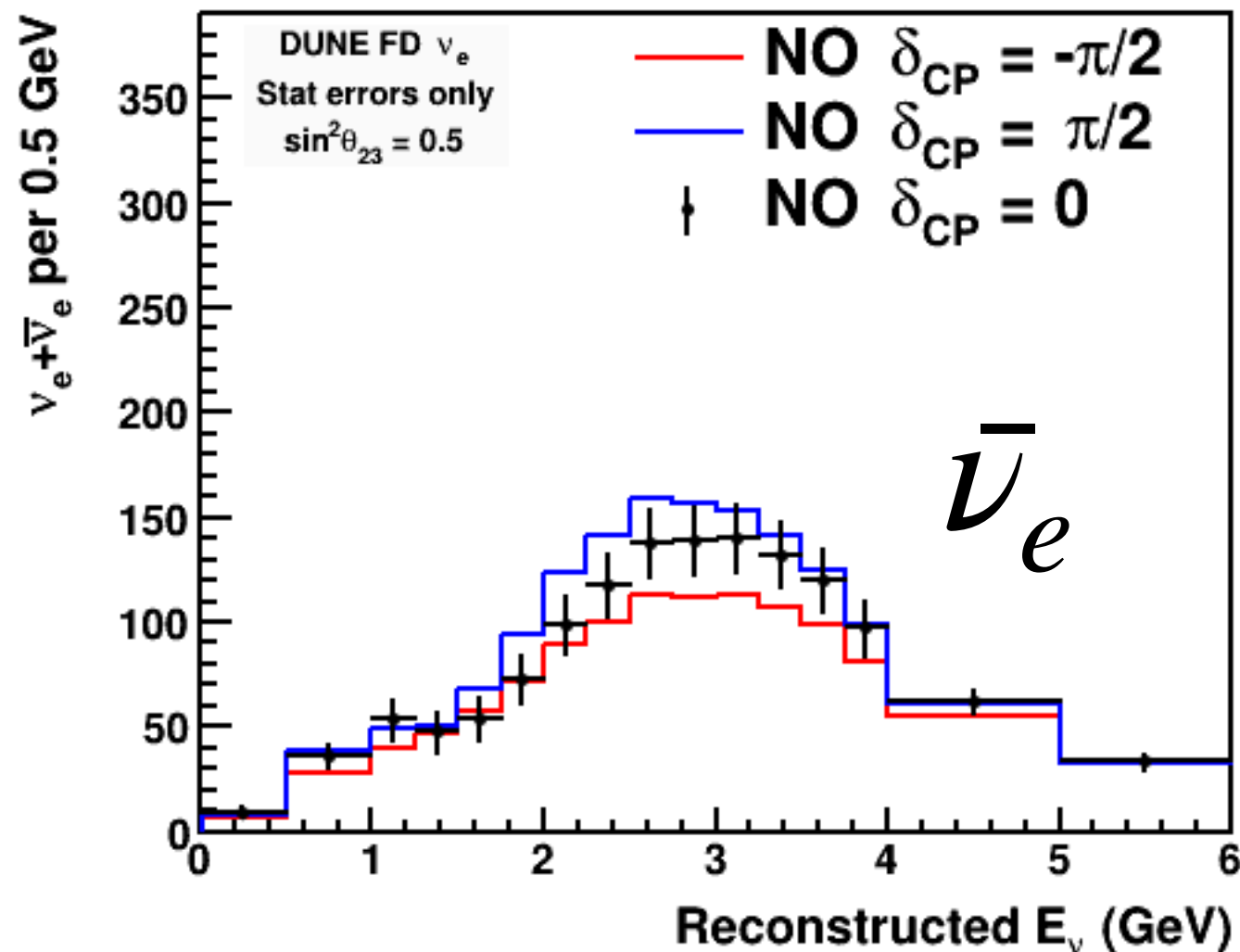
# DUNE EXPECTED SPECTRA



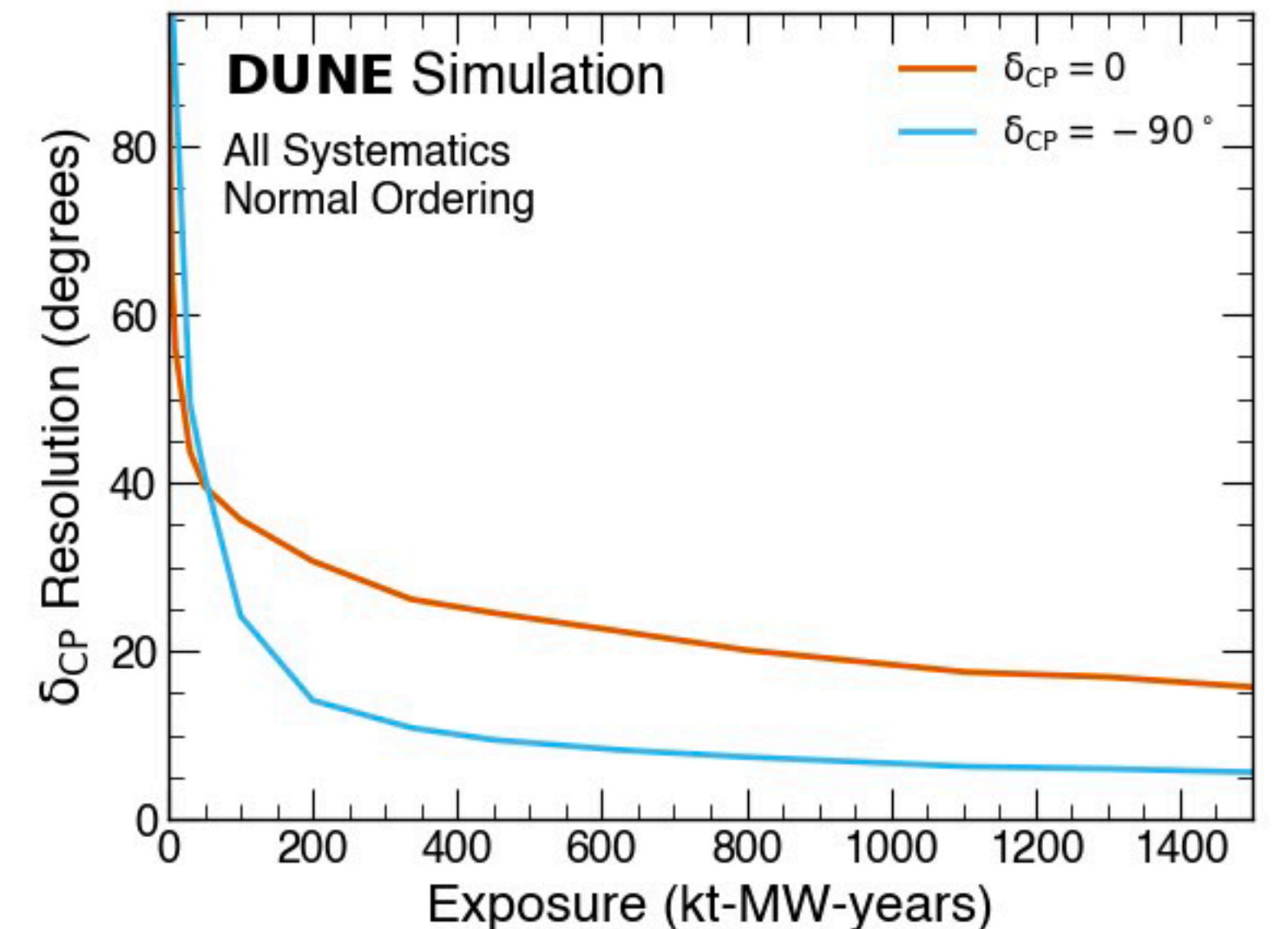
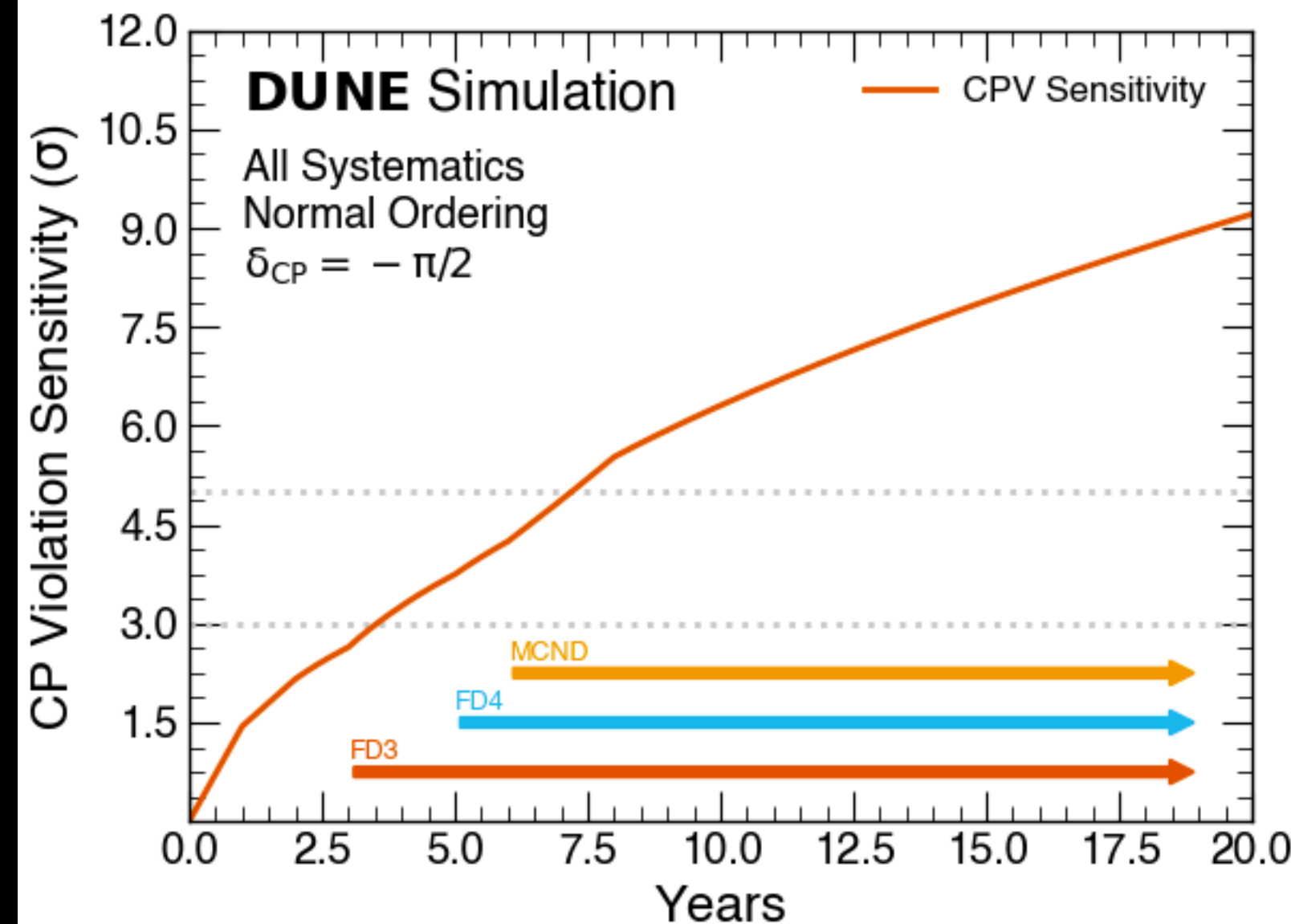
FHC 20kt 2.8E21 POT +  
40kt 6.6E21 POT



RHC 20kt 2.2E21 POT +  
40kt 6.6E21 POT



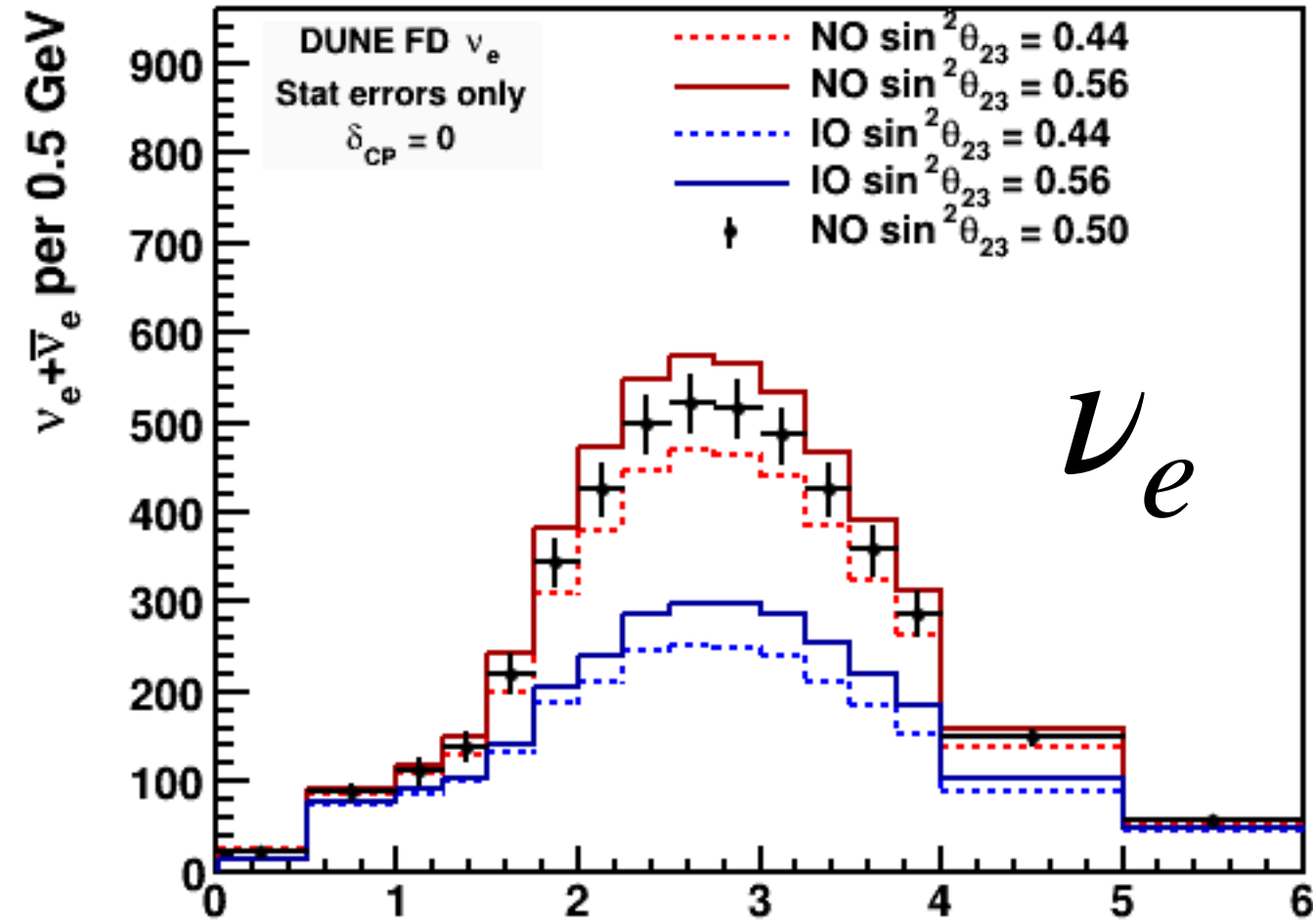
- Wide-band beam: two oscillation minima (p.33)
- If  $\delta_{CP} \sim -\pi/2$ , DUNE will measure an enhancement in  $\nu_e$  appearance, and a reduction in  $\bar{\nu}_e$  appearance



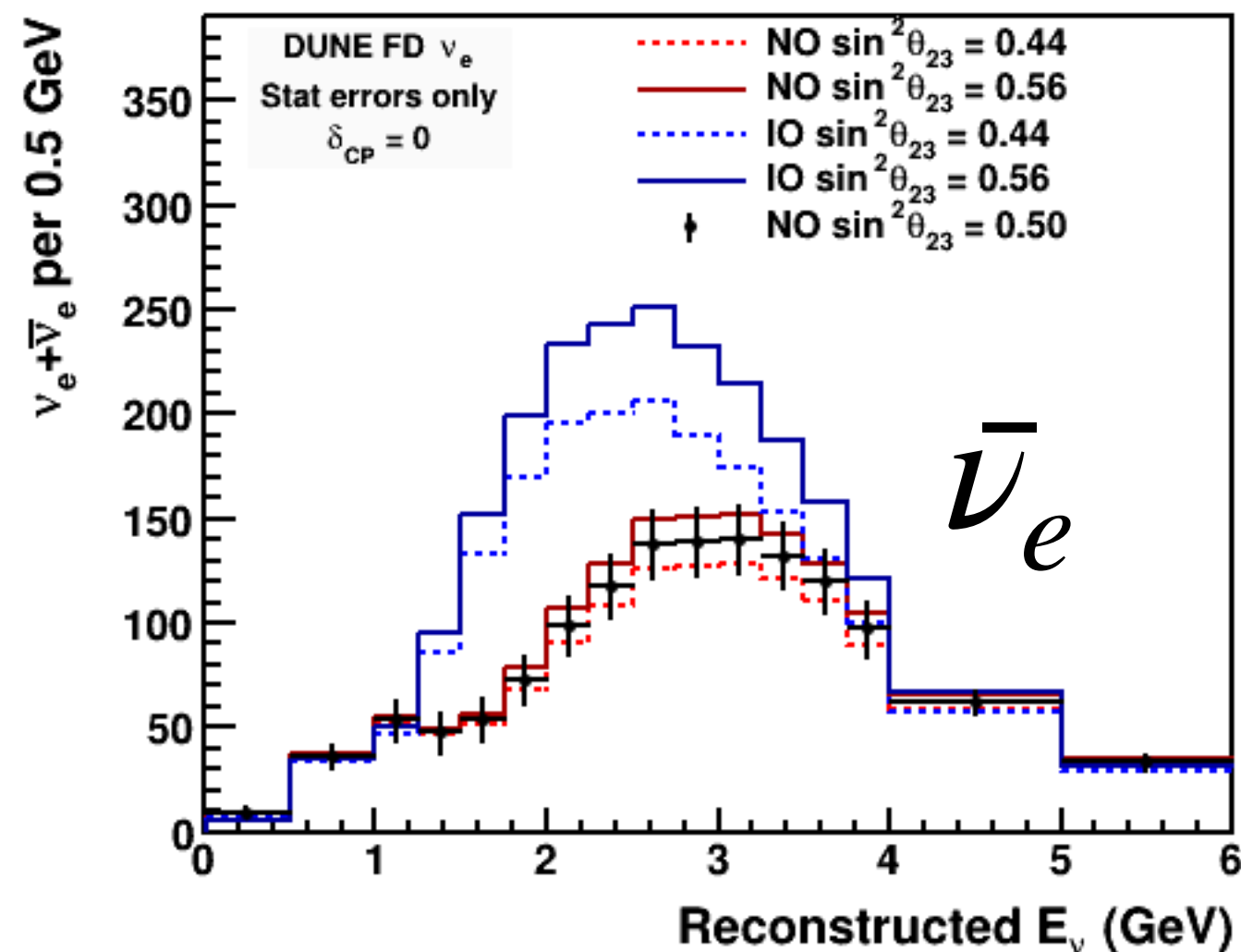
# DUNE EXPECTED SPECTRA



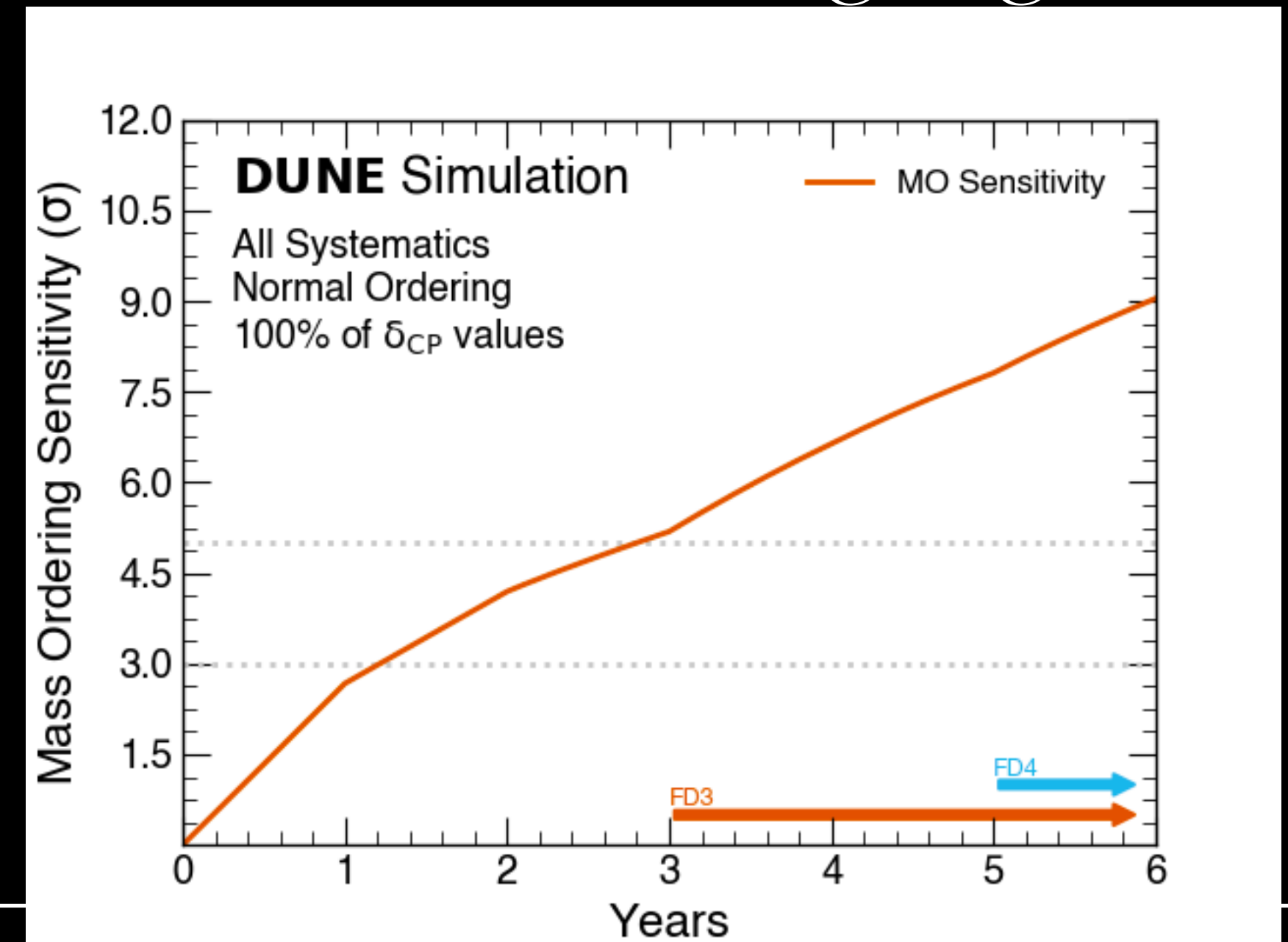
FHC 20kt 2.8E21 POT +  
40kt 6.6E21 POT



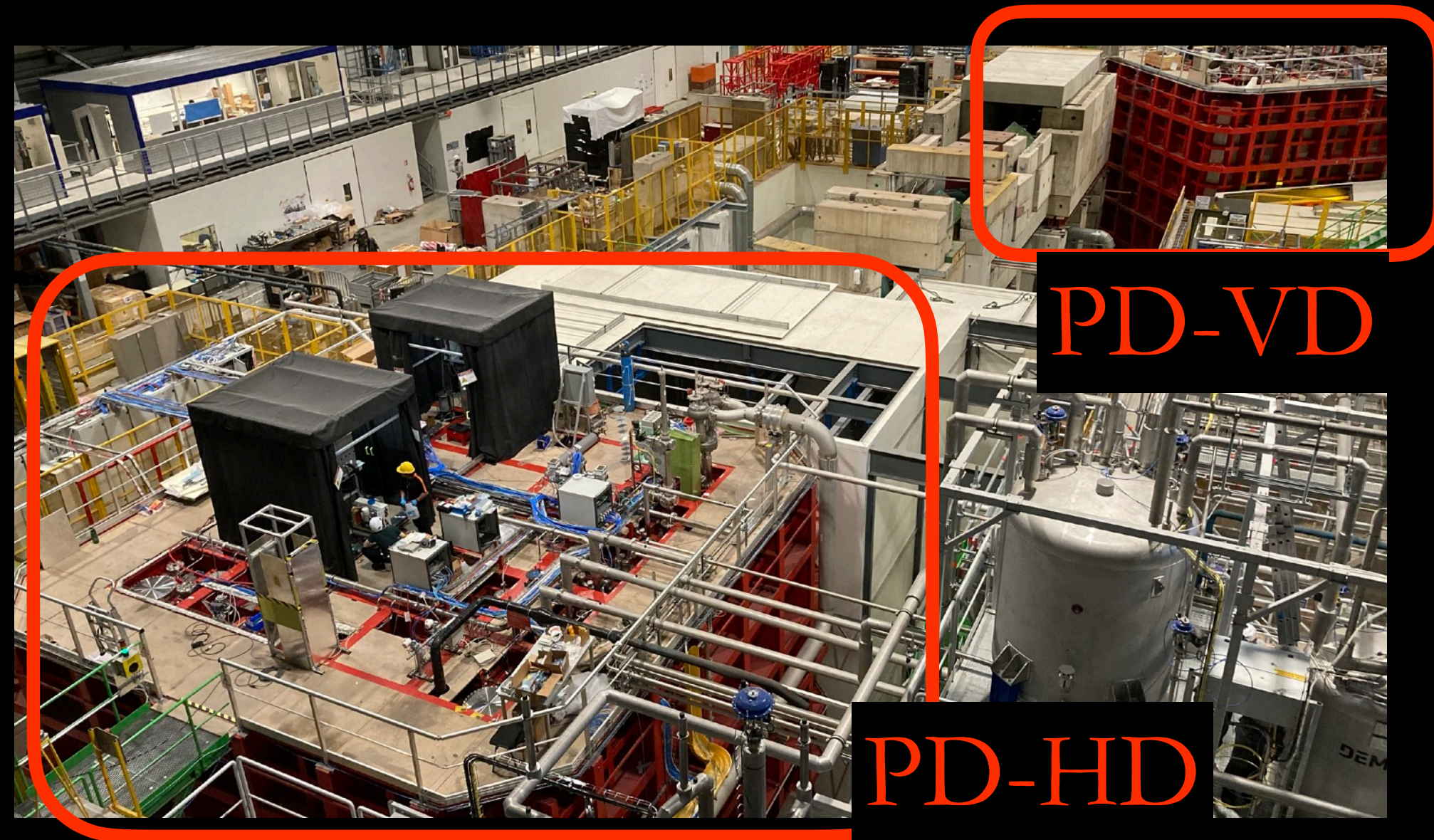
RHC 20kt 2.2E21 POT +  
40kt 6.6E21 POT



- Long baseline gives DUNE sensitivity to mass ordering (MO) through matter effects
- If the mass ordering is normal, DUNE will measure a much larger enhancement in  $\nu_e$  appearance, and a reduction in  $\bar{\nu}_e$  appearance
- MO,  $\delta_{CP}$ , and  $\theta_{23}$  all affect spectra with different shapes  $\rightarrow$  additional handle on resolving degeneracies



# DUNE AND PROTODUNE STATUS



- ProtoDUNEs @ CERN
- HD detector taking data with beam, cosmics and calibration systems
- VD detector starting in the fall
- Far Detector
- Excavation complete, installation in 2026-27
- Physics in 2028 or early 2029
- Beam physics with Near Detector 2031

